

# Precision top-quark physics

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Large Hadron Collider Physics Conference  
Belgrade, May 26, 2023

# Outline

- Introduction
- Top-quark pair production
  - NNLO and beyond
  - $t\bar{t}$ ,  $Wt$  and  $b\bar{b}4l$
- $t\bar{t}H$
- Summary

Many more interesting results presented in the Top Physics session

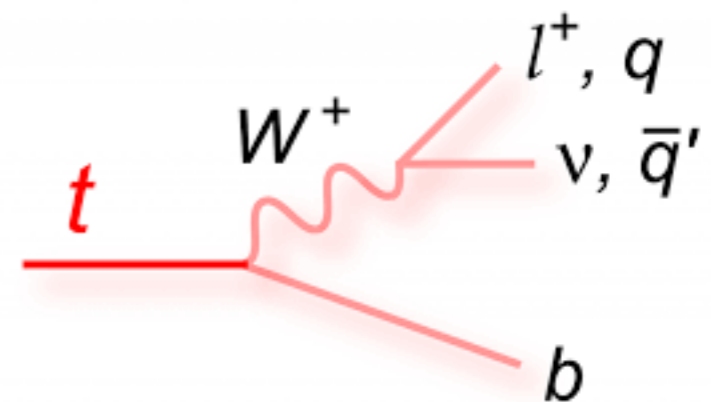
# Introduction

The top quark has a very special place in the Standard Model

- It is the heaviest elementary particle  $m_t \sim 173 \text{ GeV}$  →  $y_t \sim 1$
- It couples strongly to the Higgs boson  $m_t = y_t v / \sqrt{2} \sim 173 \text{ GeV}$
- It decays through EW interaction before hadronizing

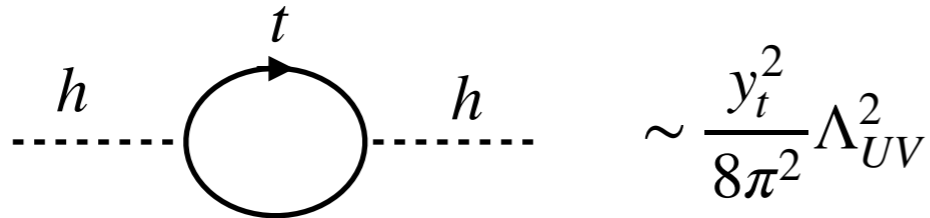
-  $\tau_{\text{had}} \sim 1/\Lambda_{QCD} \sim 10^{-23} \text{ s}$

-  $\tau_t = 1/\Gamma_t \sim \left( G_F m_t^3 |V_{tb}|^2 \right)^{-1} \sim 5 \cdot 10^{-25} \text{ s}$

