



# Recent Developments in Heavy-Ion Theory

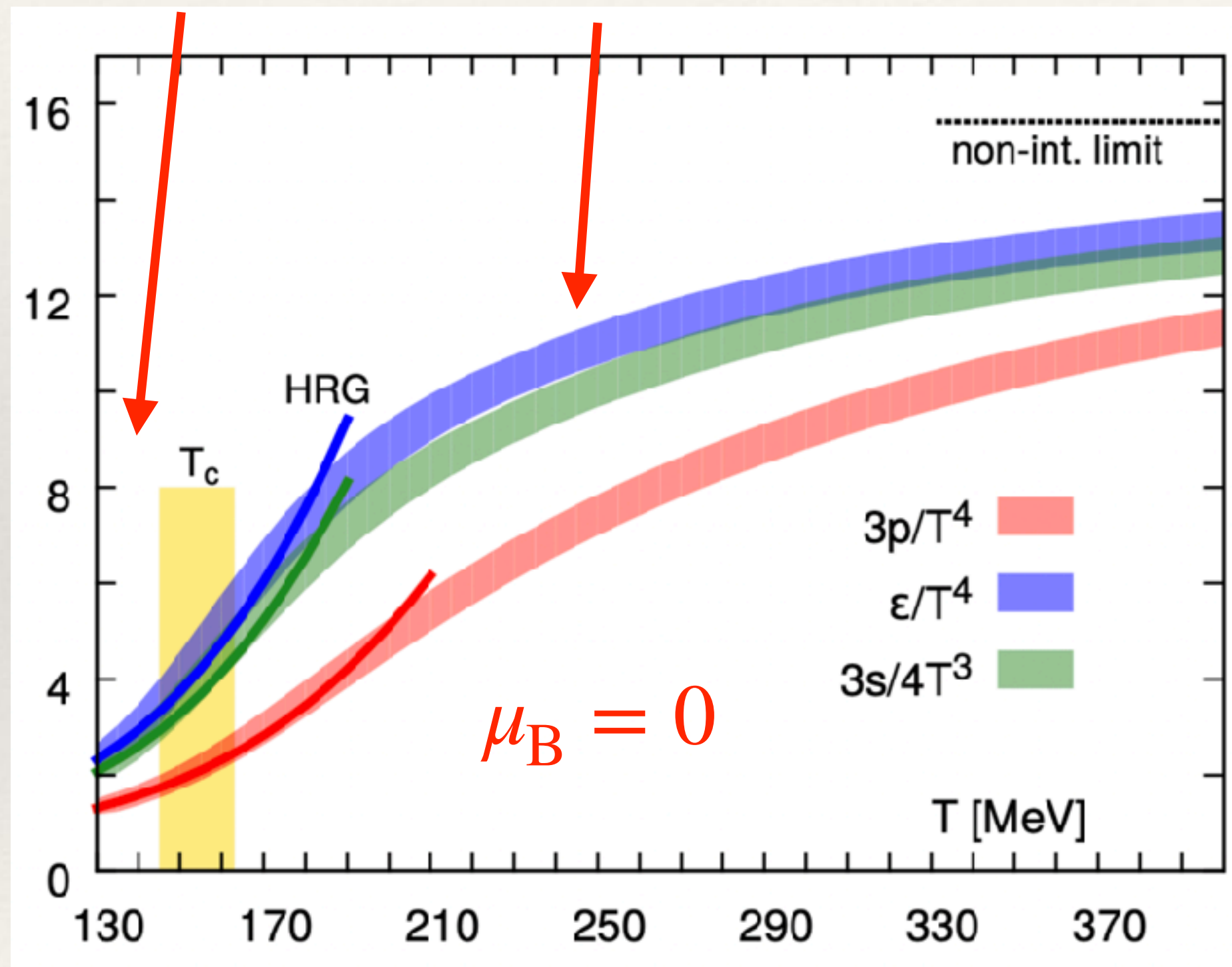


**Shanshan Cao**  
***Shandong University***

# QCD matter under extreme conditions

## Lattice equation of state

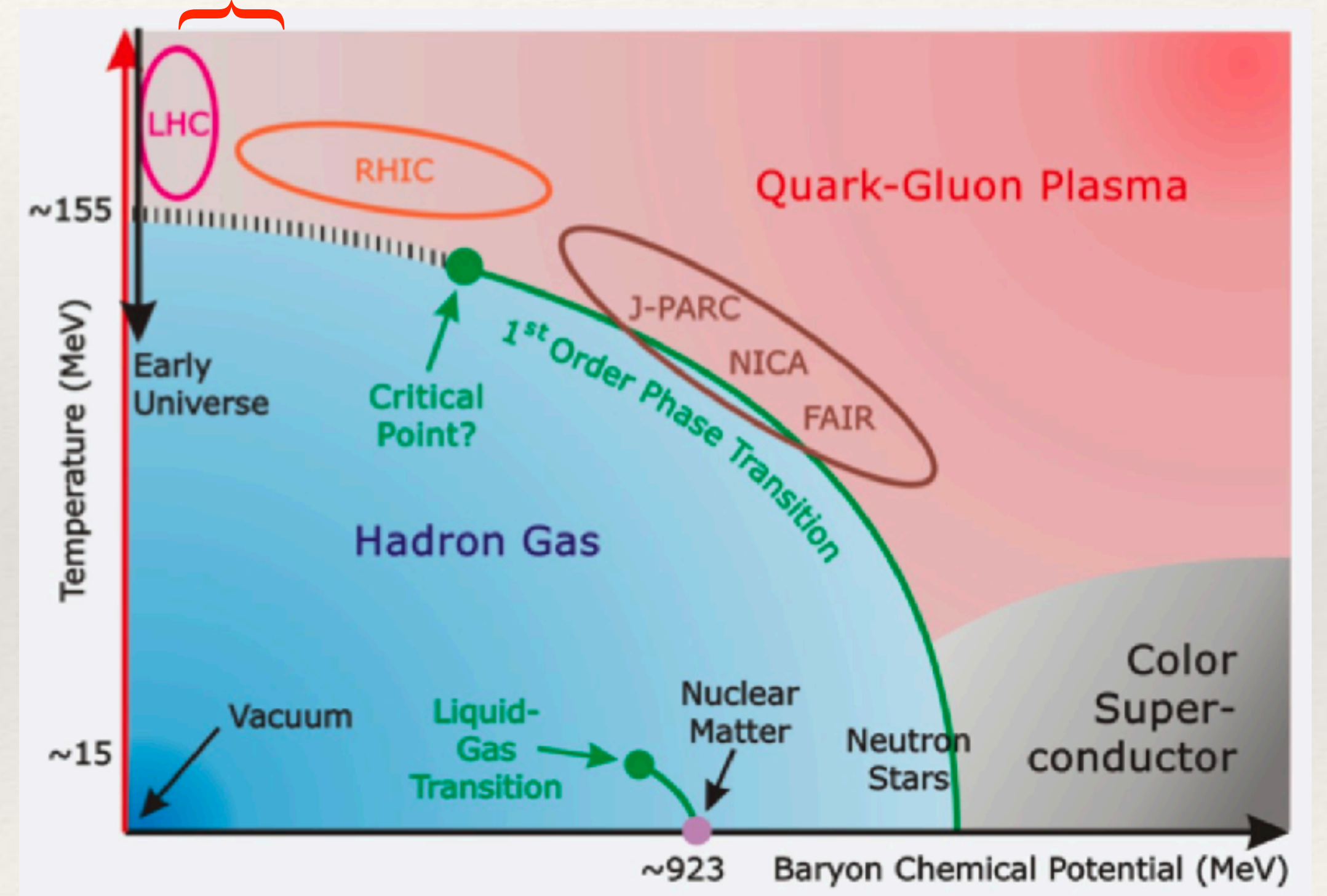
hadron gas      quark-gluon plasma



[ HotQCD, Phys. Rev. D 90 (2014) 094503 ]

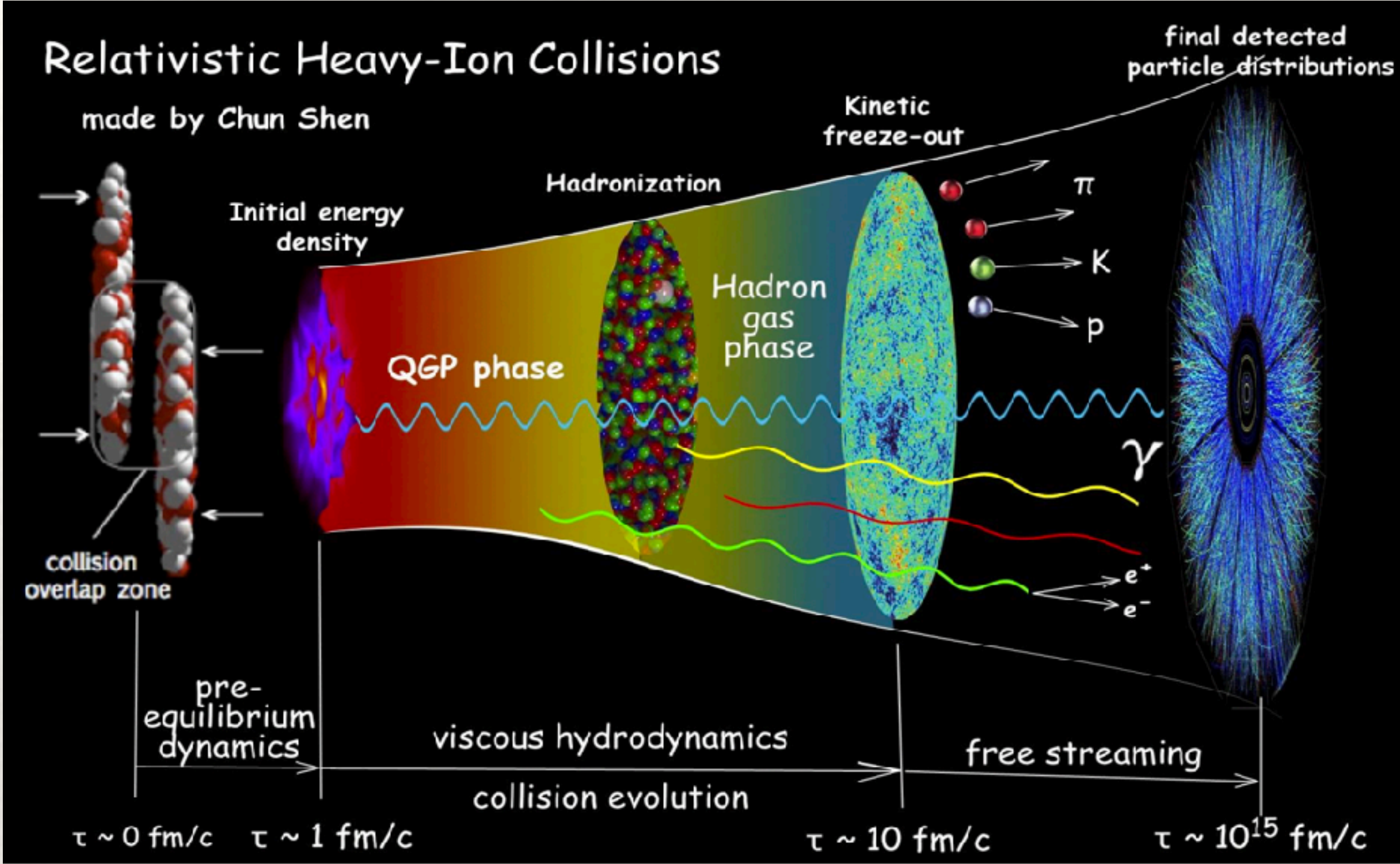
## Exploring QCD phase diagram with current and future facilities

this talk

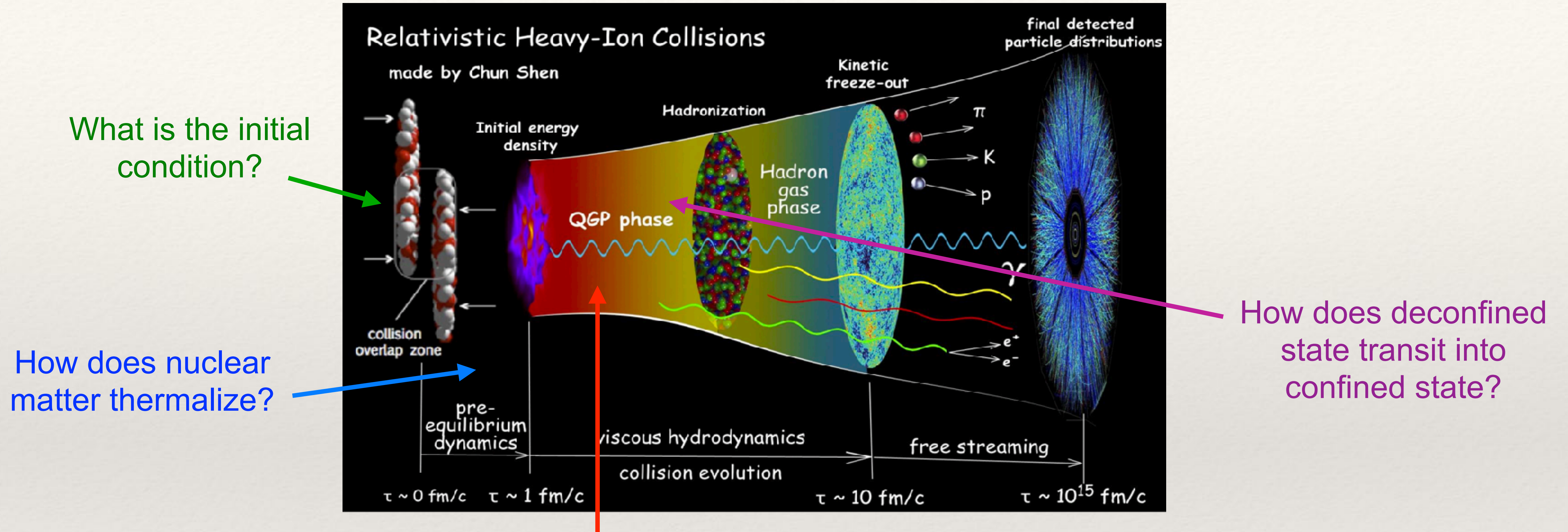


[ by A. Steidl ]

# Questions and challenges for ultra-relativistic collisions



# Questions and challenges for ultra-relativistic collisions



What are the thermal and transport properties of the QGP?

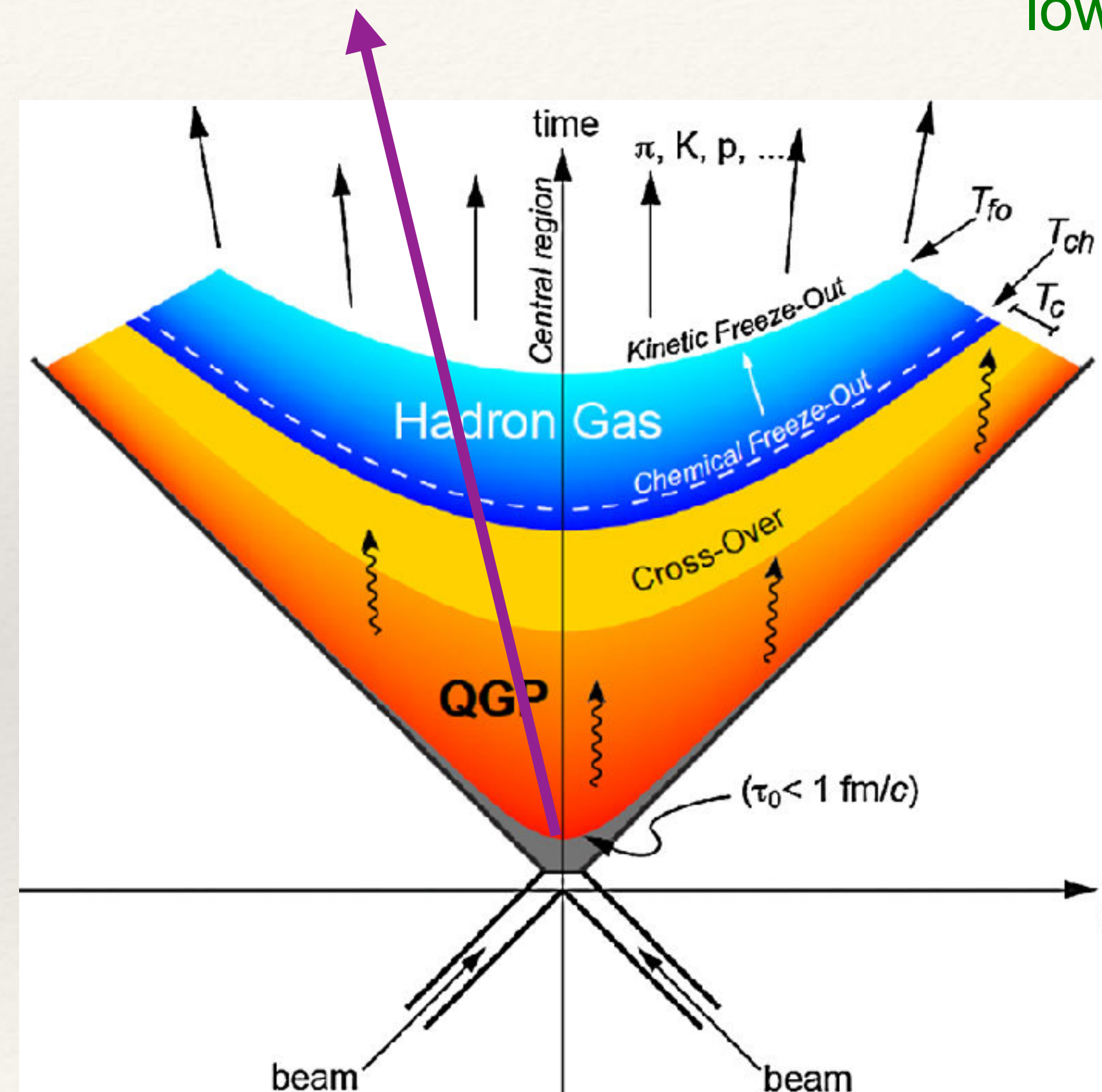
How do energetic particles interact with the QGP?

- **Challenges:** non-perturbative nature of QCD, many-body problem, ...

# Different probes of nuclear matter

## Hard probes

jets and heavy quarks  
from initial high- $Q^2$   
processes



## Soft probes

low  $p_T$  hadrons emitted by the QGP  
from chemical freeze-out

## Electromagnetic probes

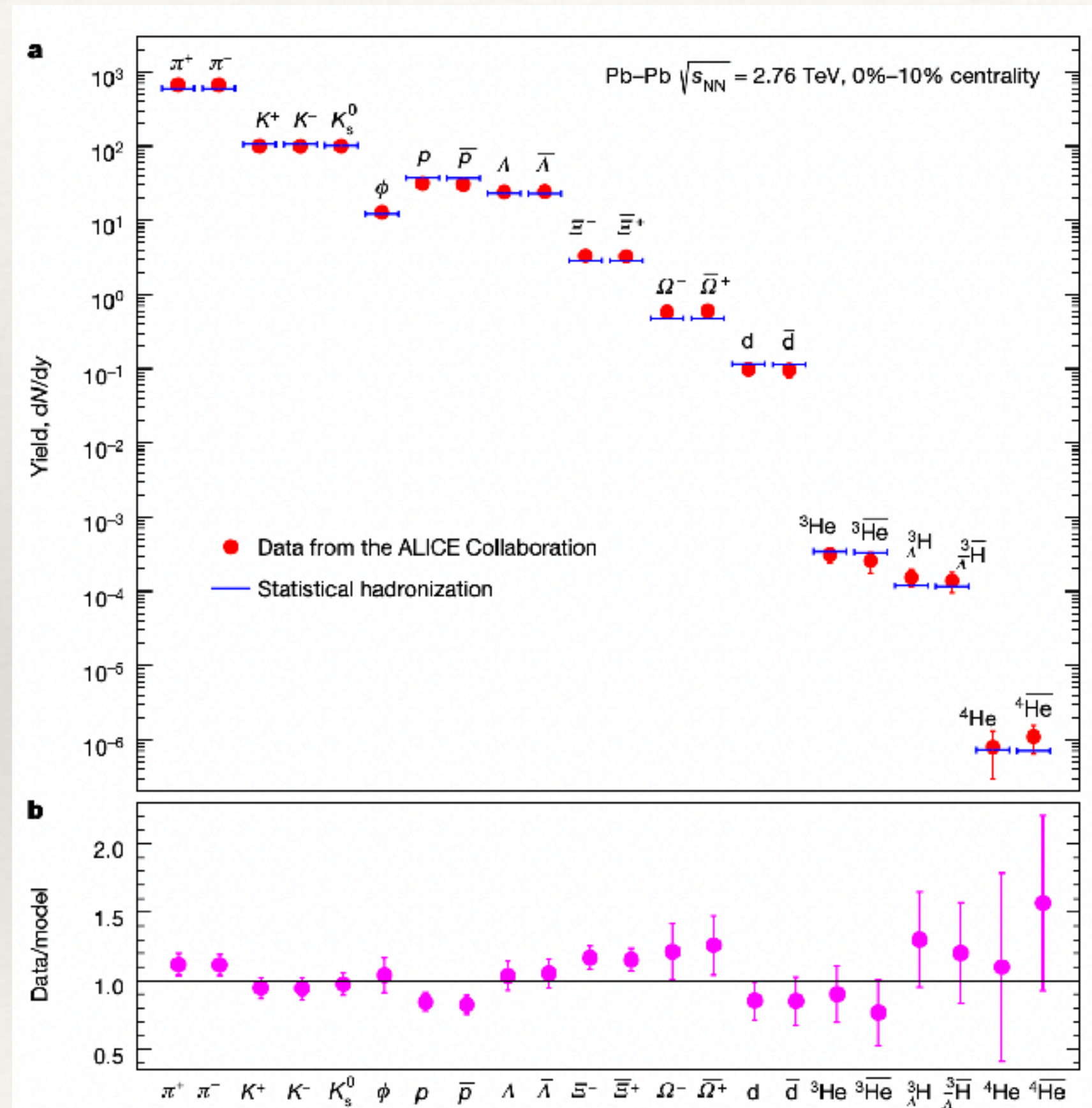
photons, di-leptons  
from the whole evolution

[ by M. Rybar / ATLAS ]