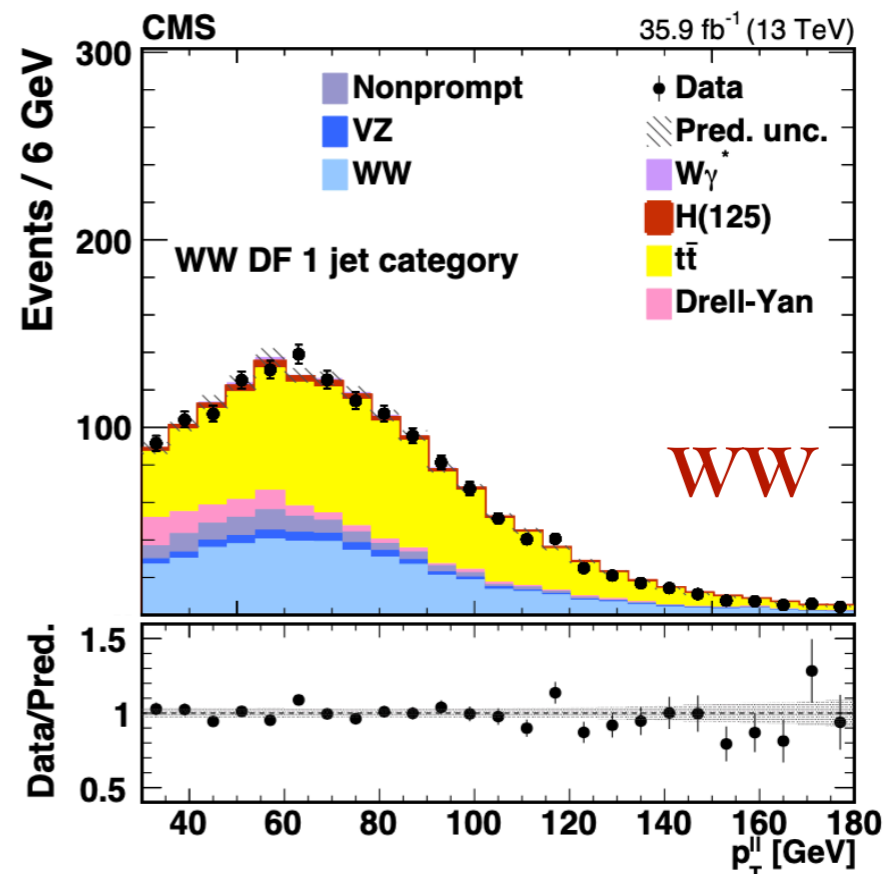
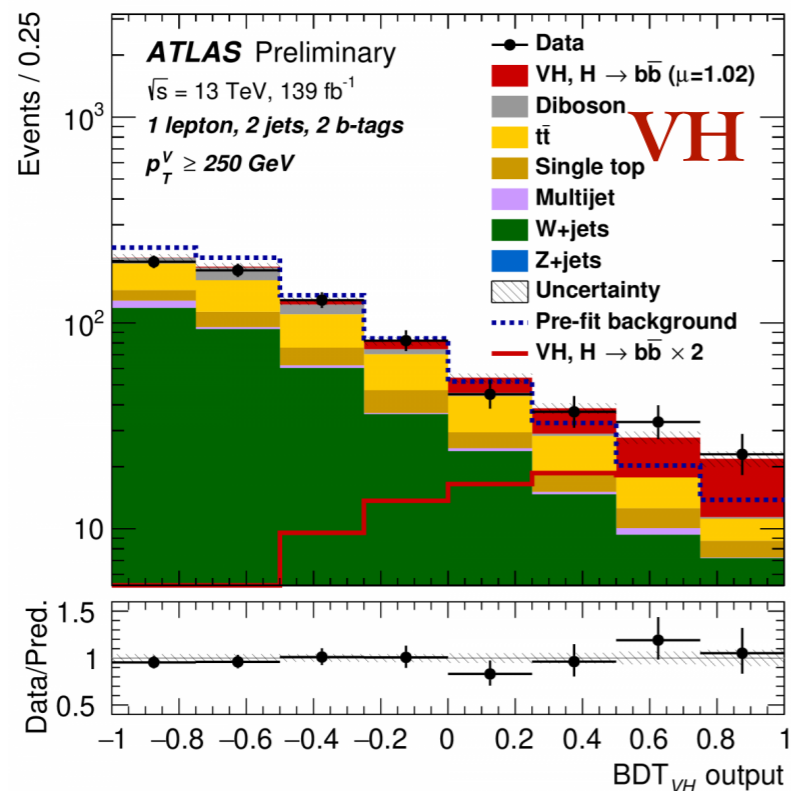