# Soft hadron yields

Surprisingly good description by the thermal model

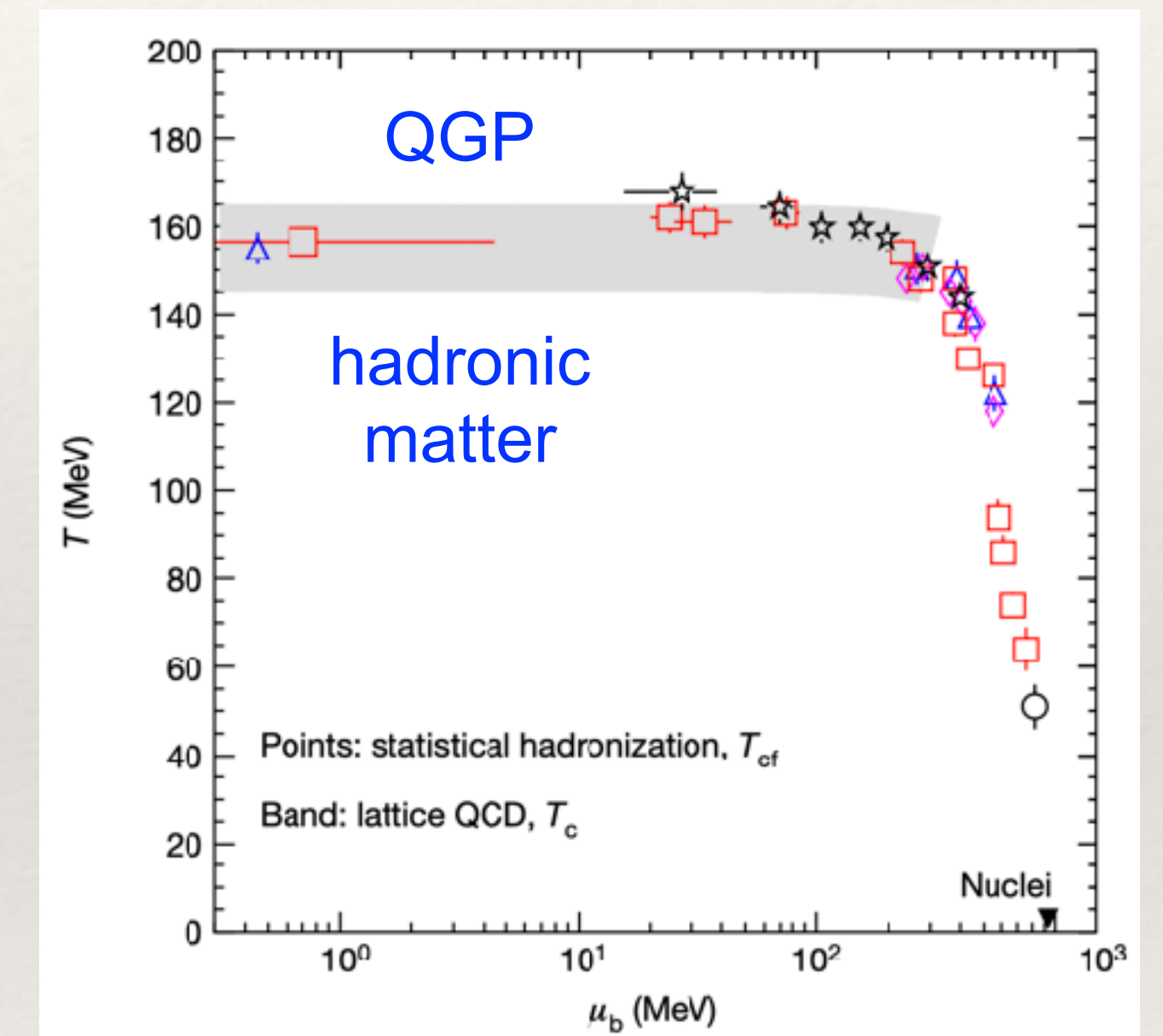
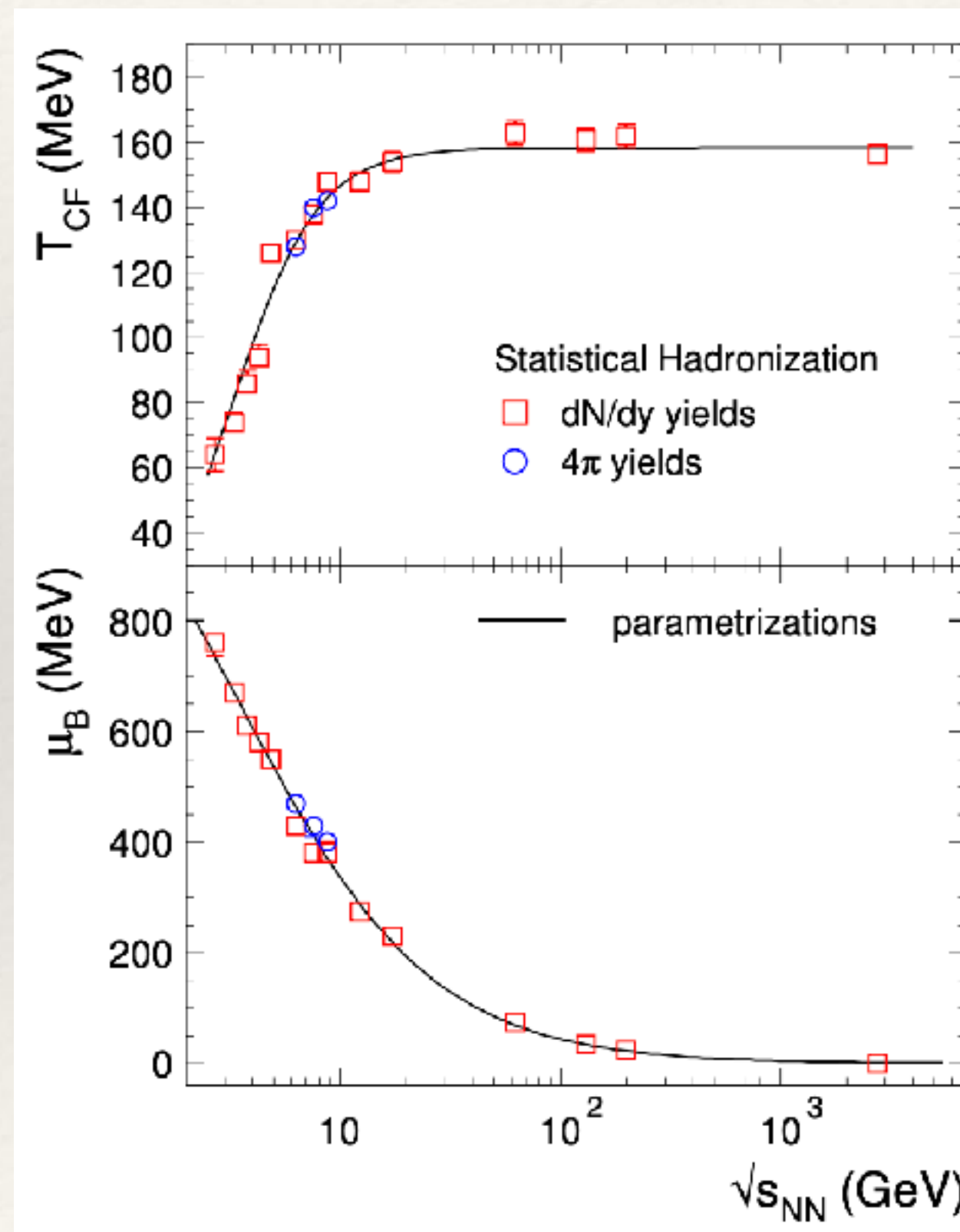
Extraction of thermal properties



[ Andronic *et al.*, Nature 561, 321 (2018) ]

Boltzmann statistics  $\rightarrow$

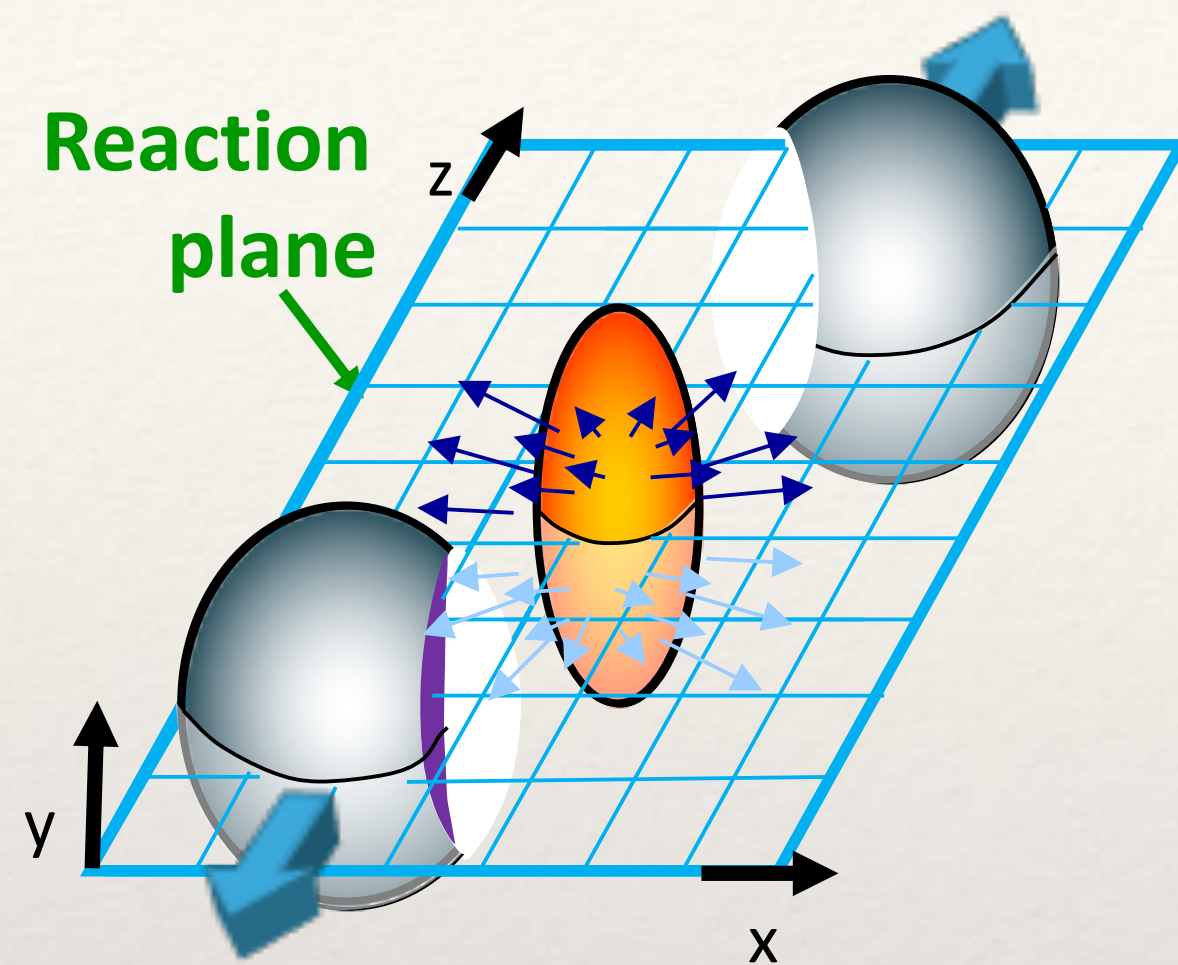
$$N_i = \frac{g_i V T^3}{2\pi^2} e^{\mu_i/T} \frac{m_i^2}{T^2} K_2 \left( \frac{m_i}{T} \right)$$



Limits:

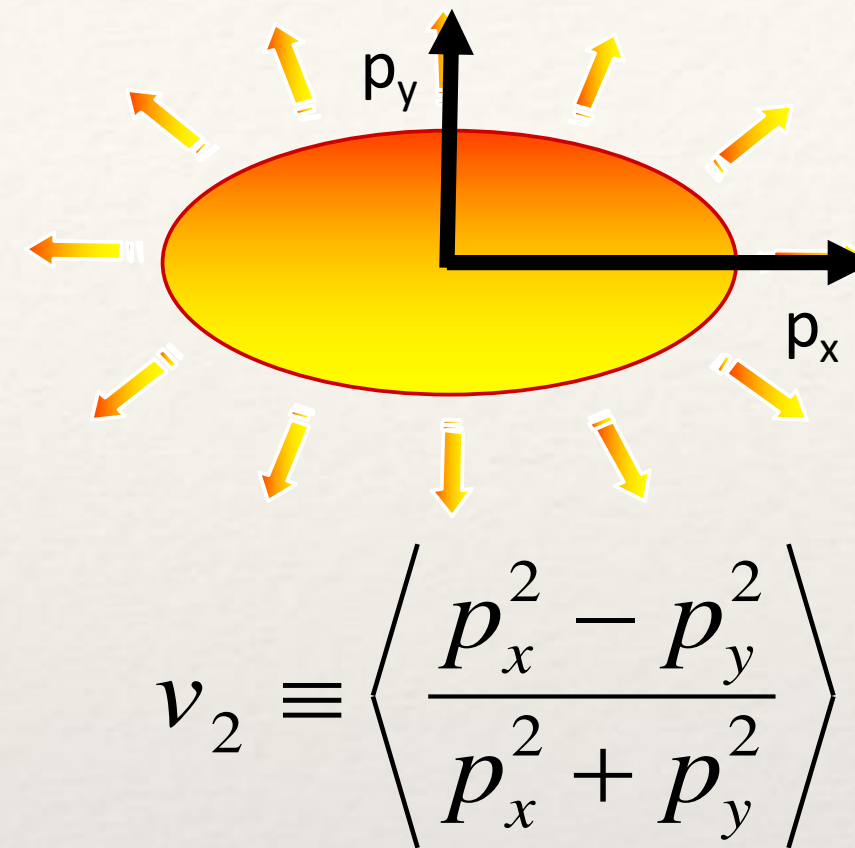
- no dynamic information
- not valid at high  $p_T$

# Collective flow of soft hadrons



Geometric anisotropy

**Elliptic flow:**



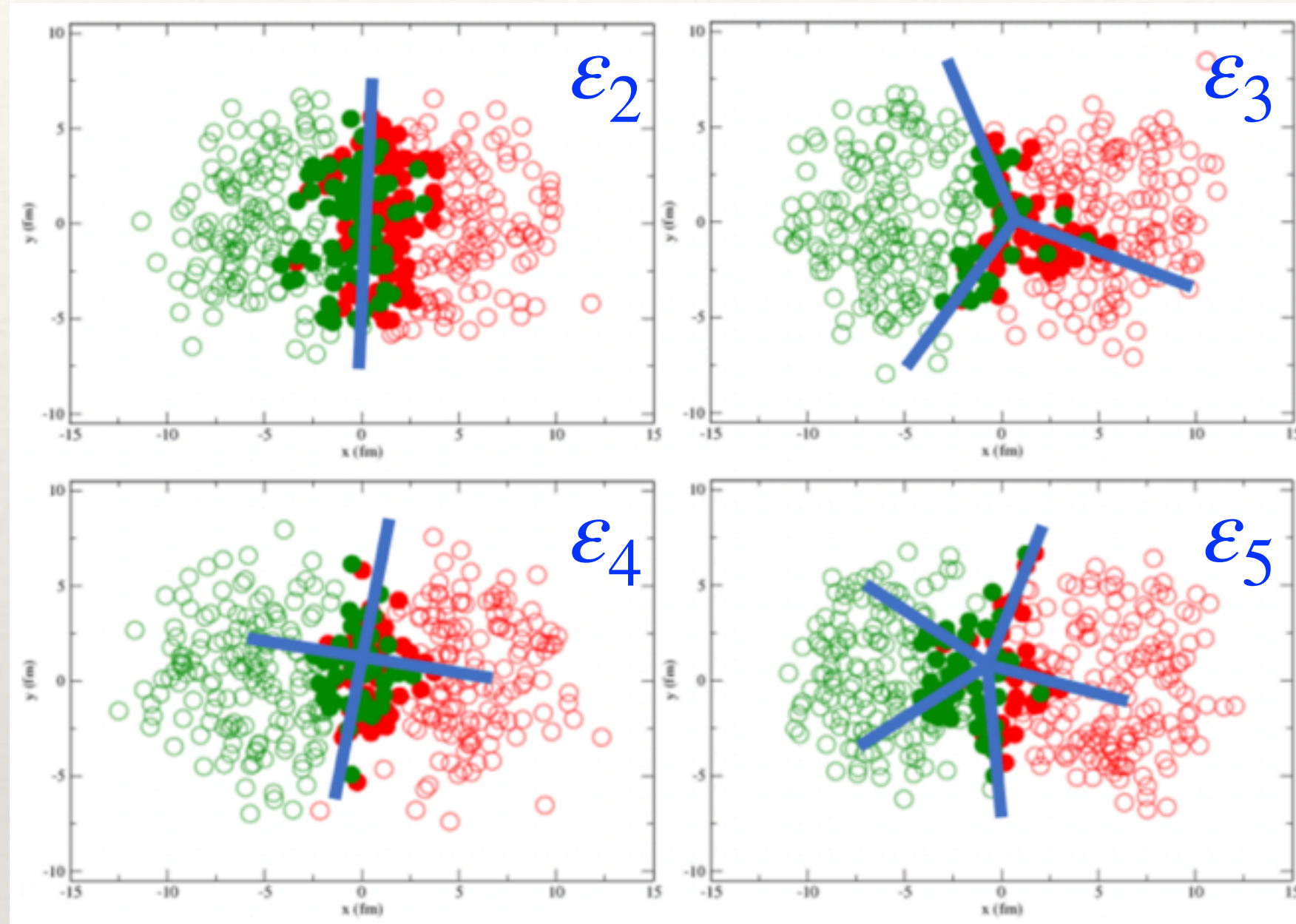
Momentum space anisotropy

Collective flow coefficients:

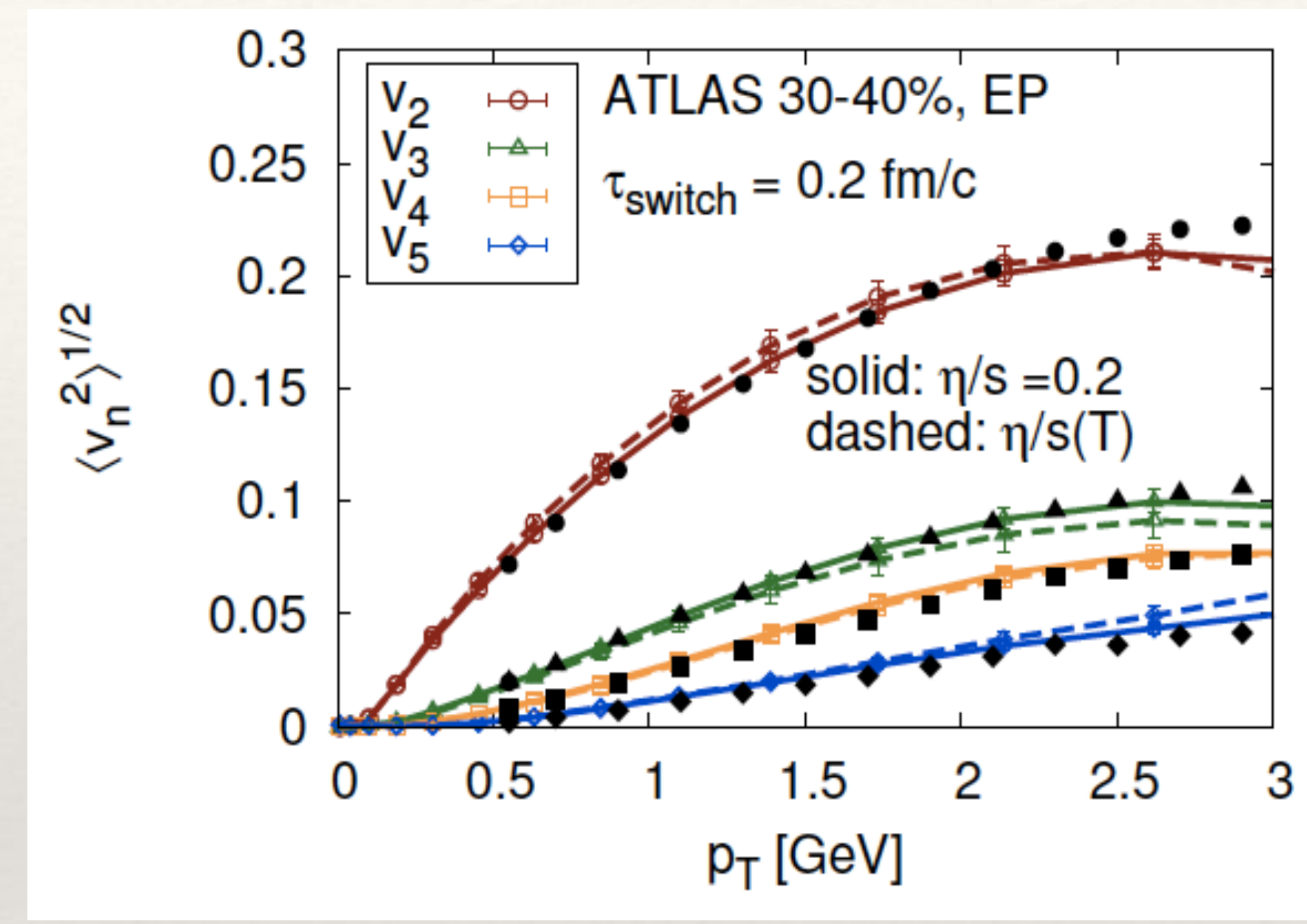
$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left\{ 1 + \sum_n 2v_n \cos \left[ n (\phi - \Phi_n) \right] \right\}$$

# Successful description by hydrodynamic model

With initial state fluctuations



Hydrodynamic calculation of  $v_n$



[ Qin, Int. J. Mod. Phys. E 24 (2015) 02, 1530001 ]

[ Schenke *et al.*, PRL 108, 25231 (2012) ]

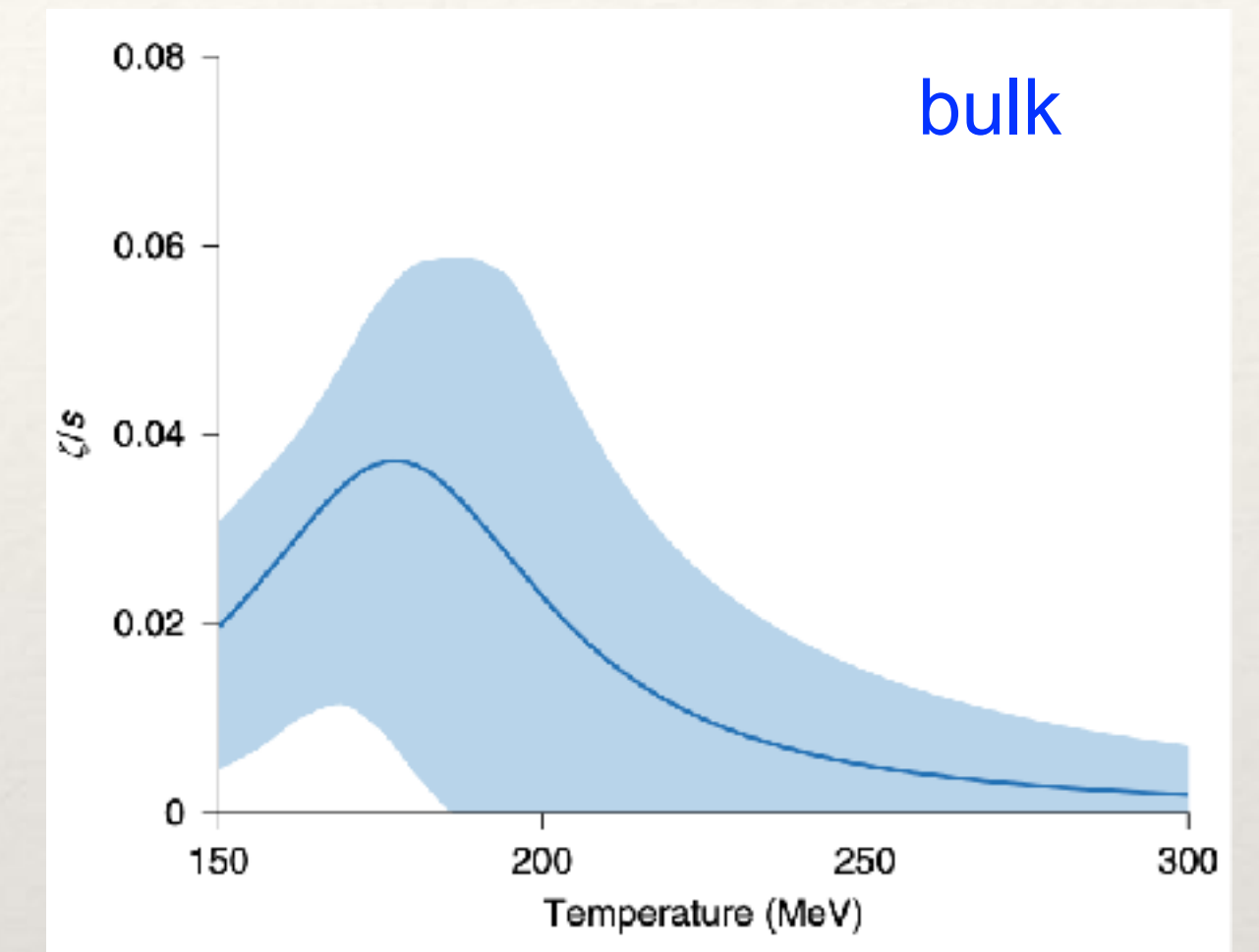
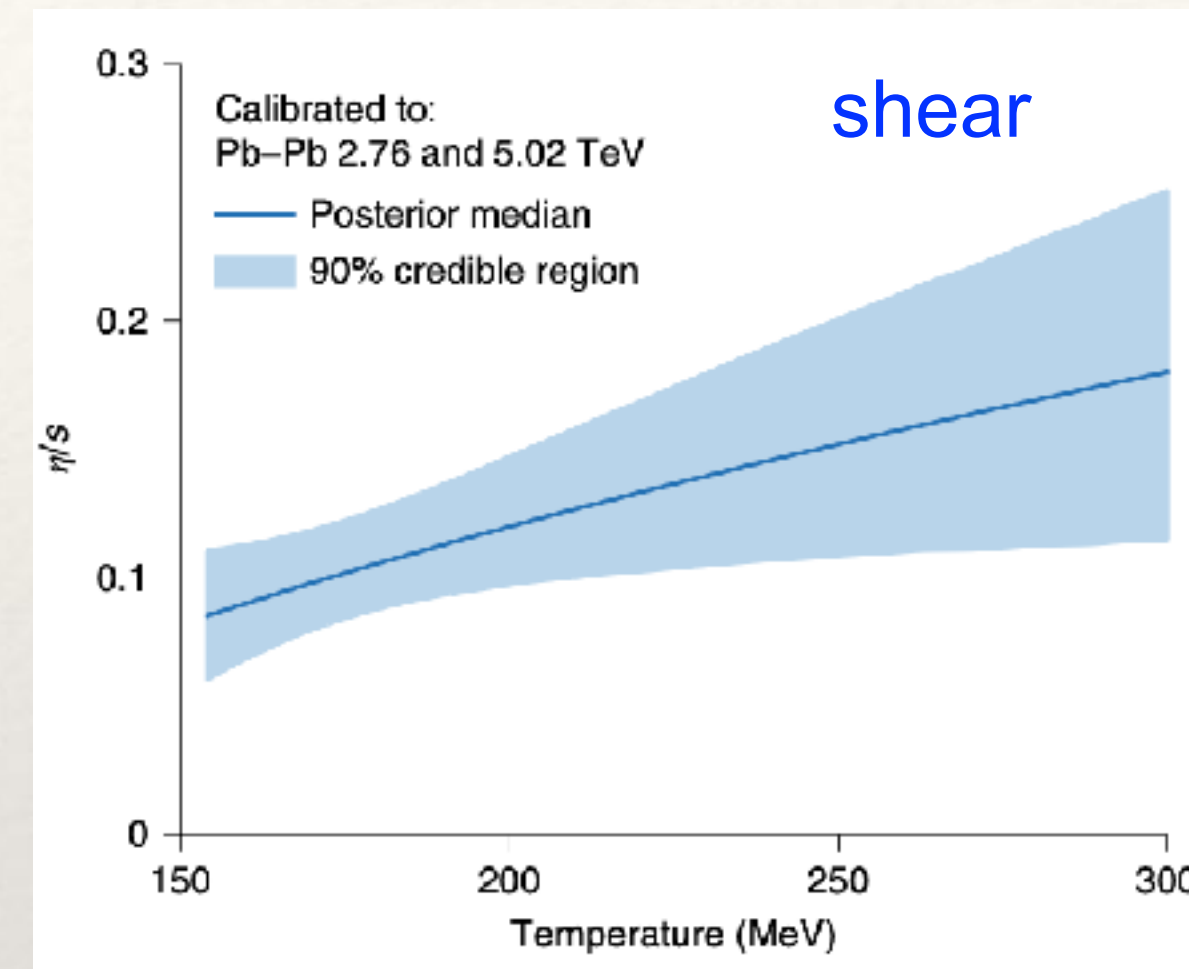
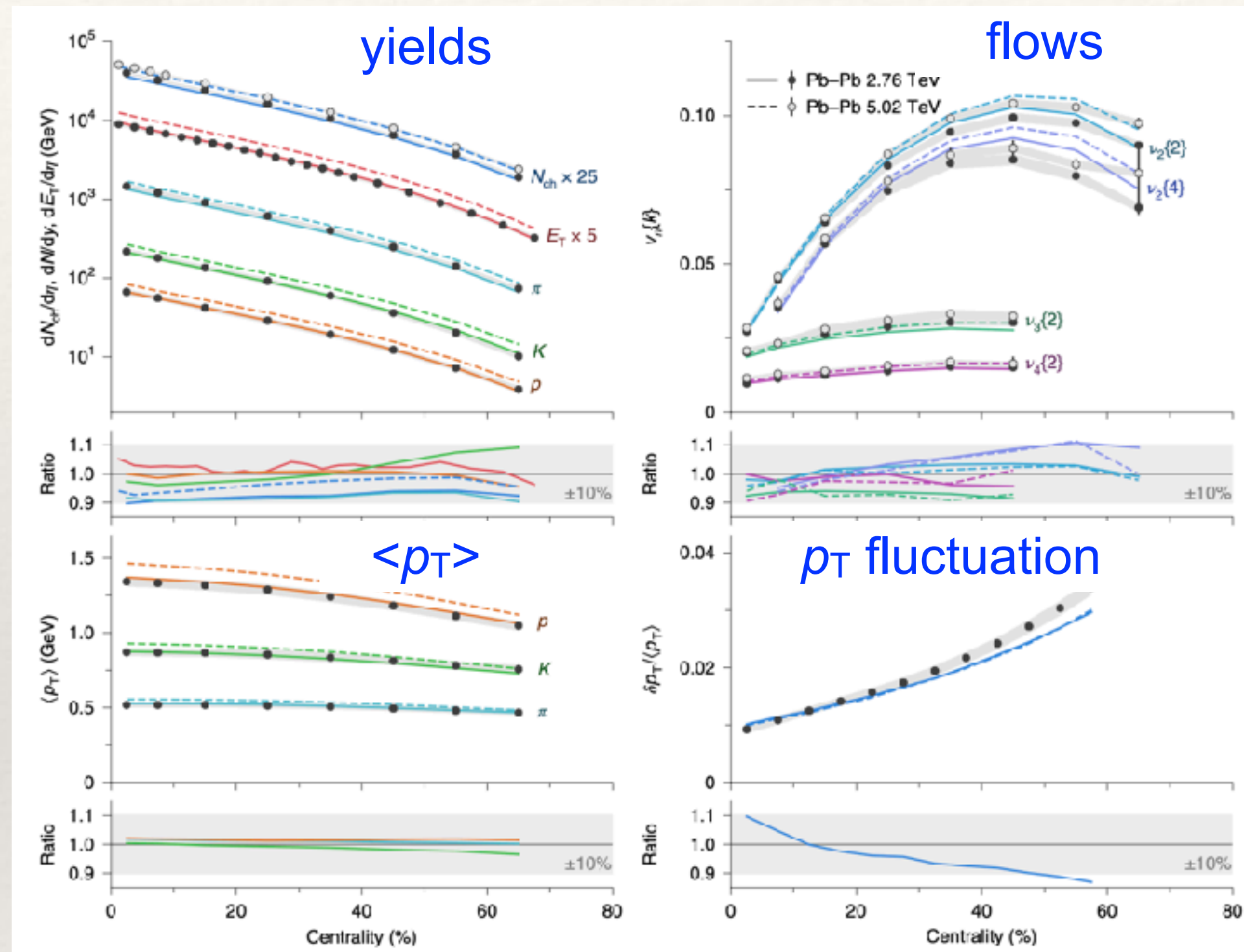
- **Small shear viscosity** extracted from model to data comparison
- **QGP is a strongly coupled system** and displays properties close to ideal fluid



# Constraints on the QGP properties

Bayesian calibration of hydrodynamic model

Shear and bulk viscosities of the QGP

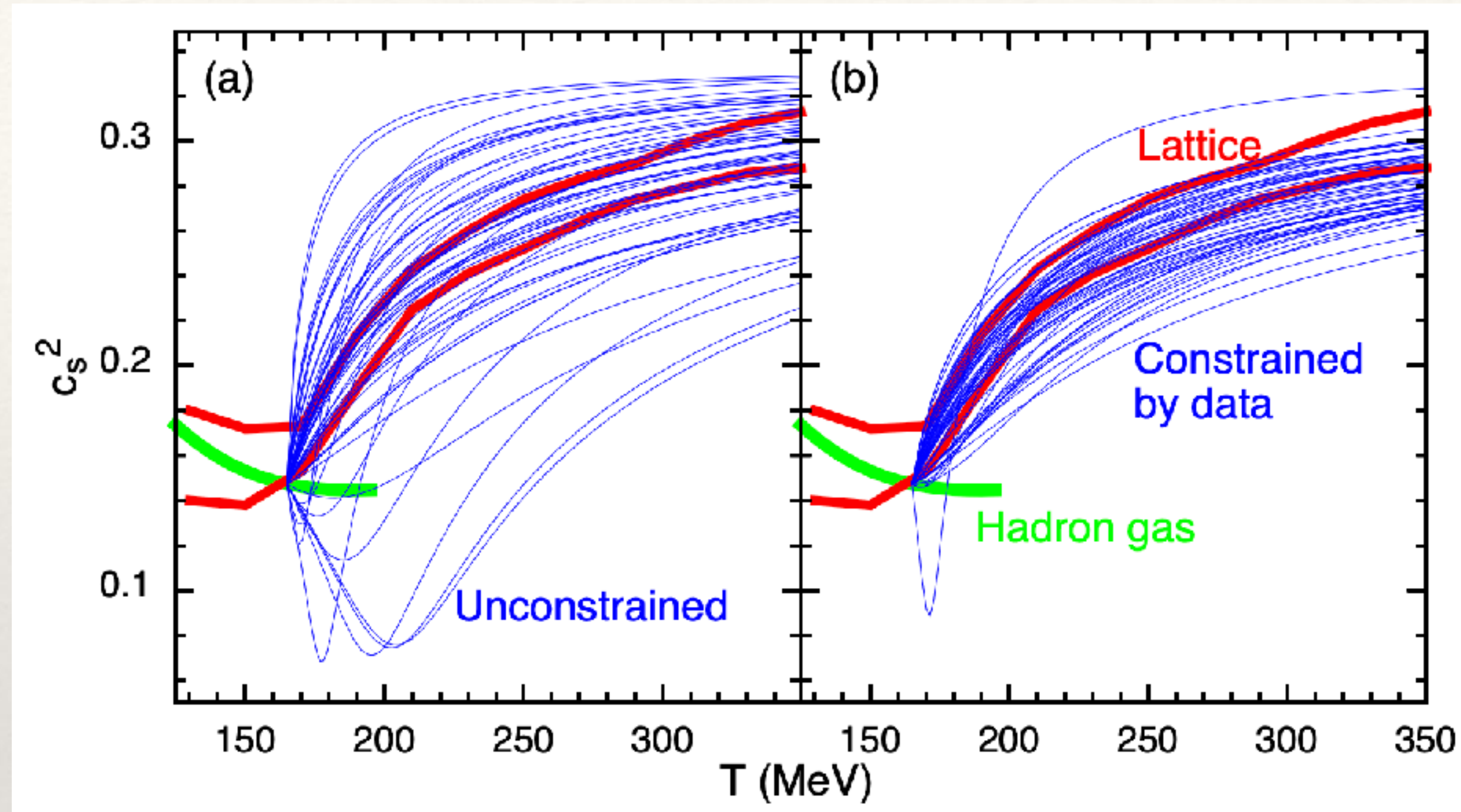


[ Bernhard, Moreland, Bass, Nature Phys. 15 (2019) 11, 1113 ]

New challenges:

- ALICE measurement of collective flow coefficients up to the 9th order [ JHEP 05 (2020) 085 ]
- Expect more stringent constraints on model calculations and the extracted QGP properties

# Constraints on the QGP Equation of State (EoS)



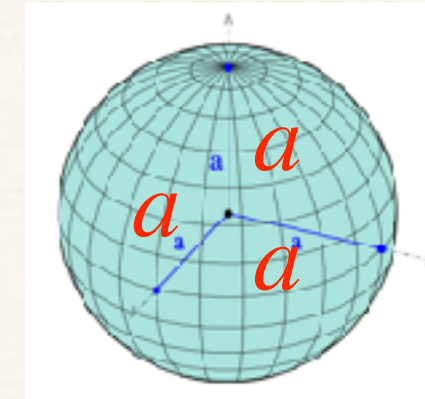
[ Pratt, *et al.*, Phys. Rev. Lett. 114 (2015) 202301 ]

- Bayesian calibration on the  $p$ ,  $K$ ,  $\pi$  yields,  $v_2$  of  $\pi$ , and two-particle femtoscopic source sizes from ALICE measurements
- Experimental data prefer an EoS that is consistent with the Lattice QCD prediction

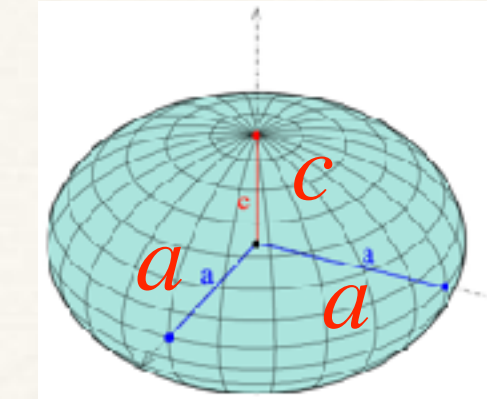
# Constraints on the Nucleus Geometry

Nucleon distribution (Woods Saxon)

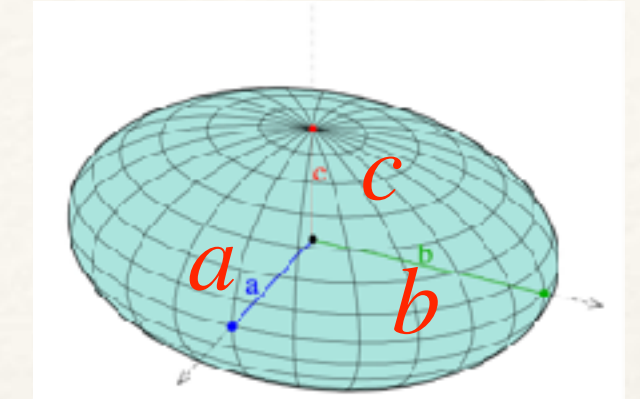
$$\rho(\vec{r}) = \left\{ 1 + \exp \left[ r - R_0 \left( 1 + \beta_2 \left[ Y_2^0(\theta, \phi) \cos \gamma + Y_2^2(\theta, \phi) \sin \gamma \right] \right) \right] \right\}^{-1}$$



$\beta_2 = 0$



$\beta_2 \neq 0, \gamma = 0$

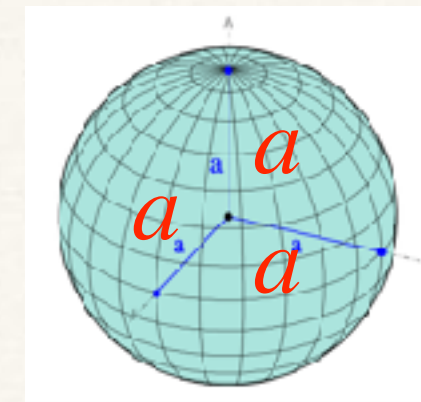


$\beta_2 \neq 0, \gamma \neq 0$

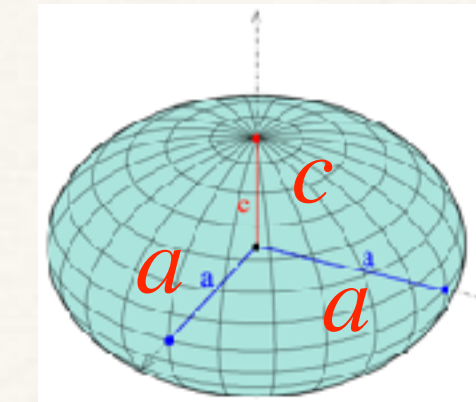
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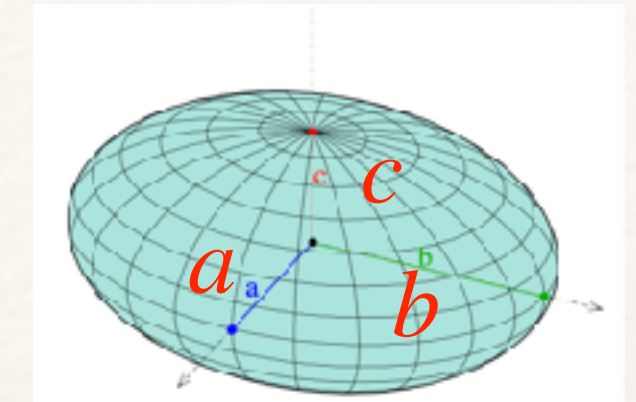
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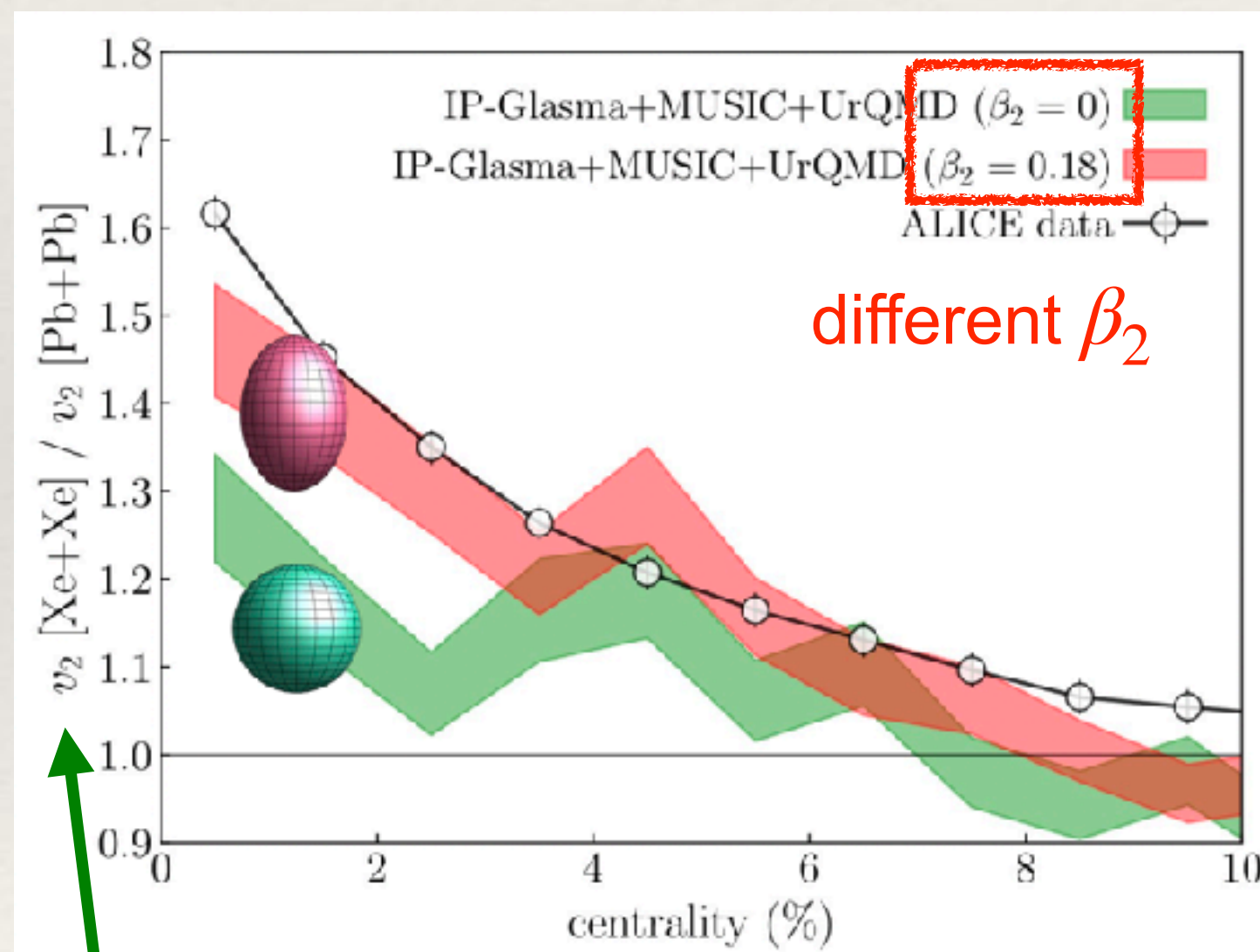


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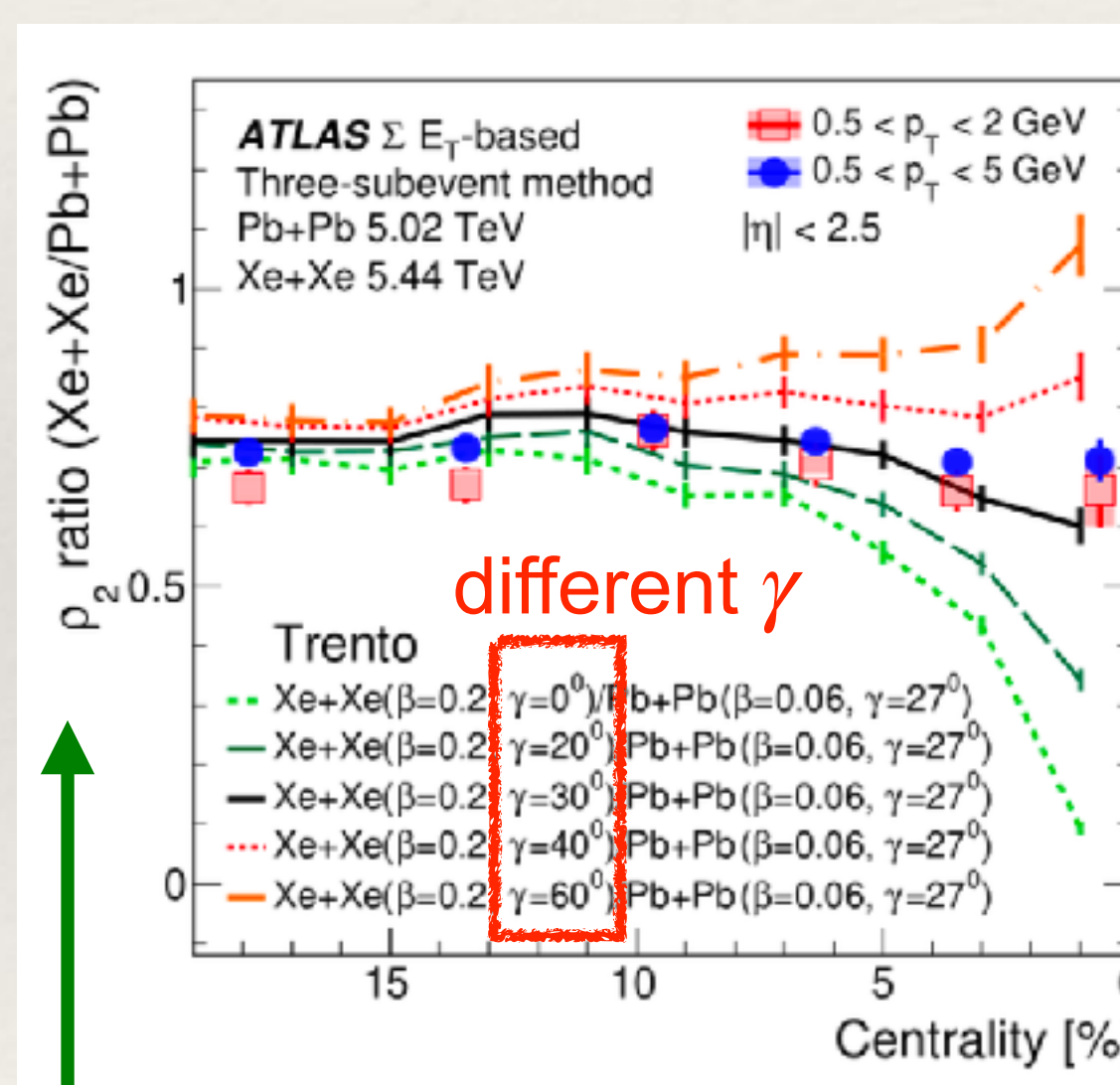
## Deformation of Xe