# Introduction

- Possible window on new physics

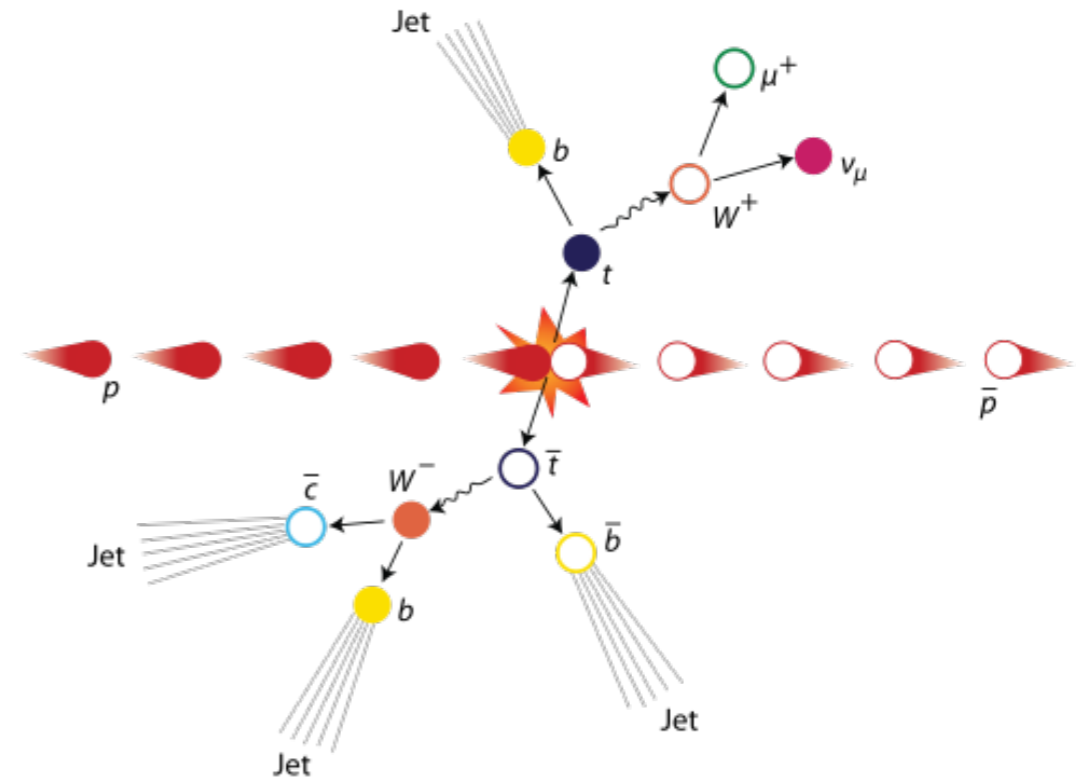


- Events with top quarks provide an ubiquitous background to SM, Higgs measurements and new physics searches

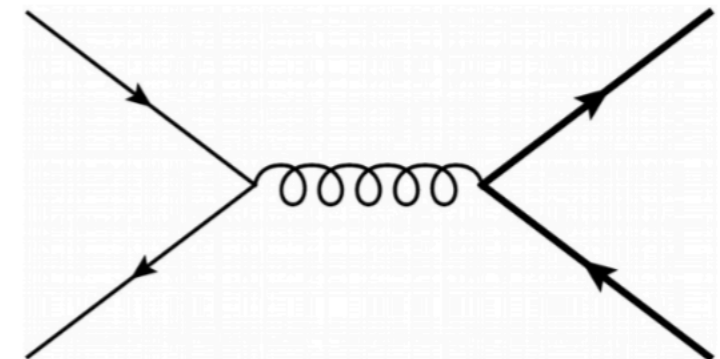
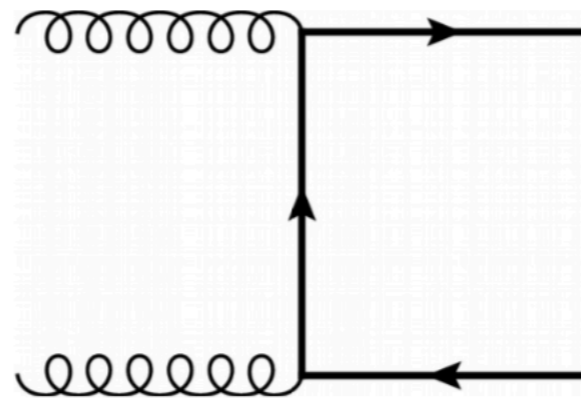
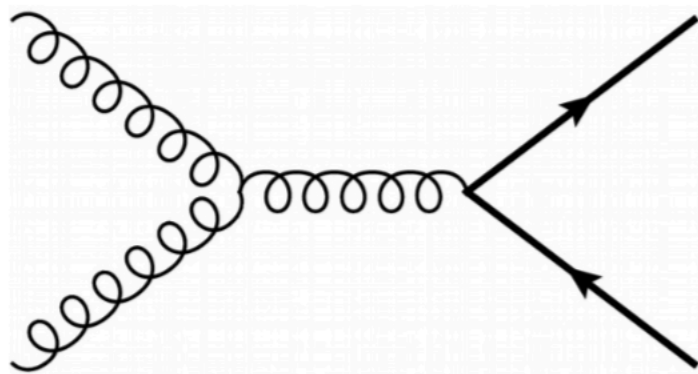