$v_2$

[ Bally *et al.*, arXiv:2209.11042 ]

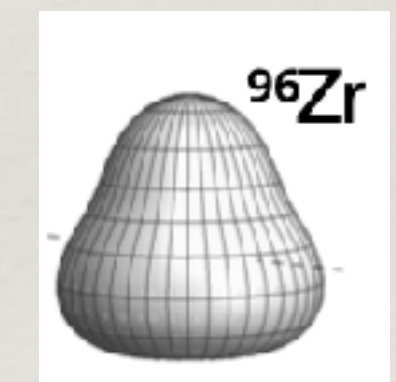
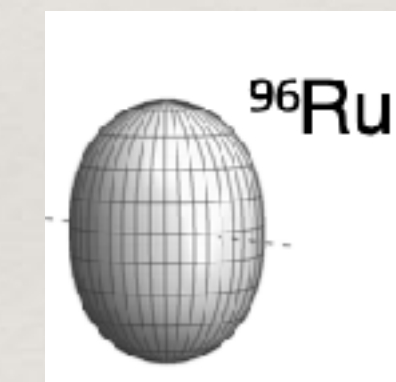
## Triaxial structure of Xe



Correlation between  $v_2^2$  and  $\delta p_T$   
(Pearson coefficient)

## Other developments:

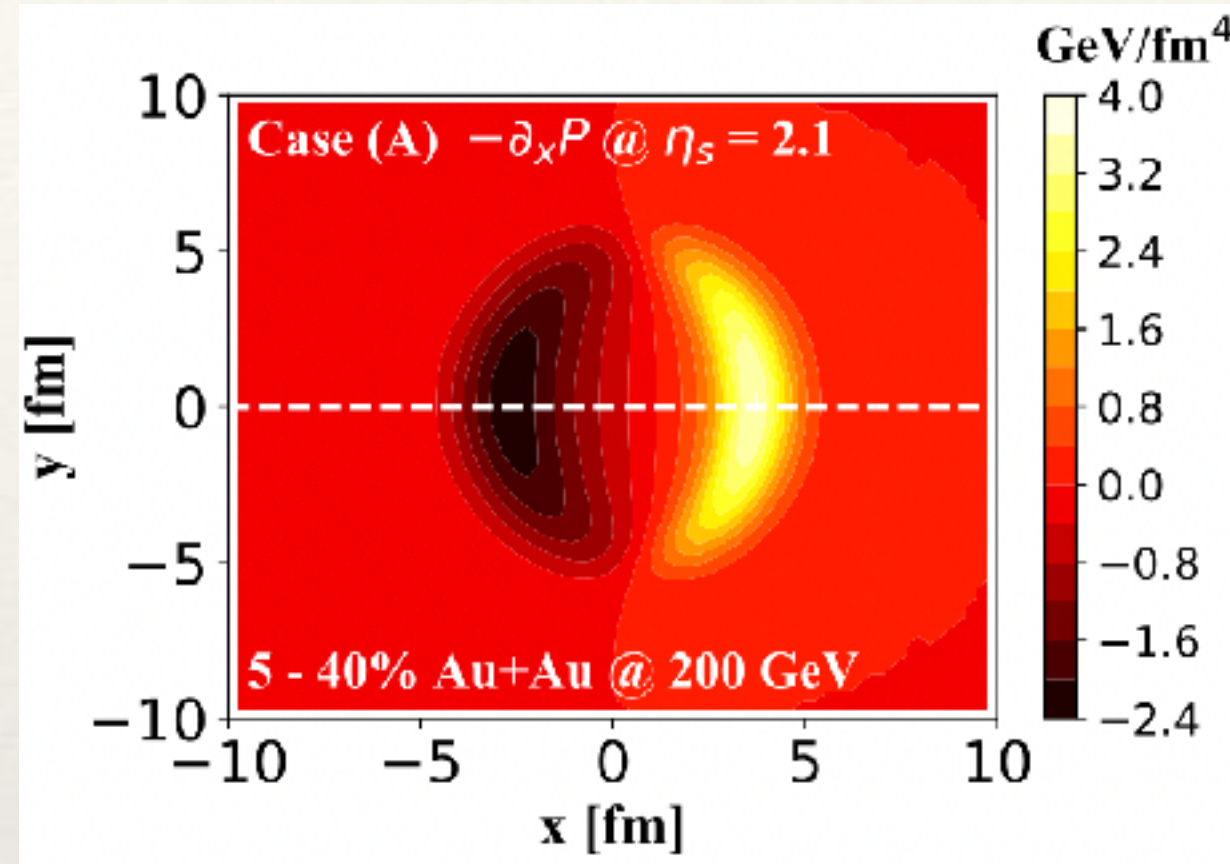
- Nuclear Geometry of Ru and Zr at RHIC



- Constrain the nucleon size using the Pearson coefficient

[ Giacalone *et al.*, Phys. Rev. Lett. 128 (2022) 4, 042301 ]

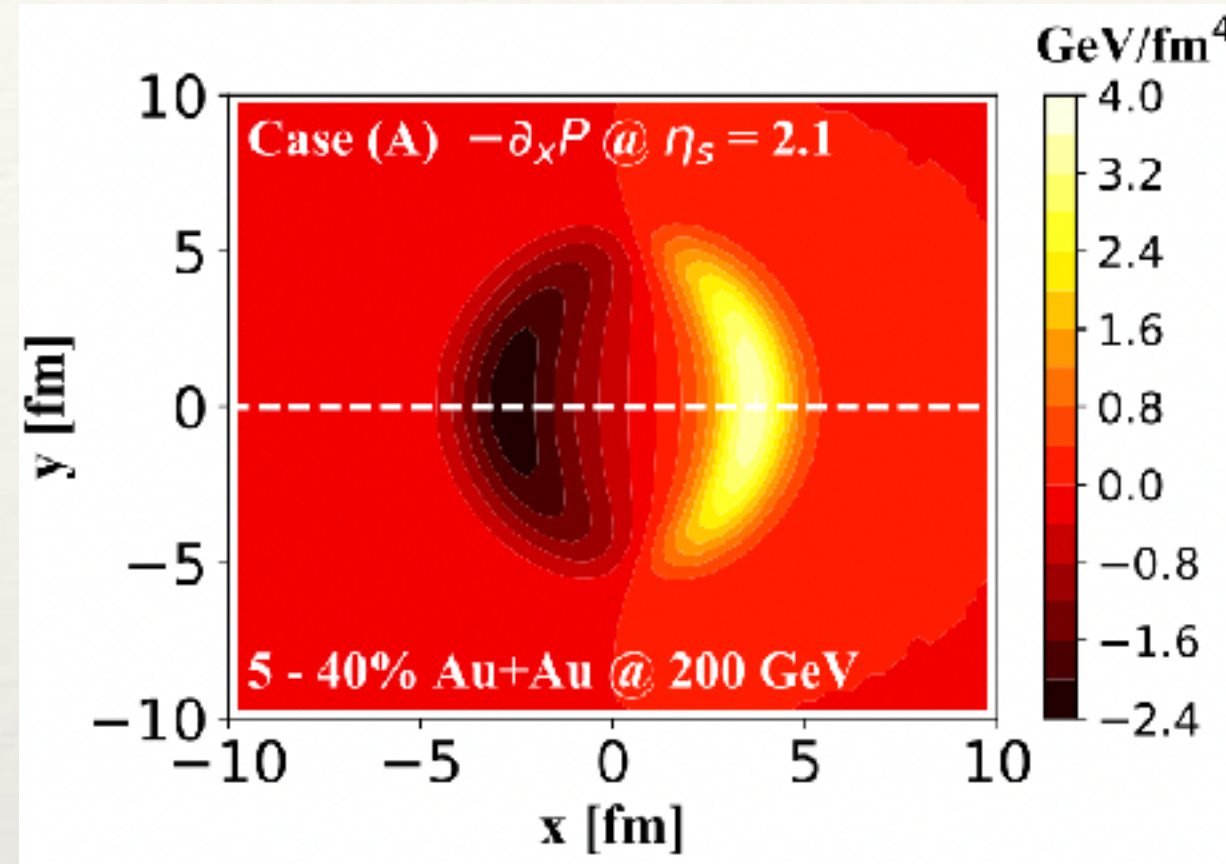
# Directed flow and longitudinal geometry of the QGP



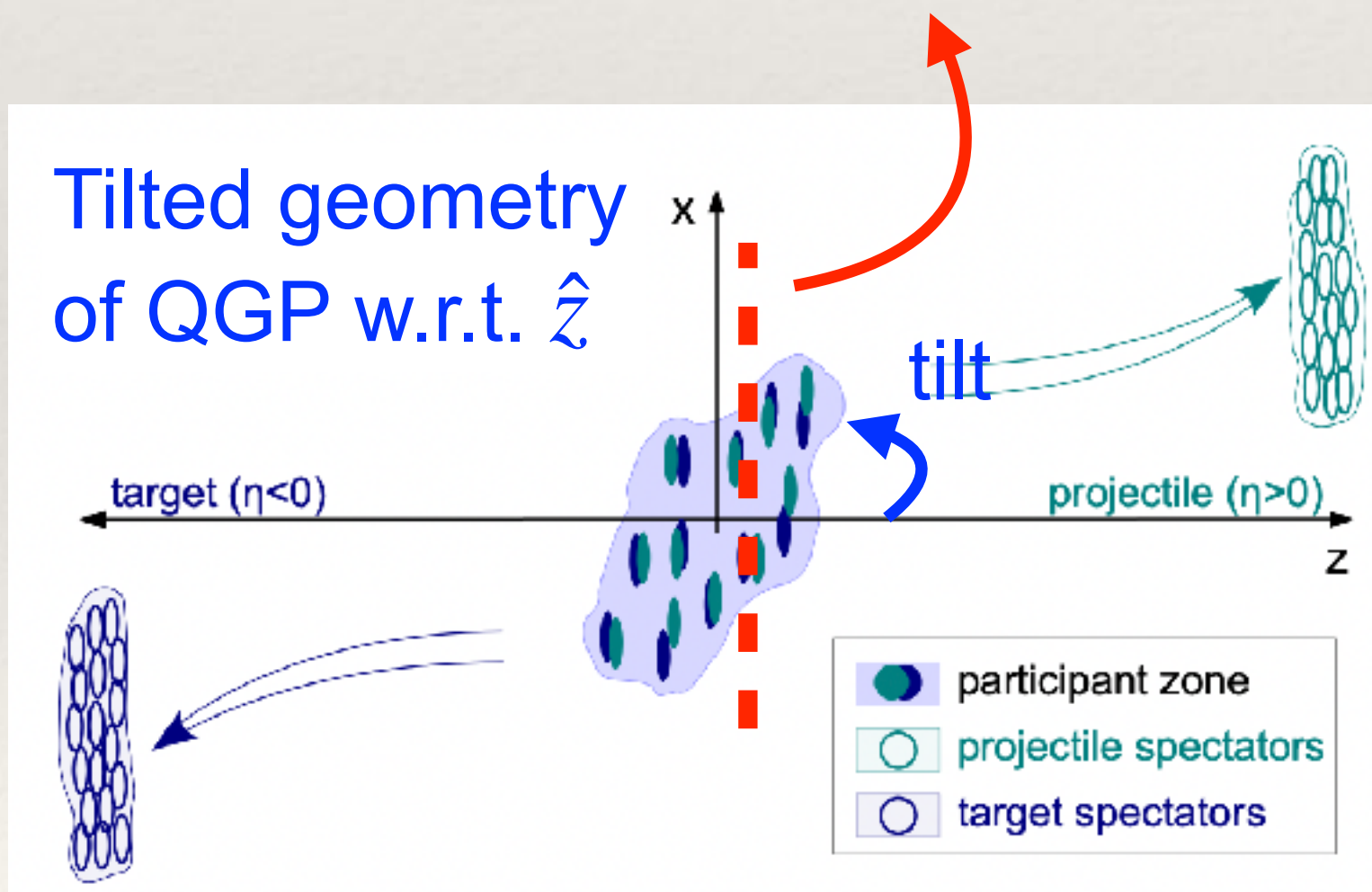
Asymmetry in  $\pm \hat{x}$

$$v_1 = \langle p_x / p_T \rangle \neq 0$$

# Directed flow and longitudinal geometry of the QGP

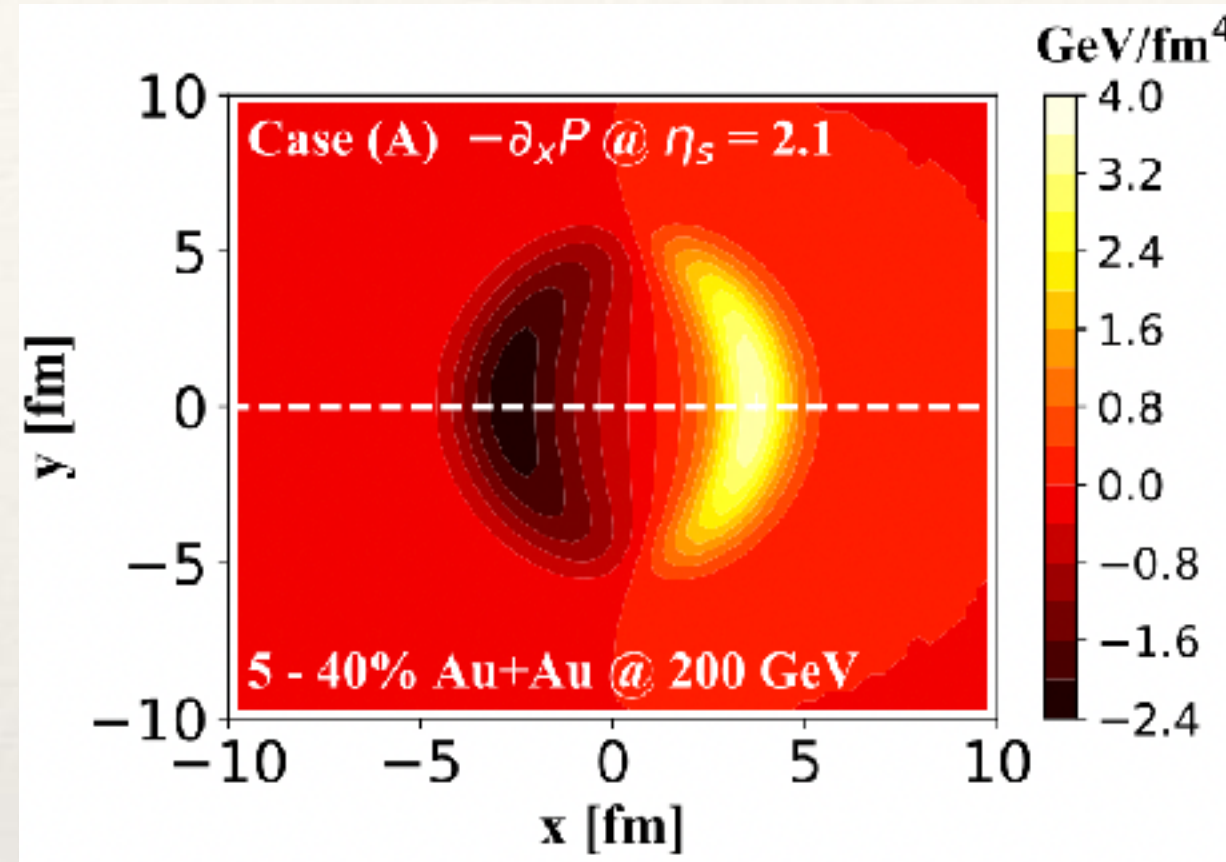


Asymmetry in  $\pm \hat{x}$   
 $v_1 = \langle p_x / p_T \rangle \neq 0$



[ ALICE, Phys. Rev. Lett. 111 (2013) 23, 232302 ]

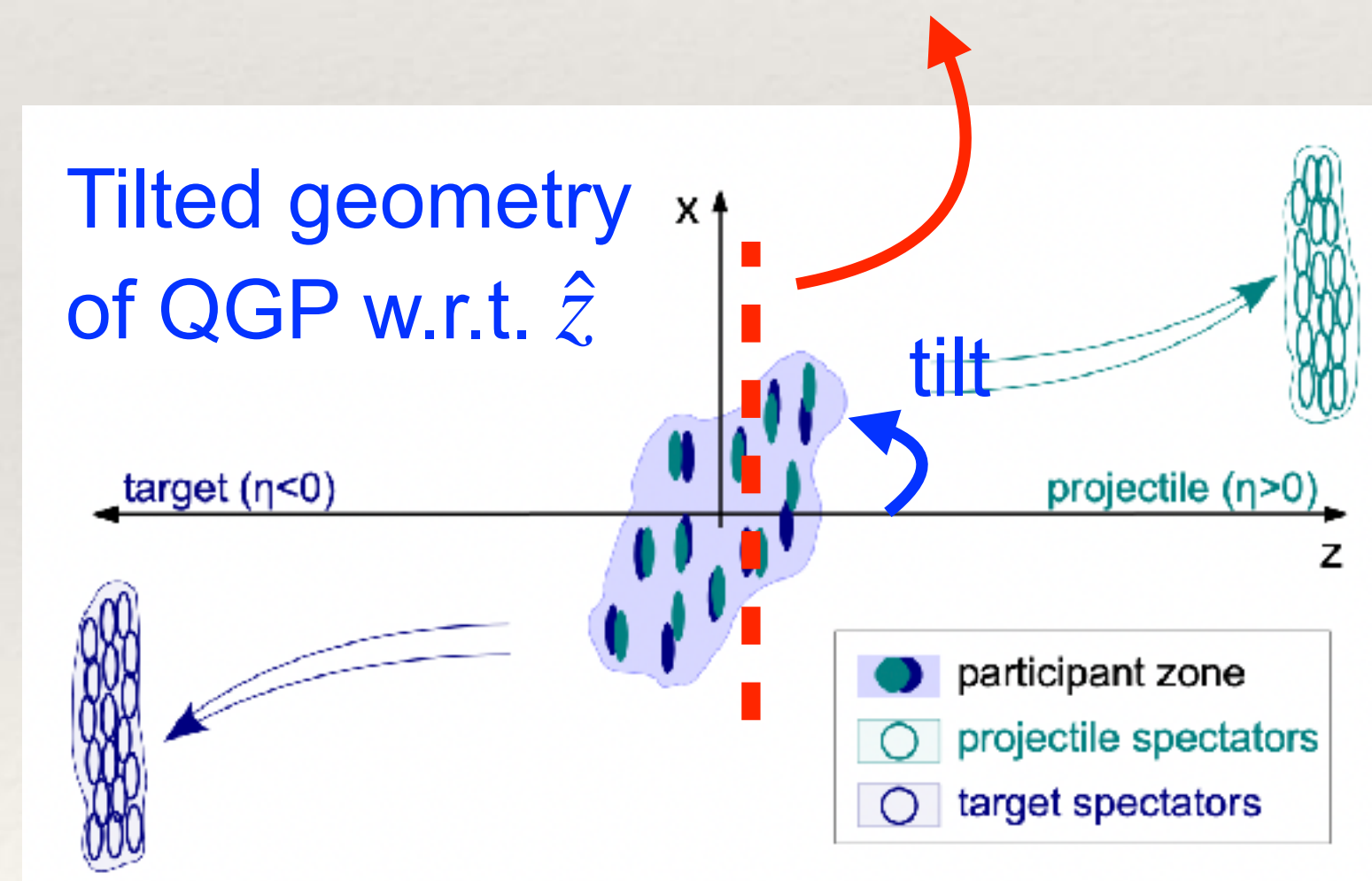
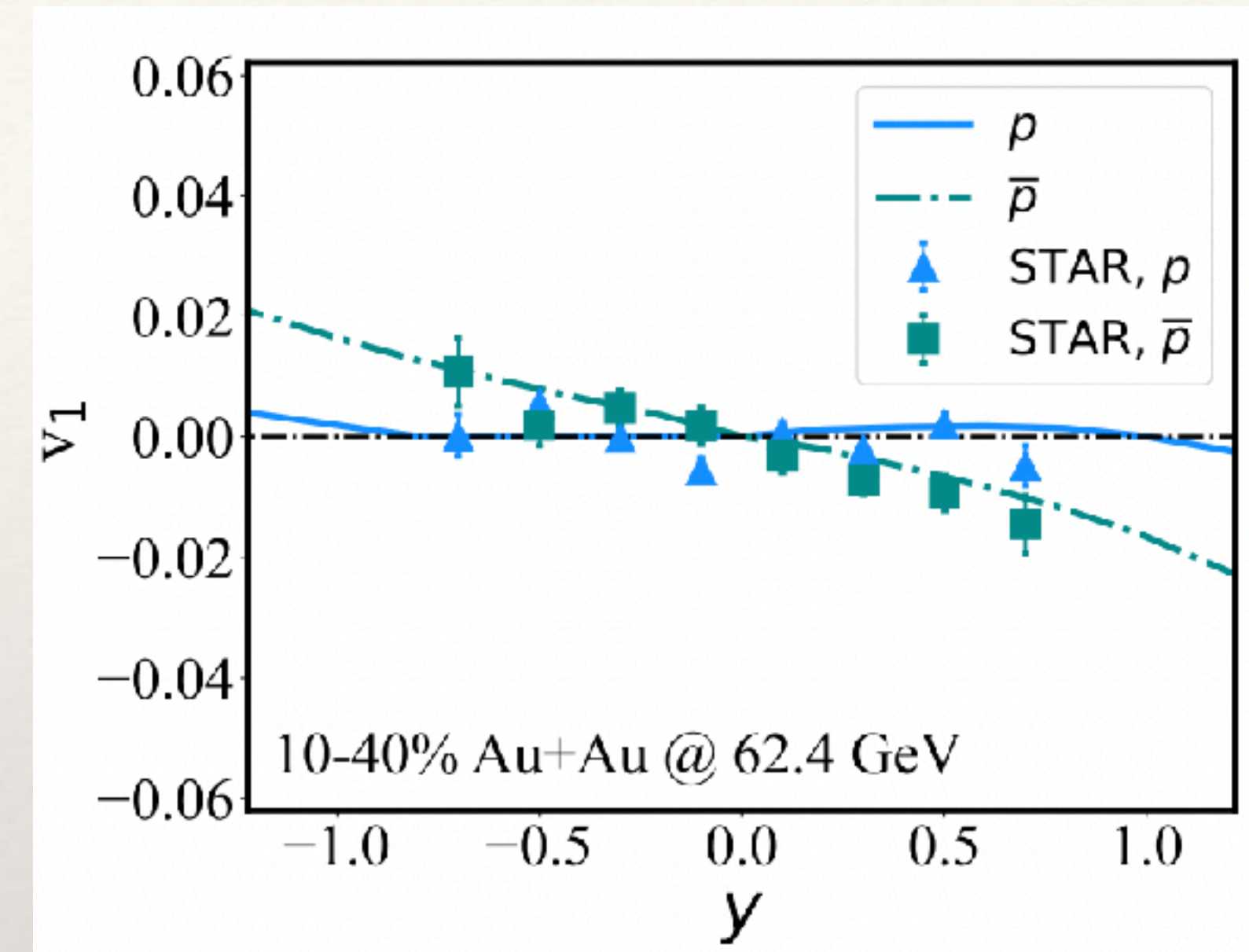
# Directed flow and longitudinal geometry of the QGP