# Introduction

Main source of top-quark events at hadron colliders is  $t\bar{t}$  production



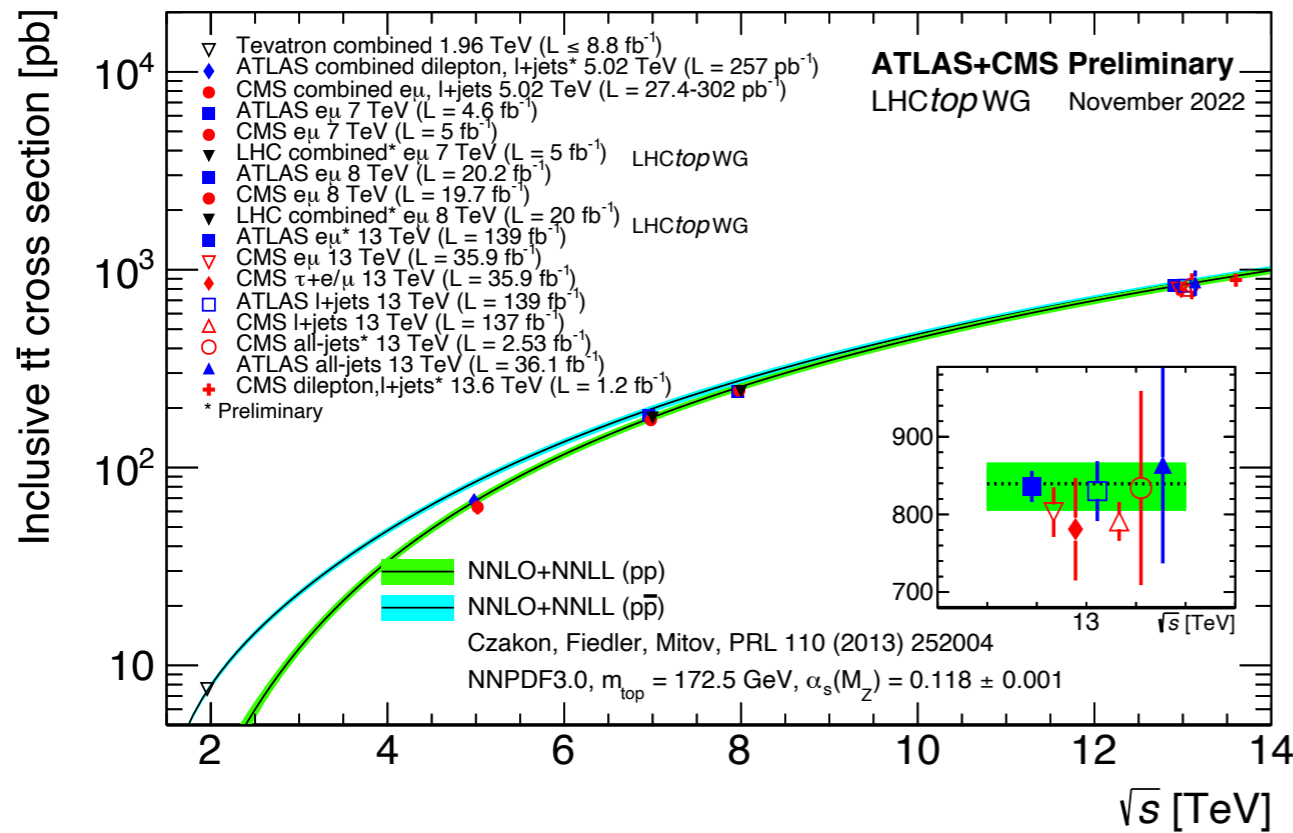
About 15  $t\bar{t}$  events per second at the LHC !



gg contribution dominant  
at the LHC (85% at LO)



# Theoretical status



Inclusive cross section known at  
NNLO+NNLL in QCD

Bärnreuther, Czakon, Mitov (2012)

Czakon, Mitov (2012)

Czakon, Fiedler, Mitov (2013)

Czakon, Fiedler, Heymes, Mitov (2015,2016)

NNLO calculation independently\*  
completed by our group

\*The only common ingredient are the  
two-loop  $gg$  and  $q\bar{q}$  virtual amplitudes

Bärnreuther et al (2013)

For the  $q\bar{q}$  channel recently confirmed by  
fully analytical calculation

Mastrolia et al (2022)

$\sigma_{\text{NNLO}}$ [pb]	MATRIX	TOP++
8 TeV	$238.5(2)^{+3.9\%}_{-6.3\%}$	$238.6^{+4.0\%}_{-6.3\%}$
13 TeV	$794.0(8)^{+3.5\%}_{-5.7\%}$	$794.0^{+3.5\%}_{-5.7\%}$
100 TeV	$35215(74)^{+2.8\%}_{-4.7\%}$	$35216^{+2.9\%}_{-4.8\%}$

Excellent agreement with Top++ !