Asymmetry in  $\pm \hat{x}$   
 $v_1 = \langle p_x / p_T \rangle \neq 0$



Rapidity-odd distribution of  $v_1$



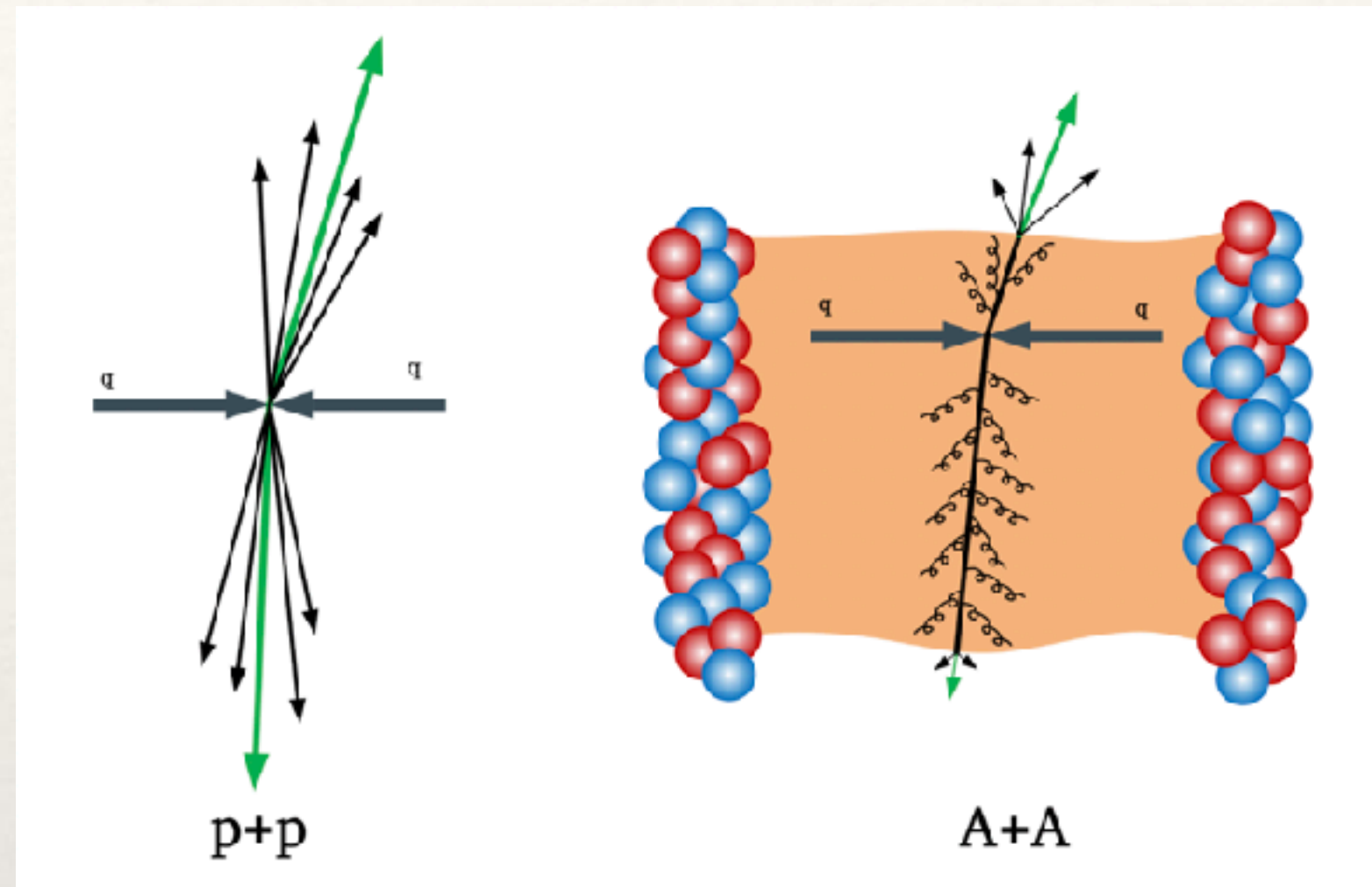
- Titled energy density  $\rightarrow$  average  $v_1(y)$
- Titled baryon density  $\rightarrow v_1$  split between  $\rho, \bar{\rho}$
- Challenges in understanding  $v_1$  at low beam energies

[ ALICE, Phys. Rev. Lett. 111 (2013) 23, 232302 ]

[ Bozek, Phys. Rev. C 106 (2022) 6, L061901 ]

[ Jiang, Wu, SC, Zhang, Phys. Rev. C 107 (2023) 3, 034904 ]

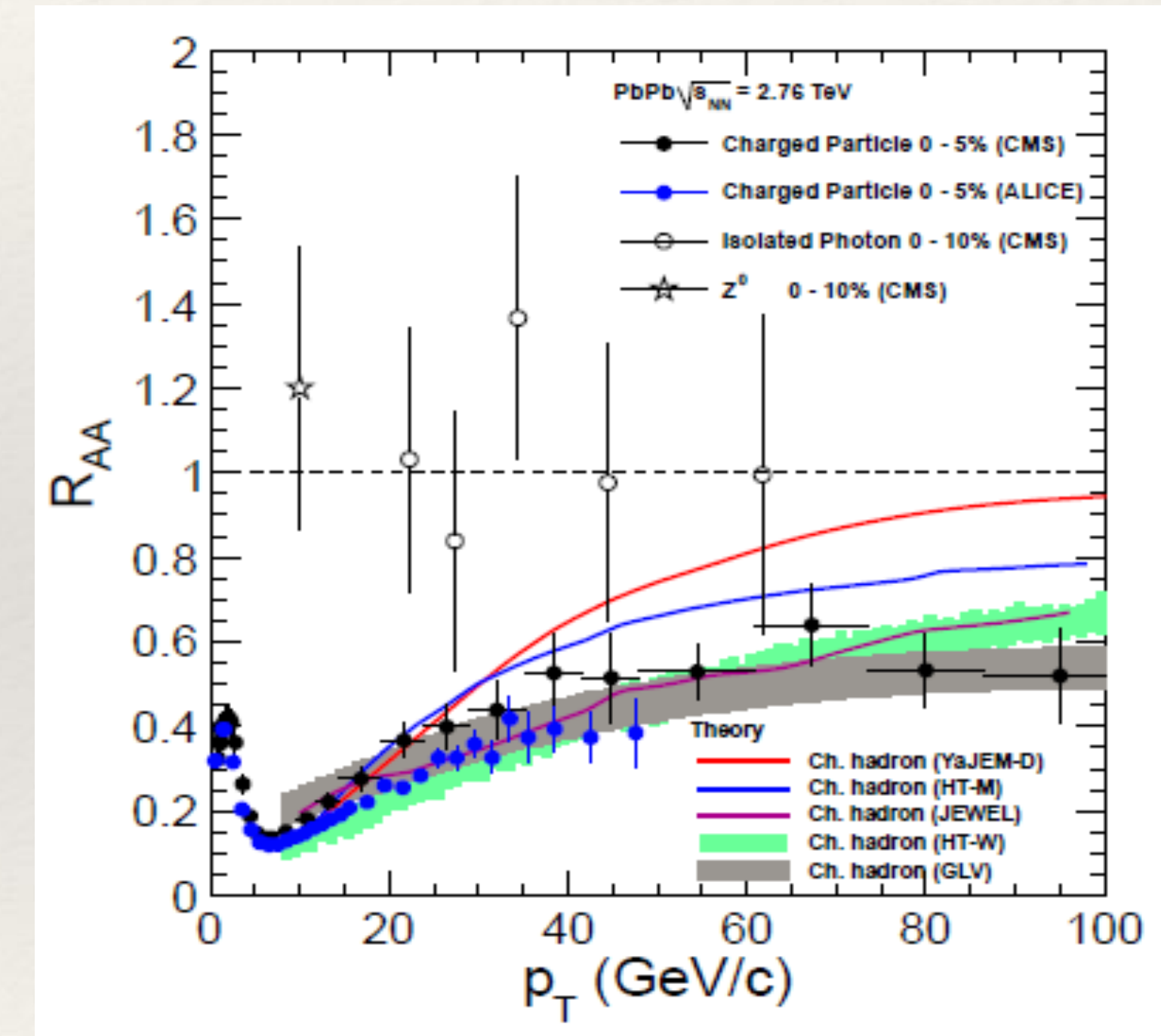
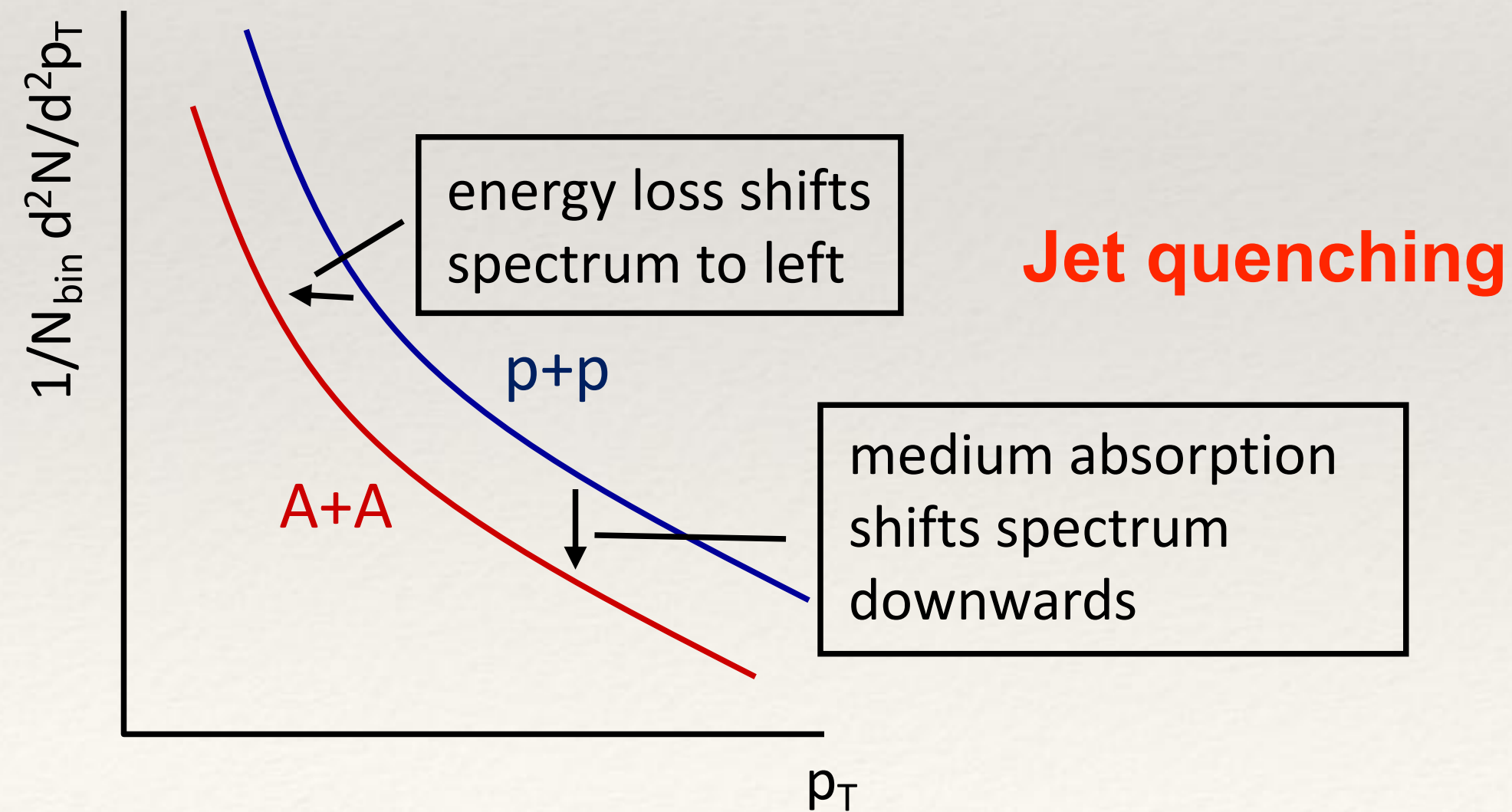
# Nuclear modification of hard probes



[ by M. Rybar / ATLAS ]

## Nuclear modification factor

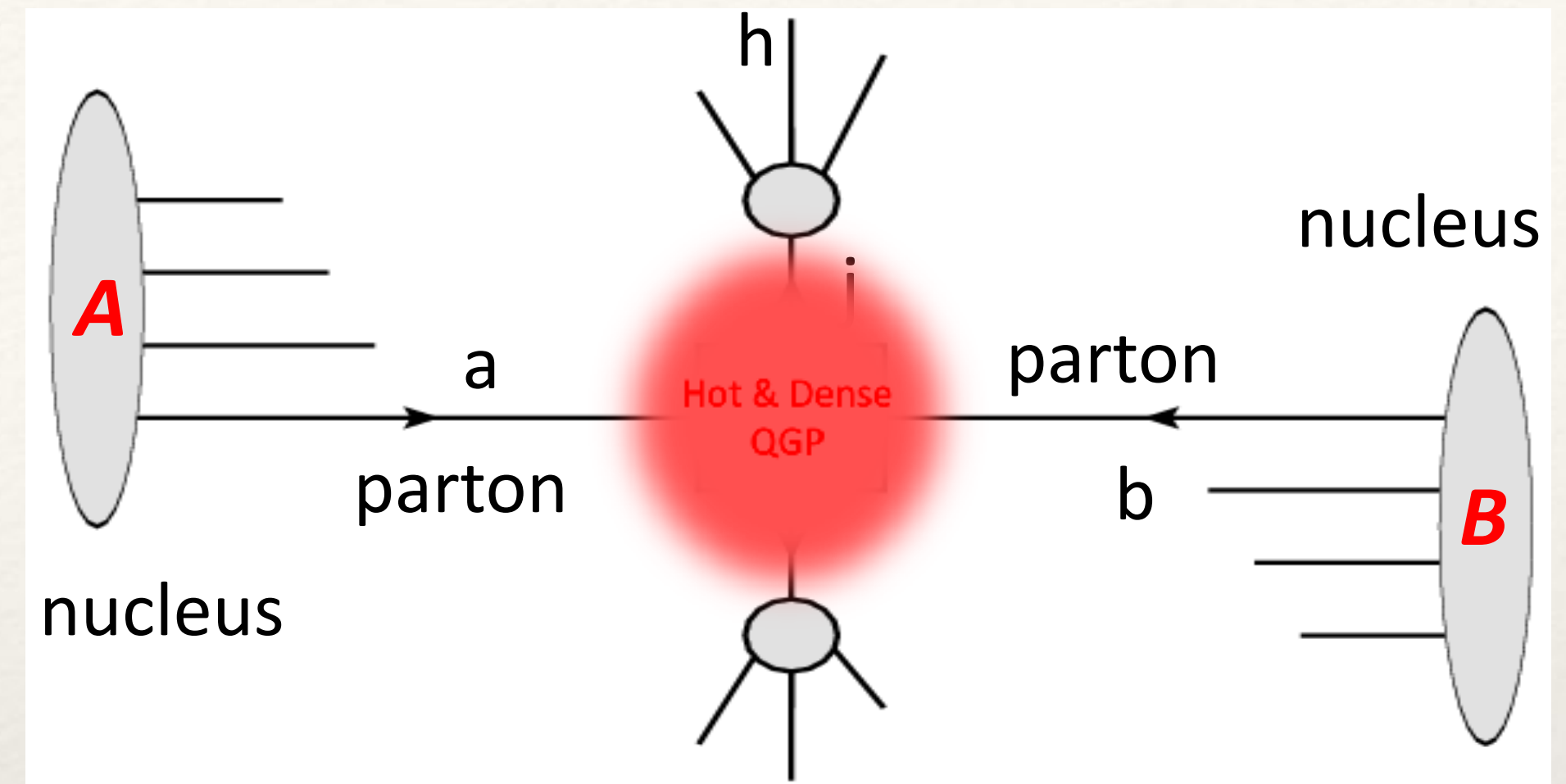
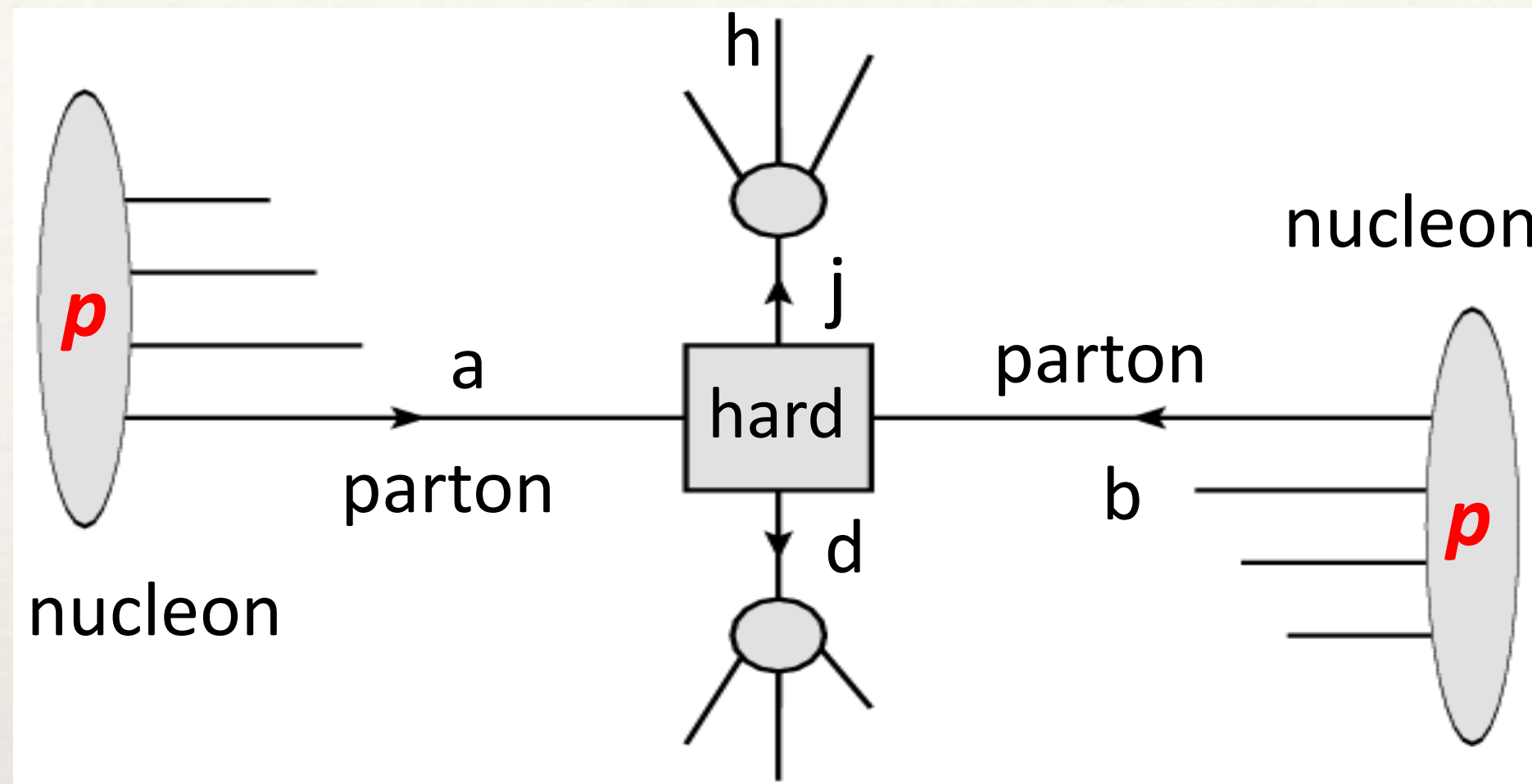
$$R_{AA} \equiv \frac{d^2 N^{AA} / dy dp_{\perp}}{d^2 N^{pp} / dy dp_{\perp} \times \langle N_{coll}^{AA} \rangle}$$



[ Mueller *et al.*, Ann. Rev. Nucl. Part. Sci. 62, 361 (2012) ]



# Theoretical framework of jet quenching



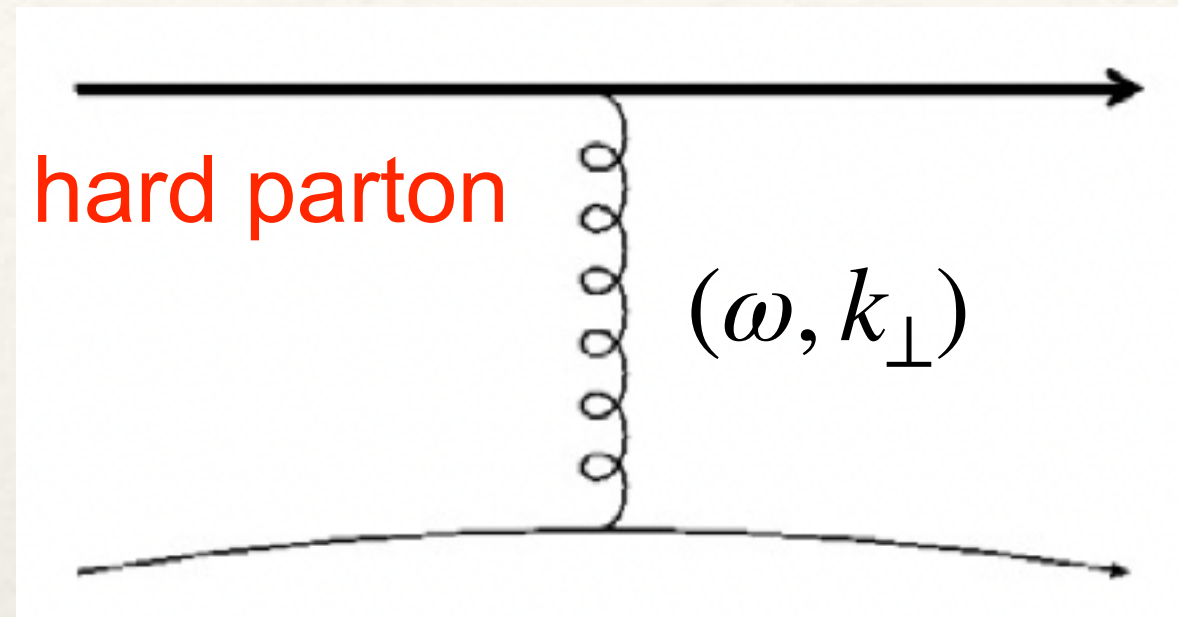
$$d\sigma_h = \sum_{abjd} f_{a/p} \otimes f_{b/p} \otimes d\sigma_{ab \rightarrow jd} \otimes D_{h/j}$$

$$d\tilde{\sigma}_h = \sum_{abjd} f_{a/A} \otimes f_{b/B} \otimes d\sigma_{ab \rightarrow jd} \otimes \tilde{D}_{h/j}$$