Catani, Devoto, Kallweit, Mazzitelli, Sargsyan, MG(2019)

# MATRIX<sub>v</sub>2.1

Terminal — -tcsh — 110x50

```
Last login: Thu May 18 11:10:29 on ttys000
grazzini~>cd Physics/MATRIX_v2.1.0
grazzini~/Physics/MATRIX_v2.1.0>./matrix
```

MATRIX allows the user to evaluate **fully differential cross sections** for a wide class of processes at hadron colliders in **NNLO QCD**, **NLO EW** and **NLO QCD** for the loop-induced contribution

Publicly available here

<http://matrix.hepforge.org>

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grazzini~/Physics/MATRIX_v2.1.0>./matrix

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M A T R I X
Version: 2.1.0                               Mar 2023
Reference: arXiv:1711.06631

Munich -- the MUlti-chaNnel Integrator at swiss (CH) precision --
Automates qT-subtraction and Resummation to Integrate X-sections

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M. Wiesemann                               (maris.wiesemann@cern.ch)

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MATRIX is based on a number of different computations and tools
from various people and groups. Please acknowledge their efforts
by citing the references in CITATIONS.bib created with every run.

<<MATRIX-MAKE>> This is the MATRIX process compilation.
<<MATRIX-READ>> Type process_id to be compiled and created. Type "list" to show
available processes. Try pressing TAB for auto-completion. Type
"exit" or "quit" to stop.
|=====>> list
```



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MATRIX allows the user to evaluate **fully differential cross sections** for a wide class of processes at hadron colliders in **NNLO QCD**, **NLO EW** and **NLO QCD** for the loop-induced contribution

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Version 2.1 includes top-pair production

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Terminal — matrix — 110x50

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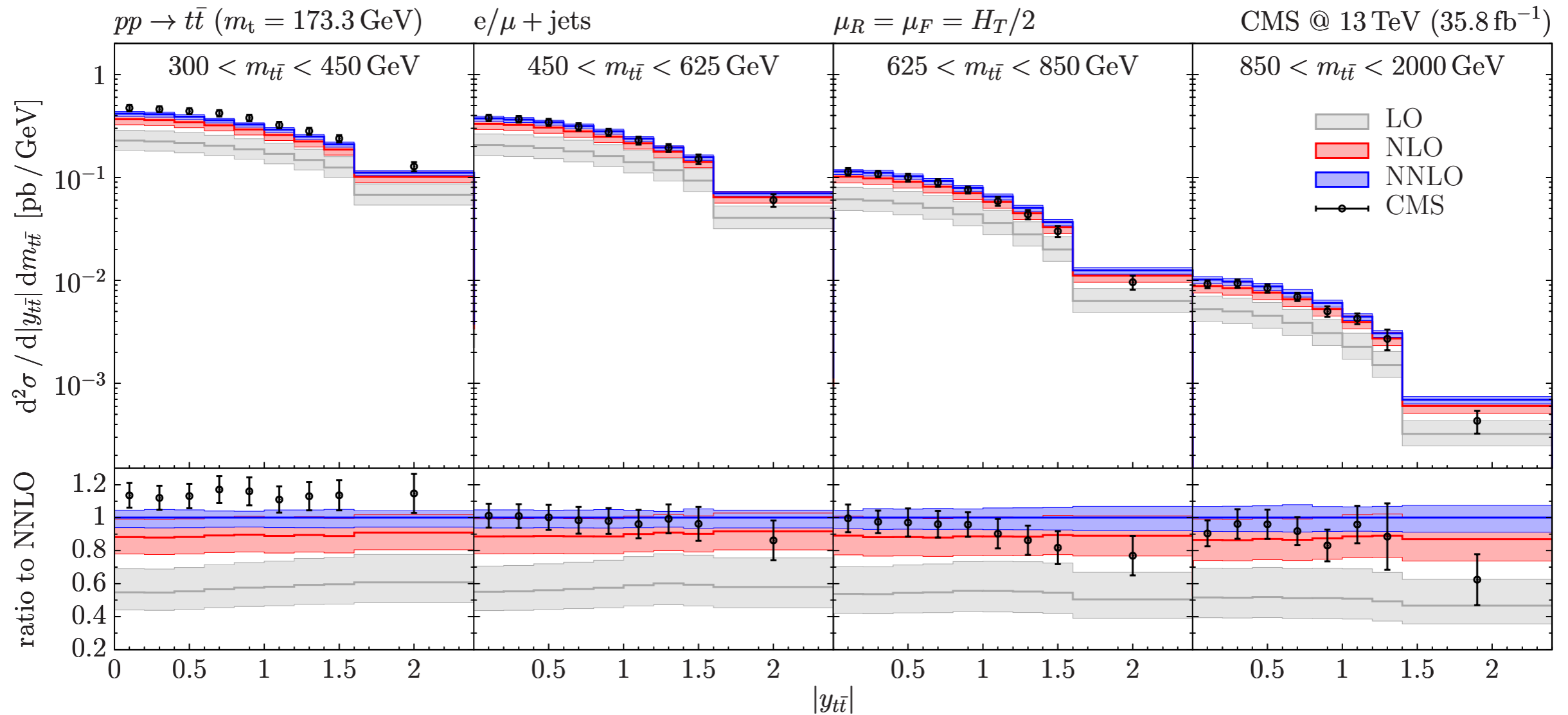
|=====|>> list

-----