- $f_{a/p}, f_{b/p} \rightarrow f_{a/A}, f_{b/B}$ : cold nuclear matter (initial state) effect, e.g., shadowing, Cronin, ... , measured in  $pA$  collisions
- $D_{h/j} \rightarrow \tilde{D}_{h/j}$ : medium modified fragmentation function, hot nuclear matter (final state) effect
- Factorization assumption:  $\tilde{D}_{h/j} = \sum_{j'} P_{j \rightarrow j'} \otimes D_{h/j'}$ , nuclear modification on parton  $j$

# Elastic and inelastic scatterings

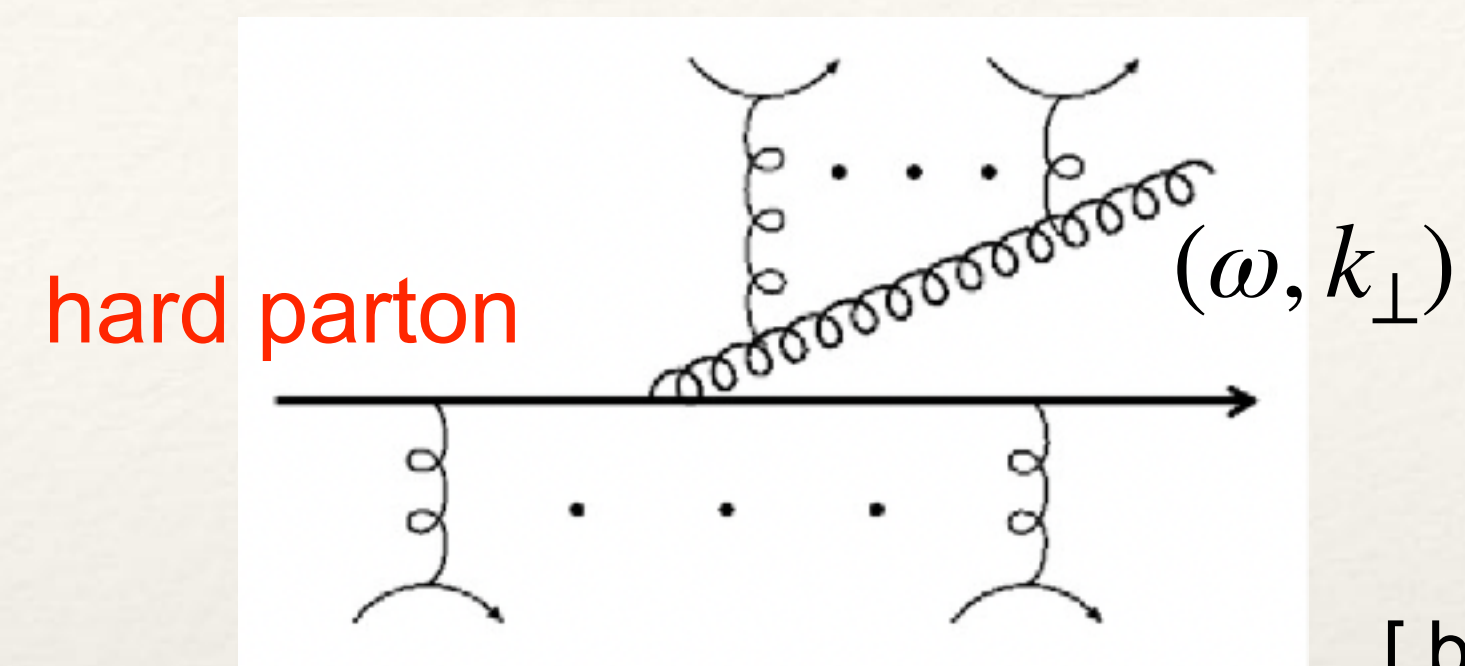
Elastic (collisional)



$$\frac{d\Gamma_{\text{el}}}{d\omega dk_{\perp}^2 dt}(T, E, \dots) = ?$$

Bjorken 1982; Bratten, Thoma 1991;  
Thoma, Gyulassy 1991; Mustafa,  
Thoma 2005; Peigne, Peshier 2006;  
Djordjevic 2006; Wicks *et al.* (DGLV)  
2007; Qin *et al.* (AMY) 2008; ...

Inelastic (radiative)



[ by G.-Y. Qin ]


$$\frac{d\Gamma_{\text{inel}}}{d\omega dk_{\perp}^2 dt}(T, E, \dots) = ?$$

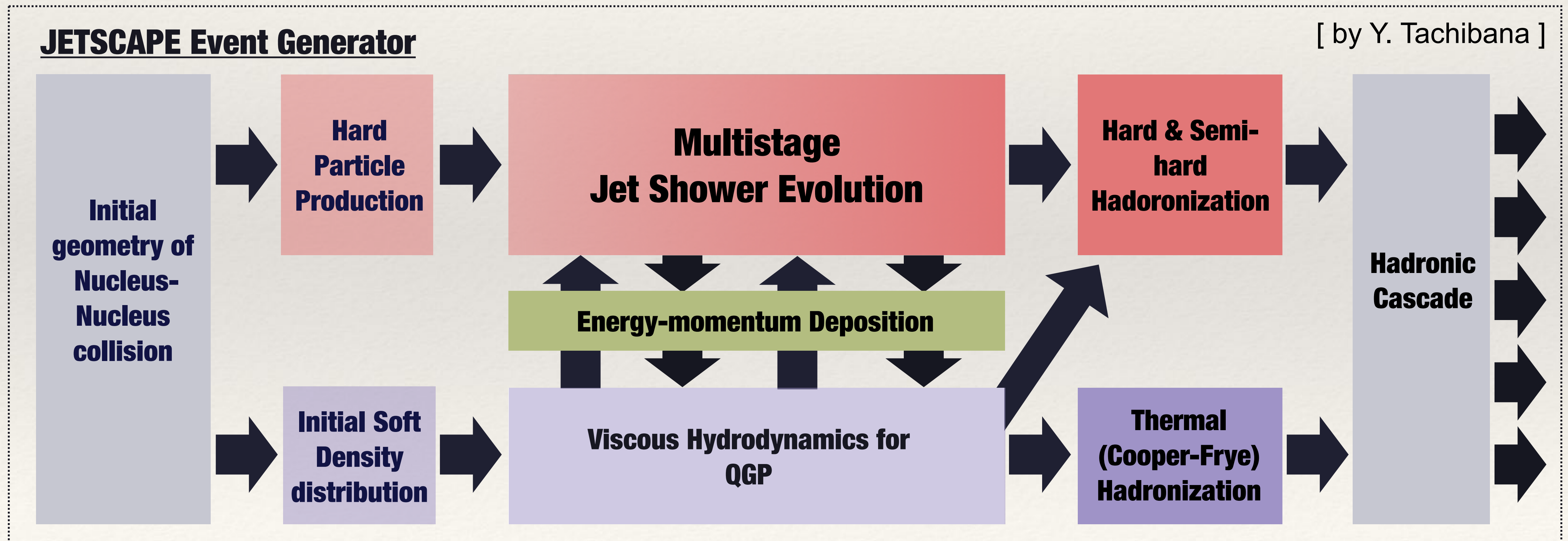
**BDMPS-Z:** Baier-Dokshitzer-Mueller-Peigne-Schiff-Zakharov  
**ASW:** Amesto-Salgado-Wiedemann  
**AMY:** Arnold-Moore-Yaffe (& Caron-Huot, Gale)  
**GLV:** Gyulassy-Levai-Vitev (& Djordjevic, Heinz)  
**HT:** Wang-Guo (& Zhang, Wang, Majumder)

**Systematic comparisons and reviews:**

Bass *et al.*, *Phys.Rev.C* 79 (2009) 024901; Majumder and Van Leeuwen, *Prog. Part. Nucl. Phys.* 66 (2011) 41;  
JET, *Phys. Rev.C* 90 (2014) 1, 014909; Qin and Wang, *Int. J. Mod. Phys. E* 24 (2015) 11, 1530014

# Multistage jet evolution framework

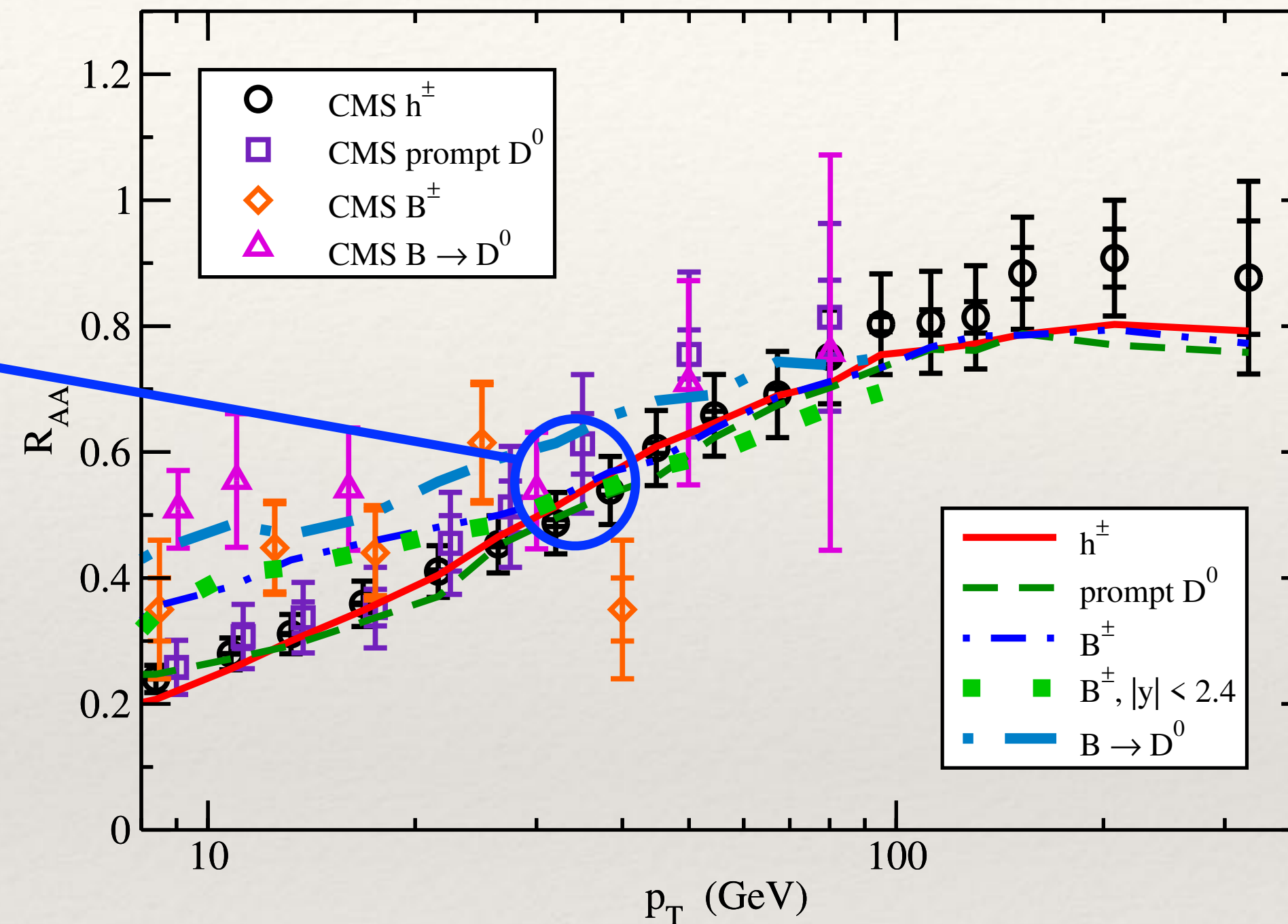
- **Multistage:** high  $Q^2$  — DGLAP-type of evolution; low  $Q^2$  — transport; thermal scale — strongly coupled approach; ...
- Monte-Carlo event generator package for heavy-ion collisions — JETSCAPE
- Open Access:  [github.com/JETSCAPE](https://github.com/JETSCAPE) [arXiv:1903.07706]



# Successful perturbative QCD calculation at high $p_T$

NLO production + **parton interaction with hydrodynamic medium** + fragmentation

Merging of  $D$  and  $B$   
 $R_{AA}$  at  $p_T \sim 40$  GeV



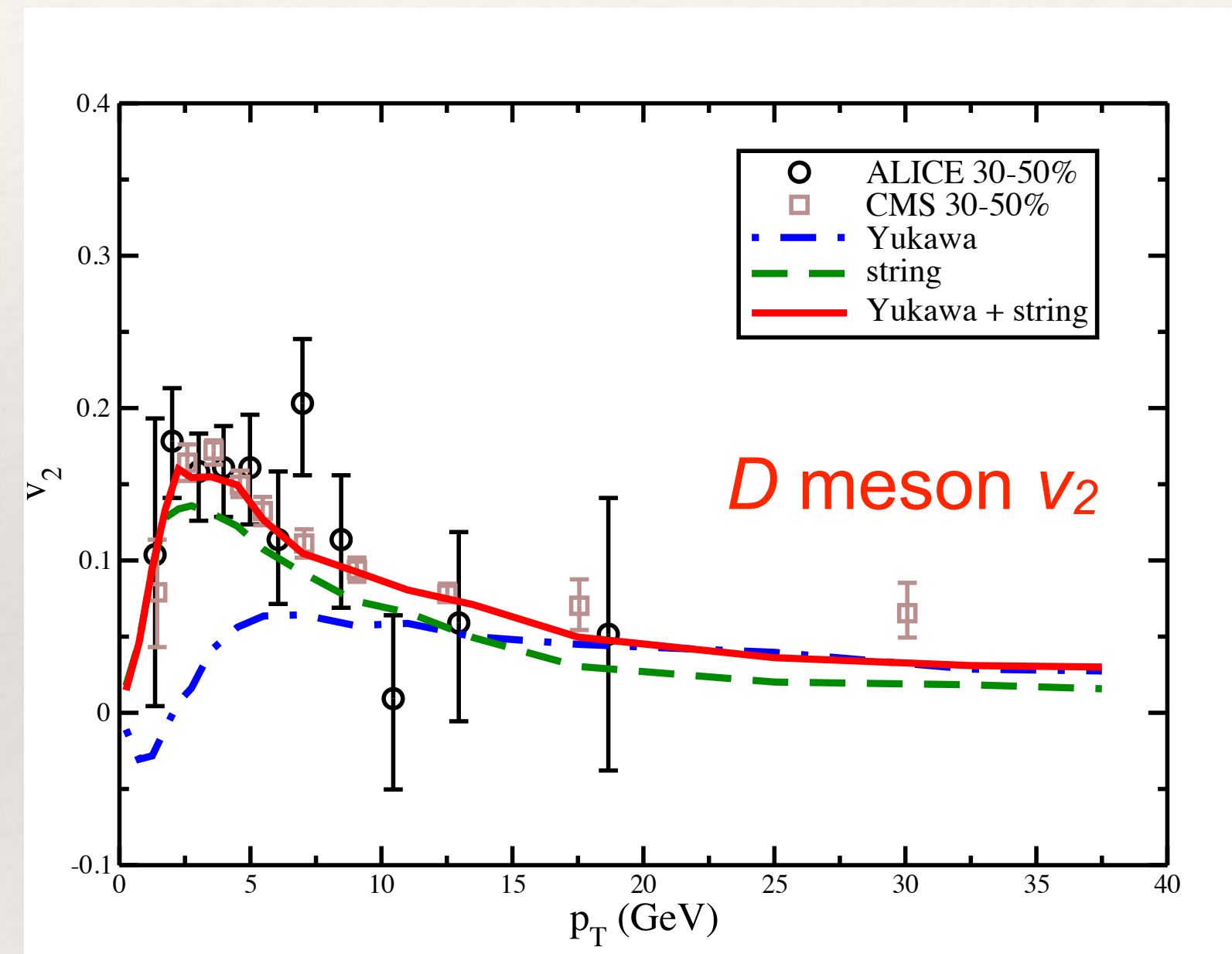
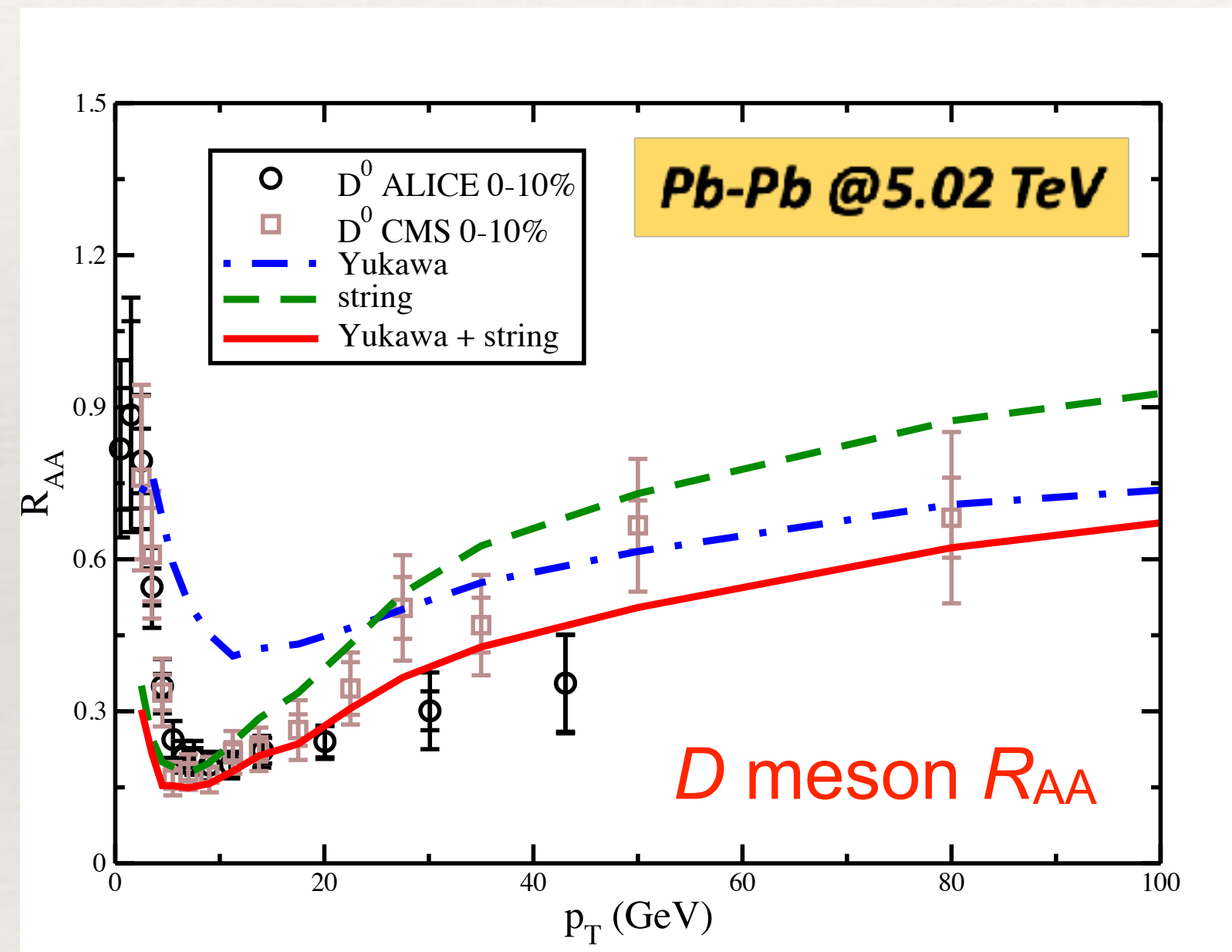
[ Xing, SC, Qin, Xing, Phys. Lett. B 805 (2020) 135424 ]

- A simultaneous description of charged hadron,  $D$  meson,  $B$  meson,  $B$ -decay  $D$  meson  $R_{AA}$ 's starting from  $p_T \sim 8$  GeV
- Predict  $R_{AA}$  separation between  $B$  and  $h / D$  below 40 GeV, but similar values above – **wait for confirmation from future precision measurement**

# Non-perturbative interactions at low $p_T$

Heavy quark interaction with **quasi-particles** → with a **general potential**

$$V(r, T) = -\frac{4}{3}\alpha_s \frac{e^{-m_d r}}{r} - \frac{\sigma}{m_s} e^{-m_s r} \quad (\text{Yukawa} + \text{string, fit to the lattice data})$$

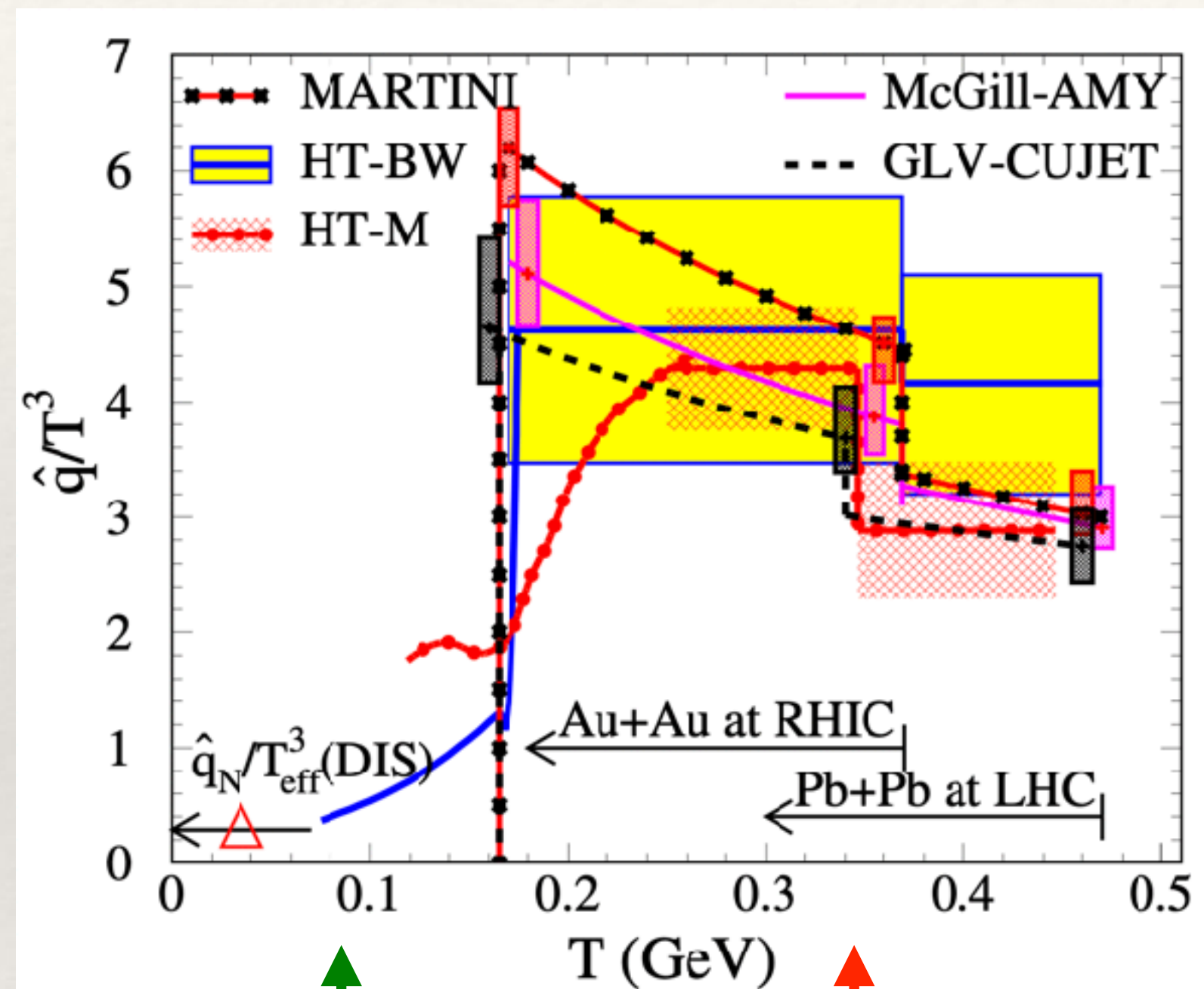


[ Xing, Qin, SC,  
Phys. Lett. B 838  
(2023) 137733 ]

- At **high  $p_T$** , the **Yukawa** interaction dominates heavy-quark-medium interaction
- At **low to intermediate  $p_T$** , the **string** interaction dominates

# Constraints on jet transport coefficient inside the QGP

$$\hat{q} \equiv d\langle k_{\perp}^2 \rangle / dt \sim \langle F^{ai+}(0) F_i^{a+}(y^-) \rangle$$



nucleus  $\ll$  QGP

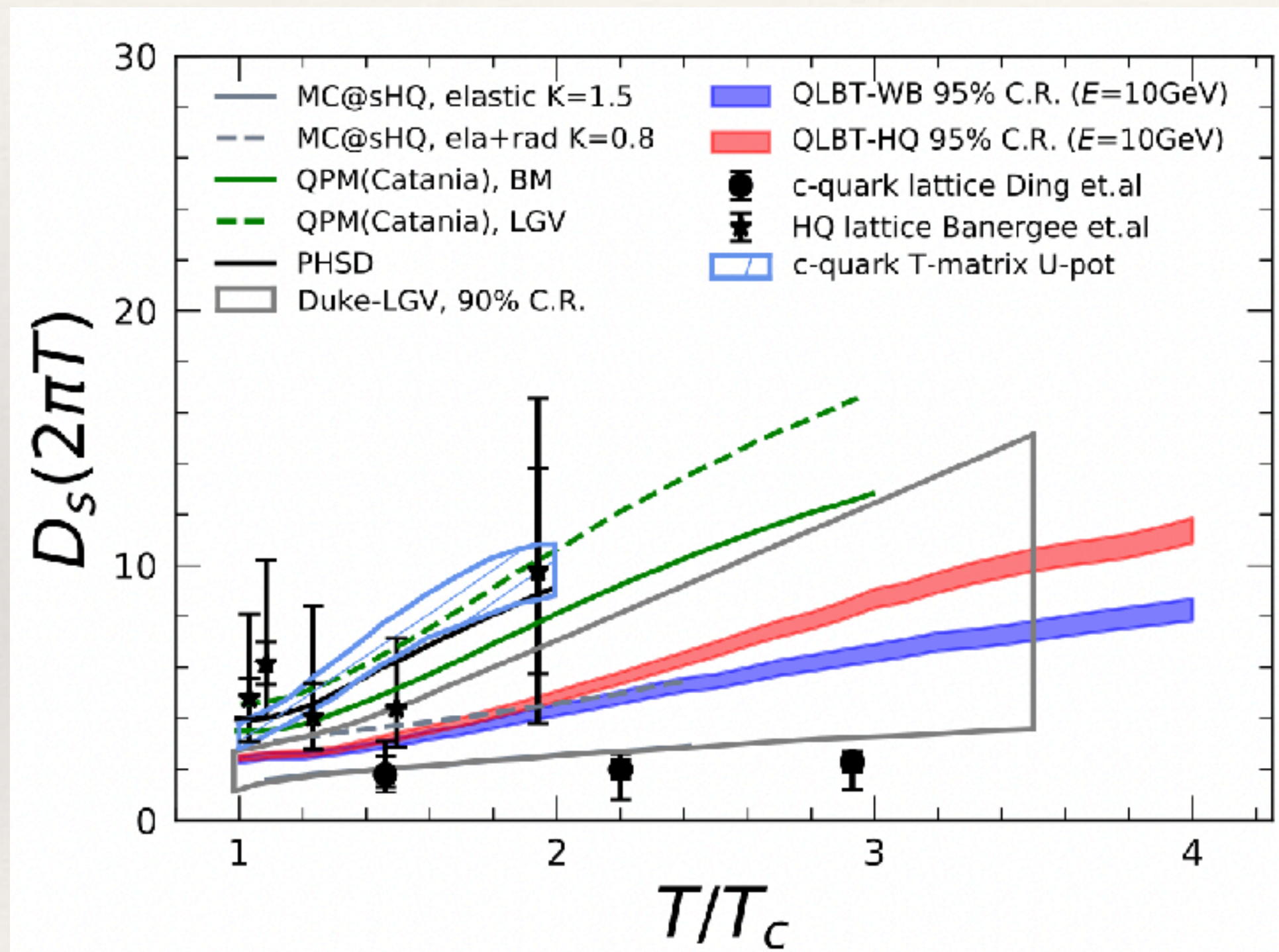
[ JET, Phys. Rev.C 90 (2014) 1, 014909 ]

- QGP is much more opaque than cold nuclear matter to jet propagation
- Recent developments on  $\hat{q}$  extraction:
  - Multistage jet evolution model with Bayesian analysis  
[ JETSCAPE, Phys. Rev. C 104 (2021) 1, 024905]
  - Information field based global interference  
[ Xie et al., arXiv:2206.01340 ]

# Constraints on heavy quark diffusion coefficient

Low energy heavy quark inside the QGP: diffusion (Brownian motion)

Spatial diffusion coefficient:  $D_s \equiv \langle |\vec{x}|^2 \rangle / (2dt)$

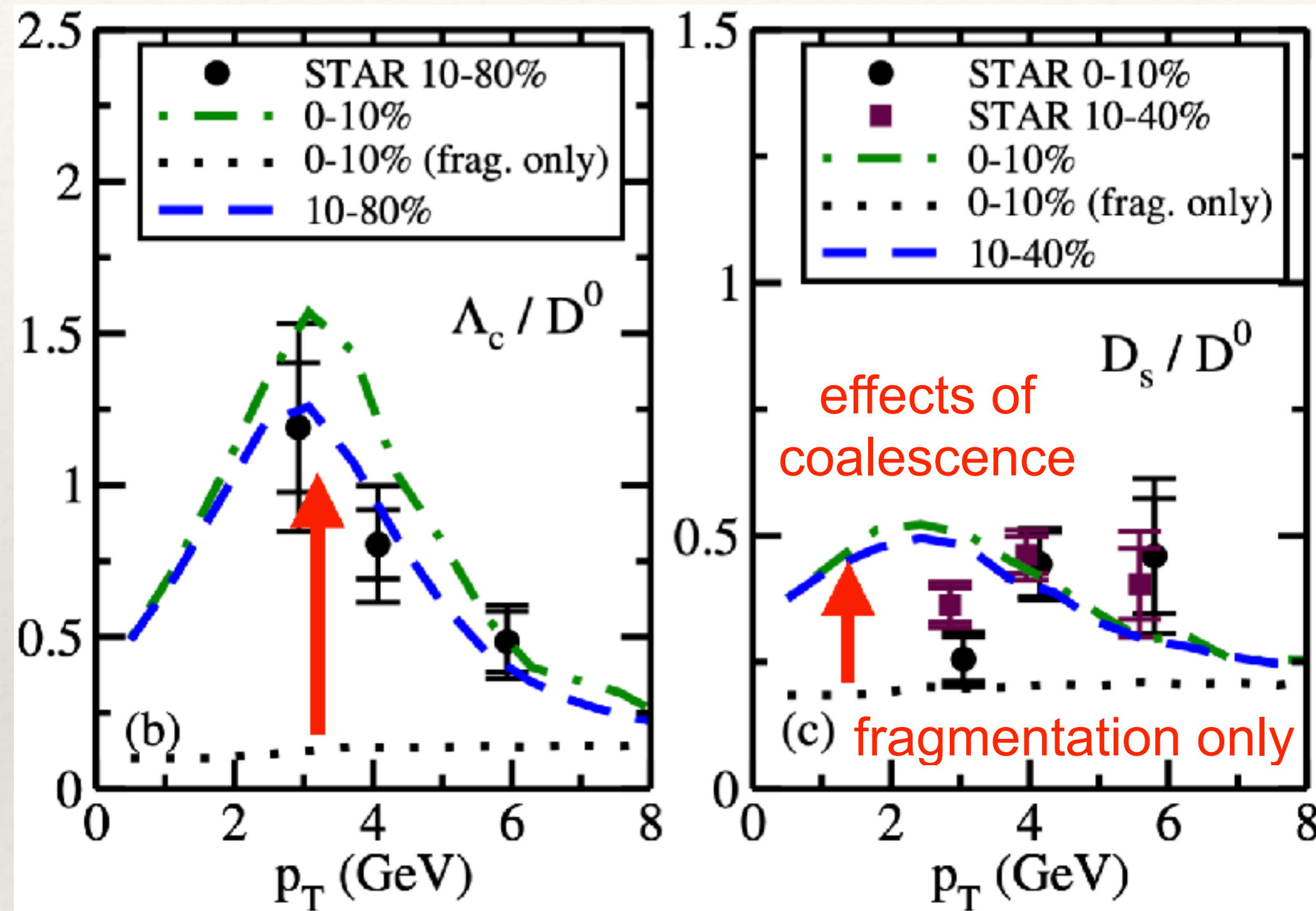


- $D_s(2\pi T) = 2 \sim 6$  extracted from model-to-data comparison
- An order of magnitude smaller than pQCD, close to the strongly coupled limit
- Strongly coupling between low energy heavy quarks and the QGP
- Consistent with the lattice QCD results

[ Liu, Xing, Wu, Qin, SC, Wang, Eur. Phys. J. C 82 (2022) 4, 350 ]

# Constraints on hadron formation and structure

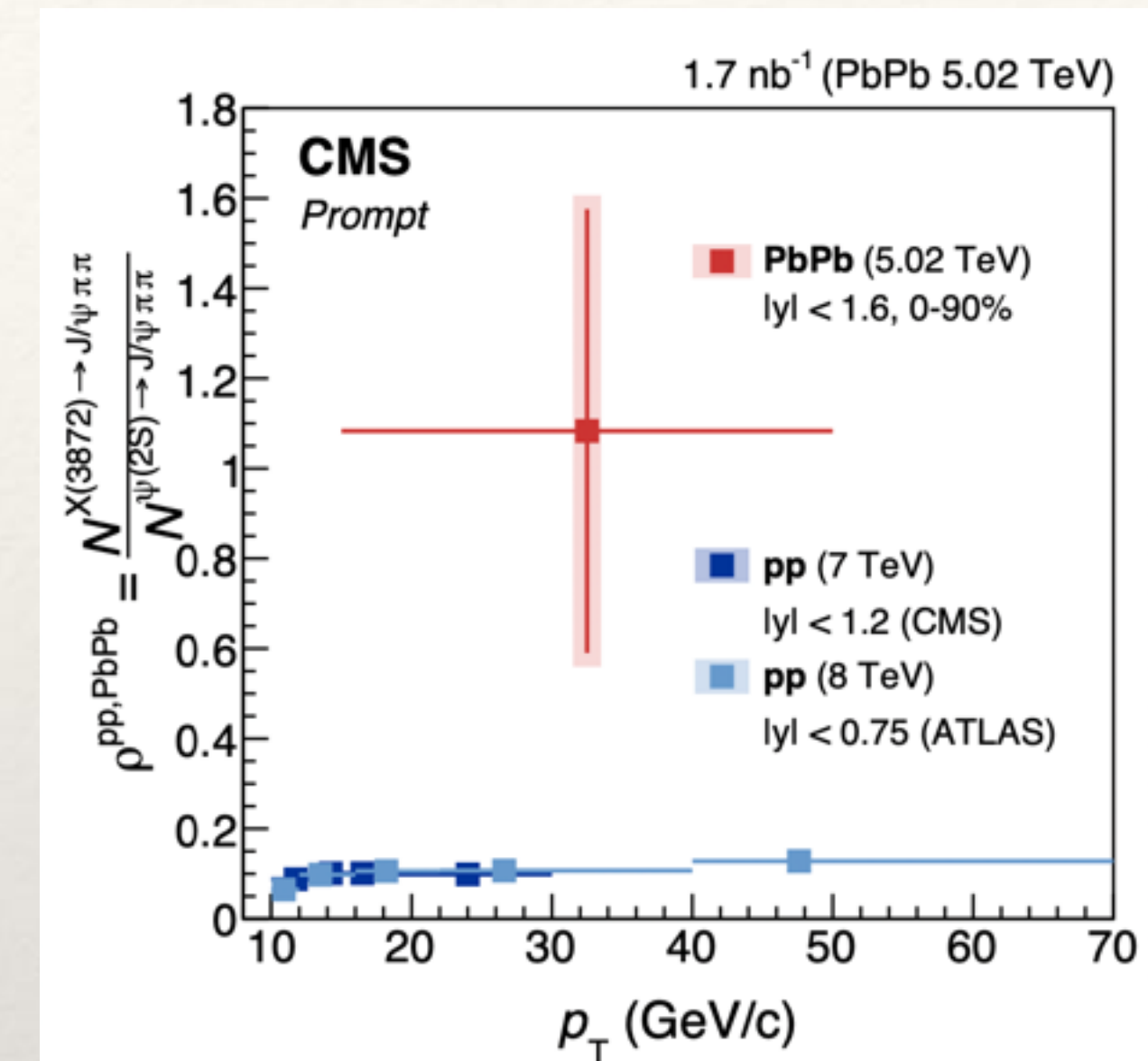
## Charmed hadron chemistry



[ SC *et al.*, Phys. Lett. B 807 (2020) 135561 ]

- Charm coalescence with thermal partons in QGP results in the large  $\Lambda_c / D^0$ ,  $B_s / B^+$ ,  $D_s / D^0$  observed at RHIC and LHC

## X(3872) in heavy-ion collisions

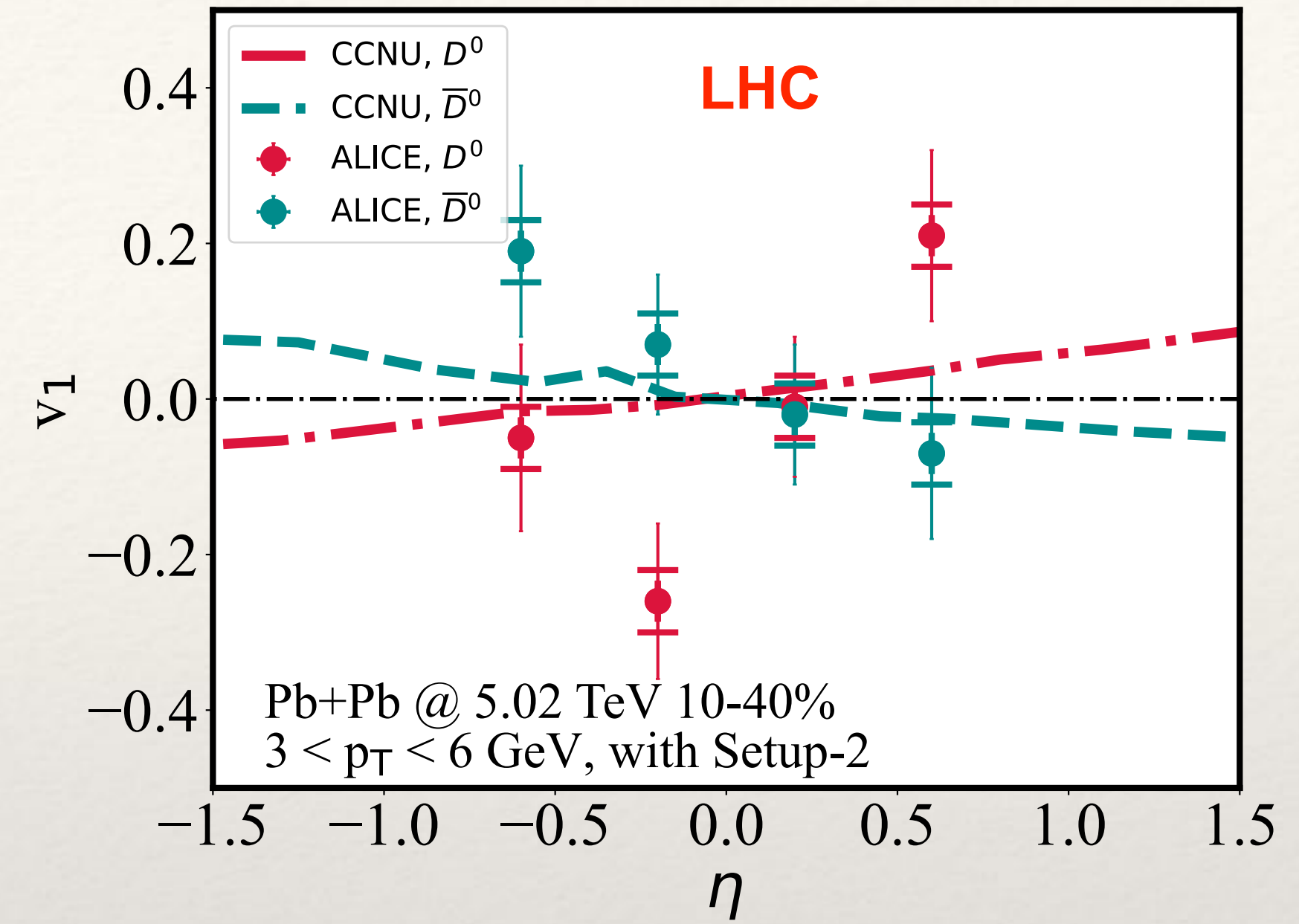
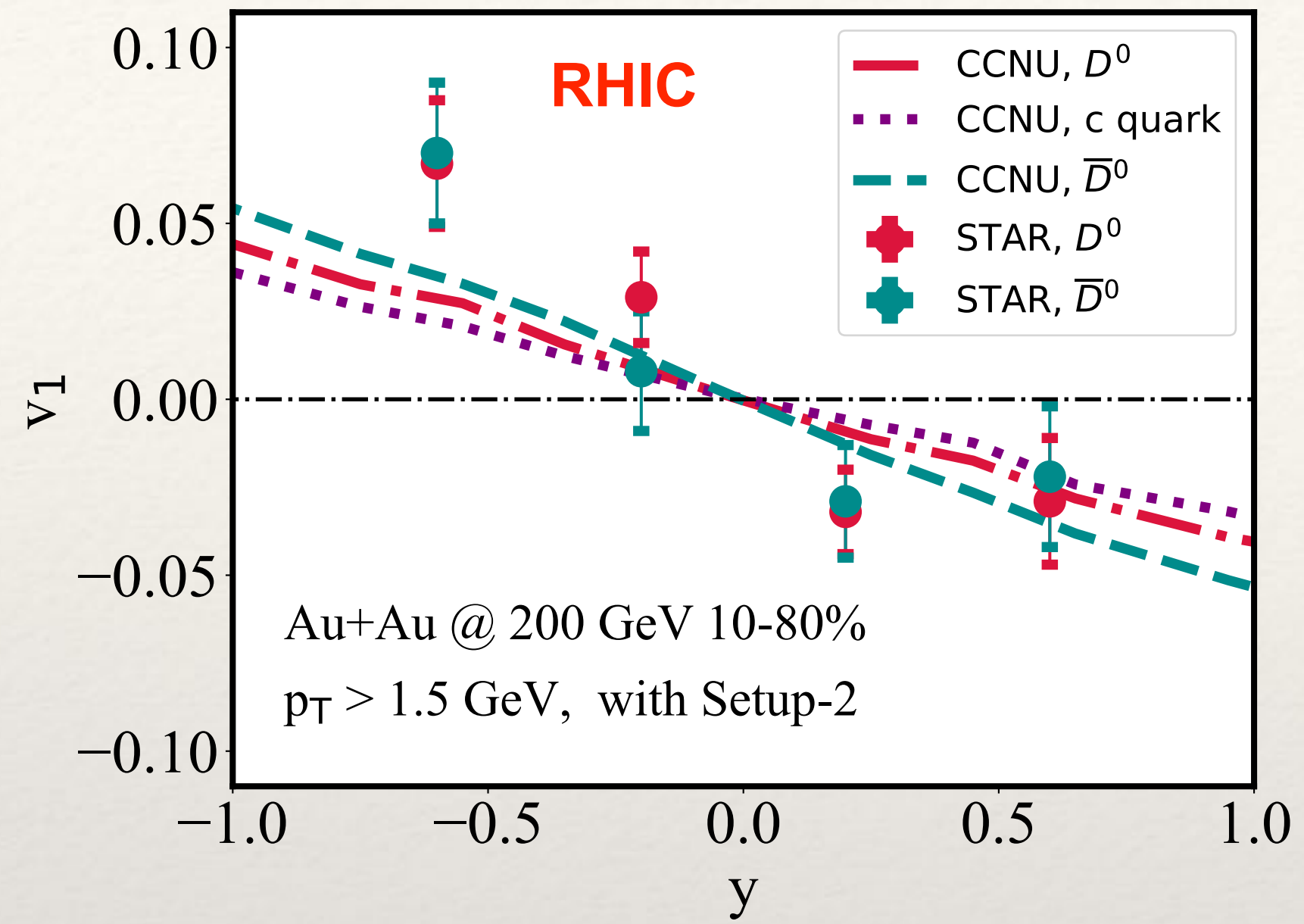


[ Phys. Rev. Lett. 128 (2022) 3, 032001 ]

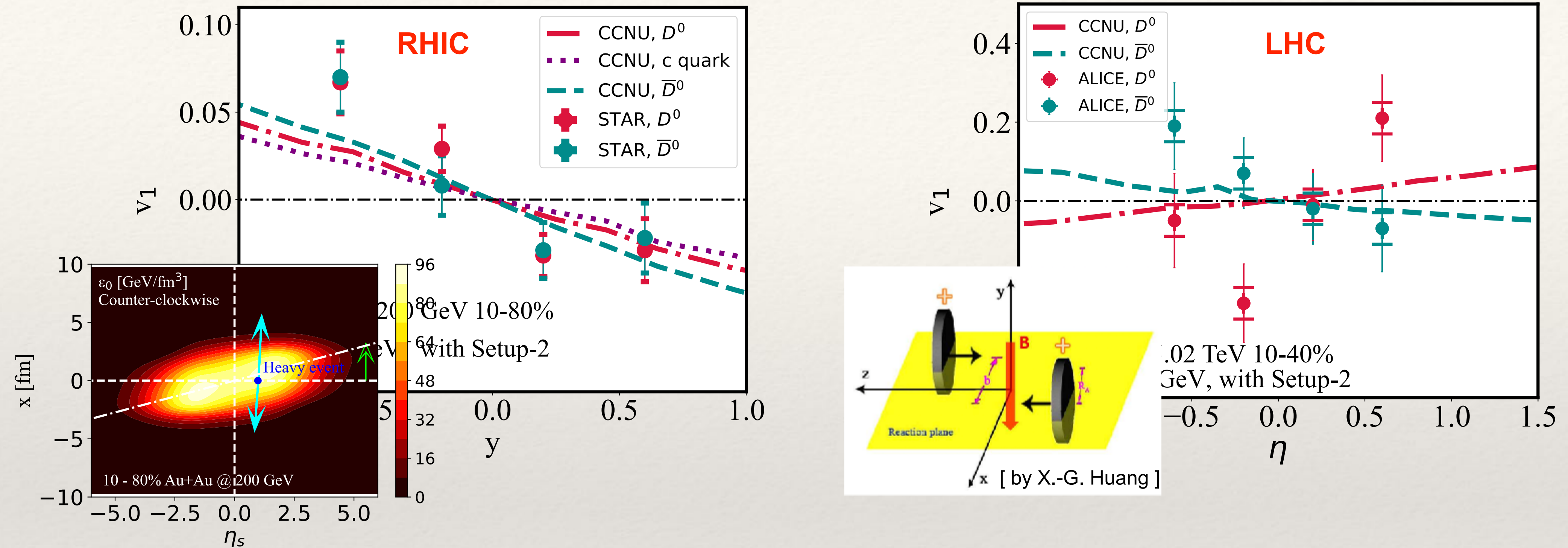
- Novel way of exploring molecule vs. tetraquark states of exotic particles [Cho and Lee, PRC 101 (2020), 2, 024902; Zhang, *et al.*, PRL, 126 (2021) 1, 012301; Wu *et al.*, EPJA, 57 (2021) 4, 122.]
- Need more precise data for conclusion



# Constraints on the E&M field with the $D$ meson $v_1$



# Constraints on the E&M field with the $D$ meson $v_1$

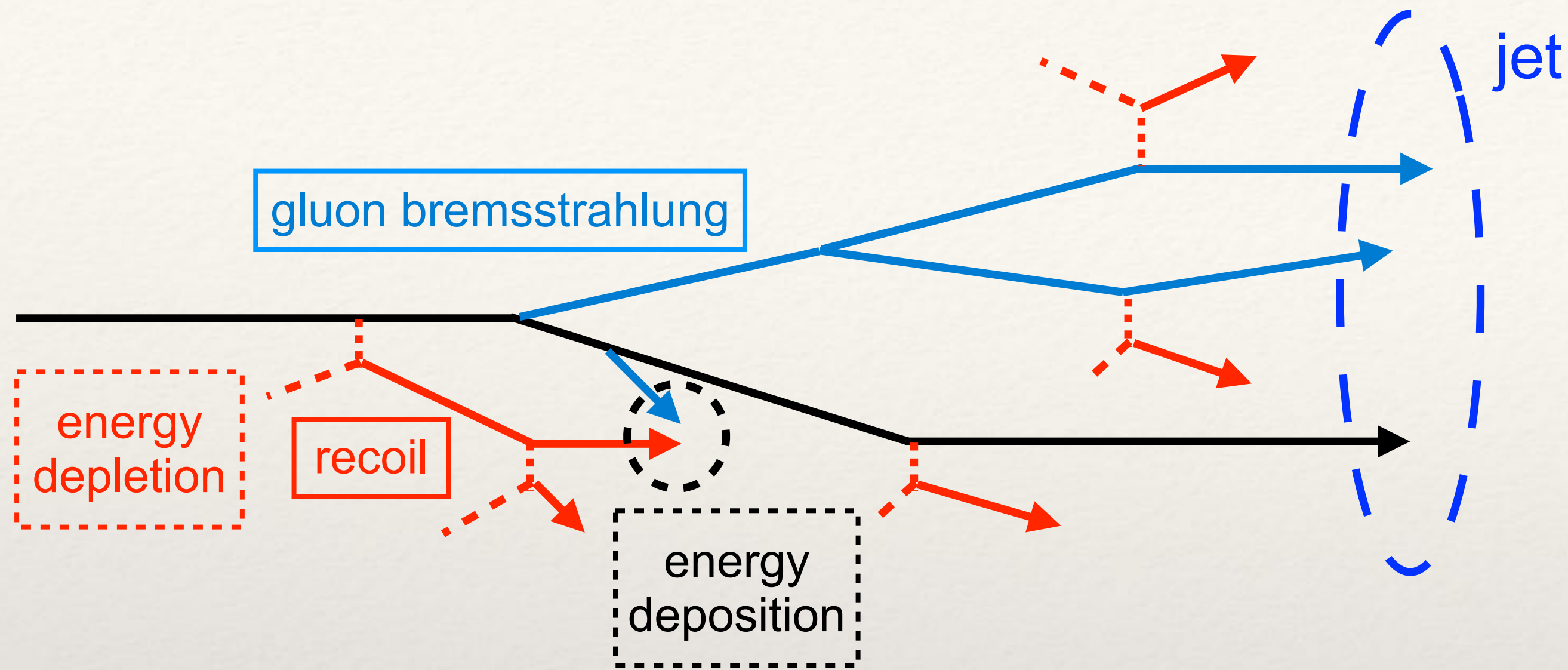


- Tilted geometry w.r.t. the beam direction dominates at the RHIC energy
- Strong E&M field dominates at the LHC energy
- Sensitivity of the  $D$  meson  $v_1$  to different E&M evolution profiles at the LHC

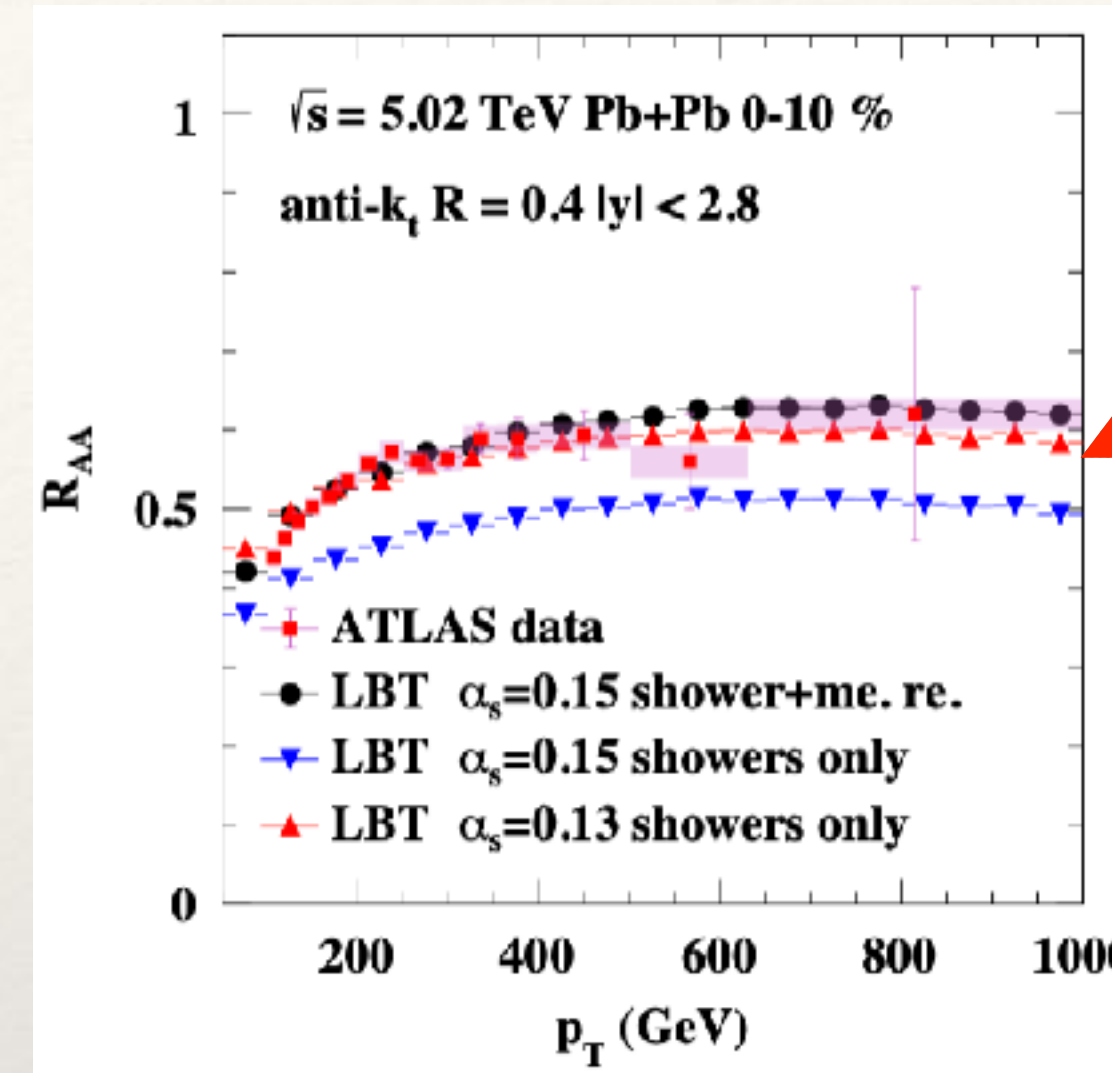
[ Sun, Plumari, Greco, Phys. Lett. B, 816 (2021) 136271]

[ Jiang, SC, Xing, Wu, Yang, Zhang, Phys. Rev. C 105(2022) 5, 054907]

# Fully reconstructed jets

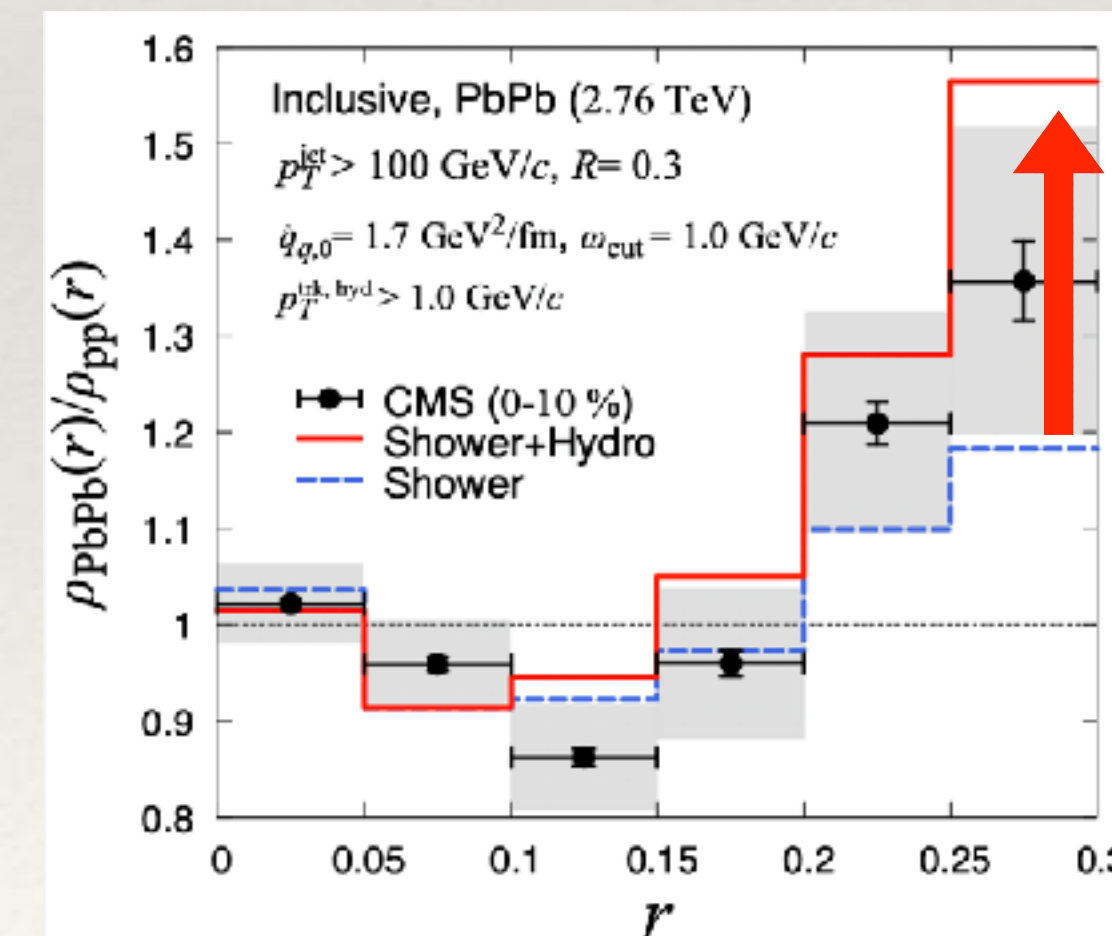


- Jet partons and medium background cannot be cleanly separated in reality
- Medium response (energy deposition + depletion) is naturally included in all jet observables
- Jet-medium interactions: medium modification of jets + medium response



Increase jet  $R_{AA}$

[ He *et al.*, PRC 99 (2019), 054911 ]



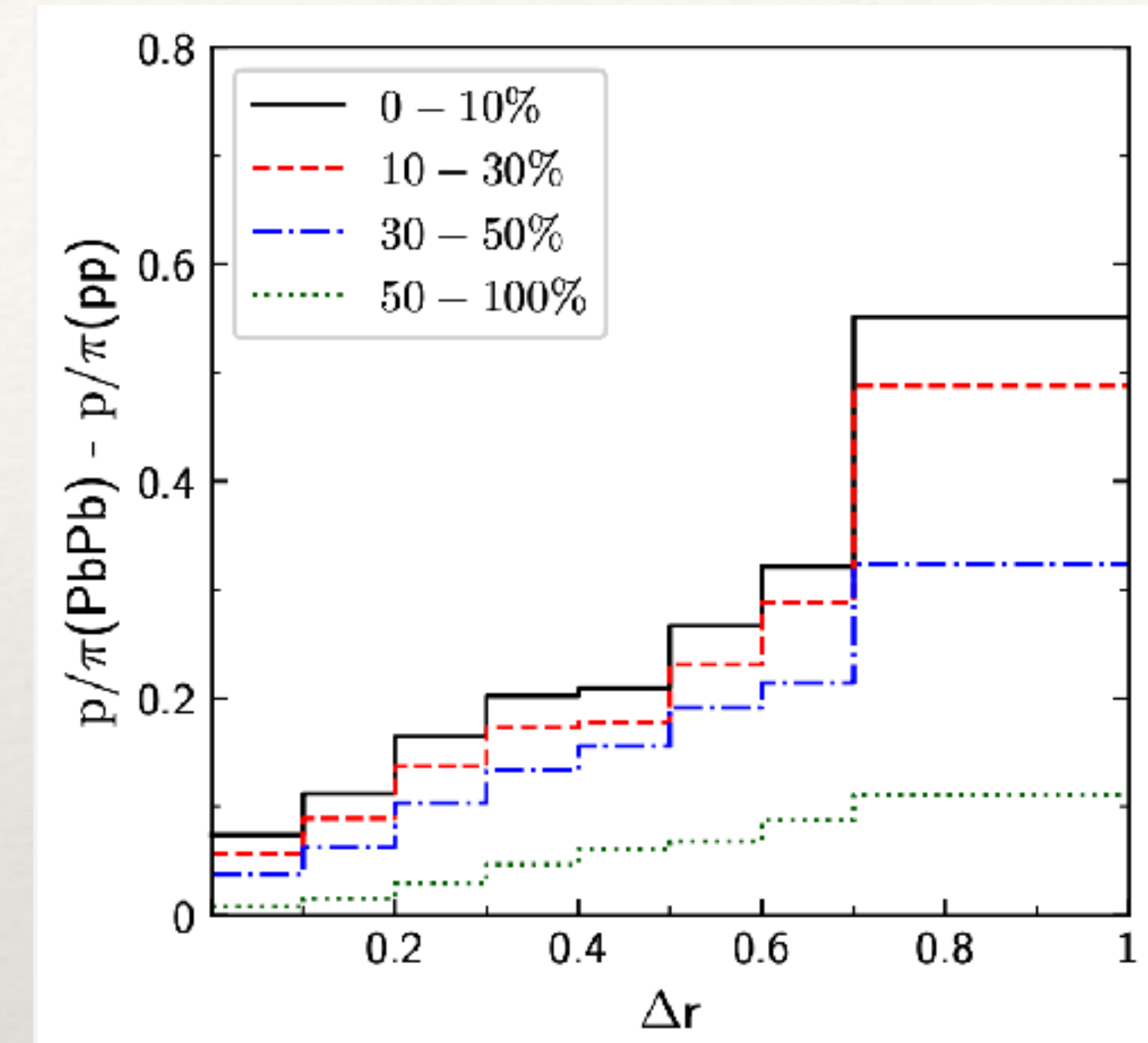
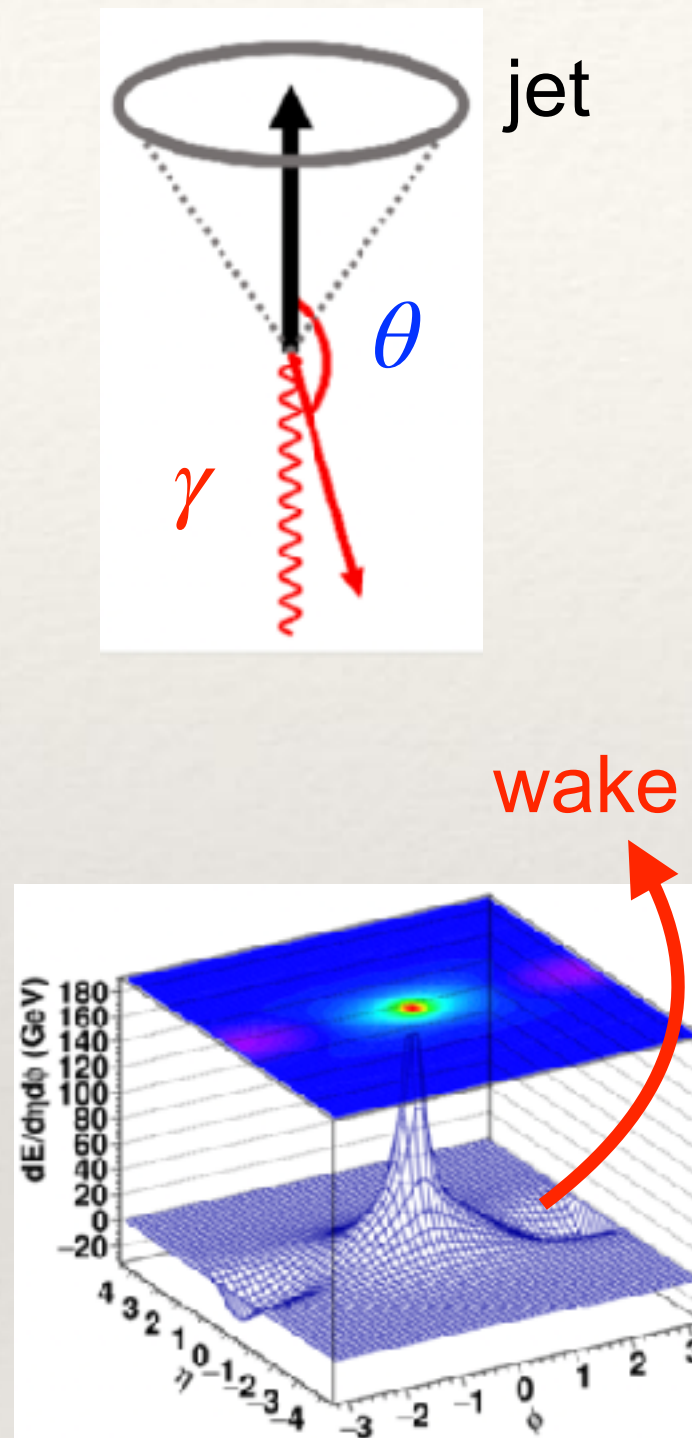
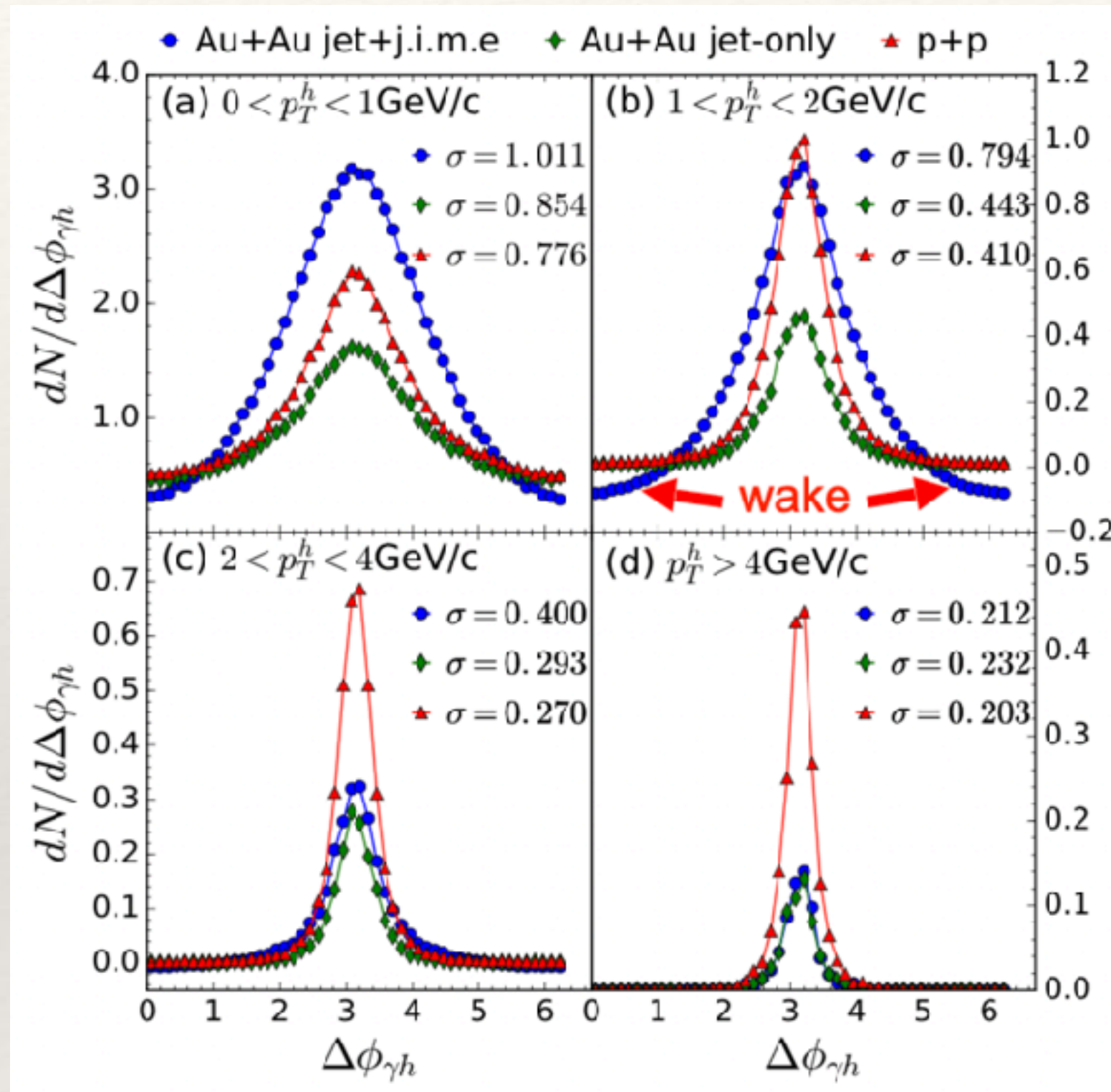
Enhancement of jet energy at large radius

[ Tachibana *et al.*, PRC 95 (2017), 044909 ]

# Search for unique signatures of medium response

Diffusion wake (energy depletion)

Hadron chemistry inside jets



- Diffusion wake predicted in the backward direction of  $\gamma/Z$  at  $1 < p_T^h < 2$  GeV

- Richer baryons inside the QGP than inside a vacuum jet
- Enhanced baryon-to-meson ratio in AA vs. pp collisions

[ Chen, SC, Luo, Pang, Wang, PLB 777 (2018) 86 ]  
 [ Yang, Luo, Chen, Pang, Wang, PRL 130 (2023) 052301 ]

[ Luo, Mao, Qin, Wang, Zhang, PLB 837 (2023) 137638 ]  
 [ Chen, SC, Luo, Pang, Wang, NPA 1005 (2021) 121934 ]

# Summary

- Overview of soft and hard probe theories in relativistic heavy-ion collisions
- Soft hadrons probe the initial geometry and fluctuation, thermal properties, transport coefficients and EoS of the QGP
- Heavy quarks and jets probe the perturbative and non-perturbative interactions, hadronization mechanism, transport coefficient inside the QGP
- More accurate understanding of nuclear matter under extreme conditions with more precise data from future LHC runs, e.g., nucleus geometry, parton energy loss, hadron structure, strong E&M field, ...

*Thank you!*