process_id || process || description
-----
pph21 >> p p --> H >> on-shell Higgs production (NNLO)
ppz01 >> p p --> Z >> on-shell Z production (NNLO,NLO EW)
ppw01 >> p p --> W^- >> on-shell W- production with CKM (NNLO)
ppwx01 >> p p --> W^+ >> on-shell W+ production with CKM (NNLO)
ppeex02 >> p p --> e^- e^+ >> Z production with decay (NNLO,NLO EW)
ppnenex02 >> p p --> v_e^- v_e^+ >> Z production with decay (NNLO,NLO EW)
ppenex02 >> p p --> e^- v_e^+ >> W- production with decay and CKM (NNLO,NLO EW)
ppexne02 >> p p --> e^+ v_e^- >> W+ production with decay and CKM (NNLO,NLO EW)
ppaa02 >> p p --> gamma gamma >> gamma gamma production (NNLO)
ppeexa03 >> p p --> e^- e^+ gamma >> Z gamma production with decay (NNLO)
ppnenexa03 >> p p --> v_e^- v_e^+ gamma >> Z gamma production with decay (NNLO)
ppenexa03 >> p p --> e^- v_e^+ gamma >> W- gamma production with decay (NNLO)
ppexnea03 >> p p --> e^+ v_e^- gamma >> W+ gamma production with decay (NNLO)
ppzz02 >> p p --> Z Z >> on-shell ZZ production (NNLO)
ppwxw02 >> p p --> W^+ W^- >> on-shell WW production (NNLO)
ppemexmx04 >> p p --> e^- mu^- e^+ mu^+ >> ZZ production with decay (NNLO,NLO gg,NLO EW)
ppeeexex04 >> p p --> e^- e^- e^+ e^+ >> ZZ production with decay (NNLO,NLO gg,NLO EW)
ppeeexnmnm04 >> p p --> e^- e^+ v_mu^- v_mu^+ >> ZZ production with decay (NNLO,NLO gg,NLO EW)
ppemxnmnex04 >> p p --> e^- mu^+ v_mu^- v_e^+ >> WW production with decay (NNLO,NLO gg,NLO EW)
ppeeexnenex04 >> p p --> e^- e^+ v_e^- v_e^+ >> ZZ/WW production with decay (NNLO,NLO gg,NLO EW)
ppemexnm04 >> p p --> e^- mu^- e^+ v_mu^+ >> W-Z production with decay (NNLO,NLO EW)
ppeeexnex04 >> p p --> e^- e^- e^+ v_e^+ >> W-Z production with decay (NNLO,NLO EW)
ppeeexnm04 >> p p --> e^- e^+ mu^+ v_mu^- >> WZ production with decay (NNLO,NLO EW)
ppeeexexne04 >> p p --> e^- e^+ e^+ v_e^- >> W+Z production with decay (NNLO,NLO EW)
ppttx20 >> p p --> top anti-top >> on-shell top-pair production (NNLO)
pnaaa03 >> p p --> gamma gamma gamma >> gamma gamma gamma production (NNLO)

|=====|>>
```

# MATRIX<sub>v</sub>2.1

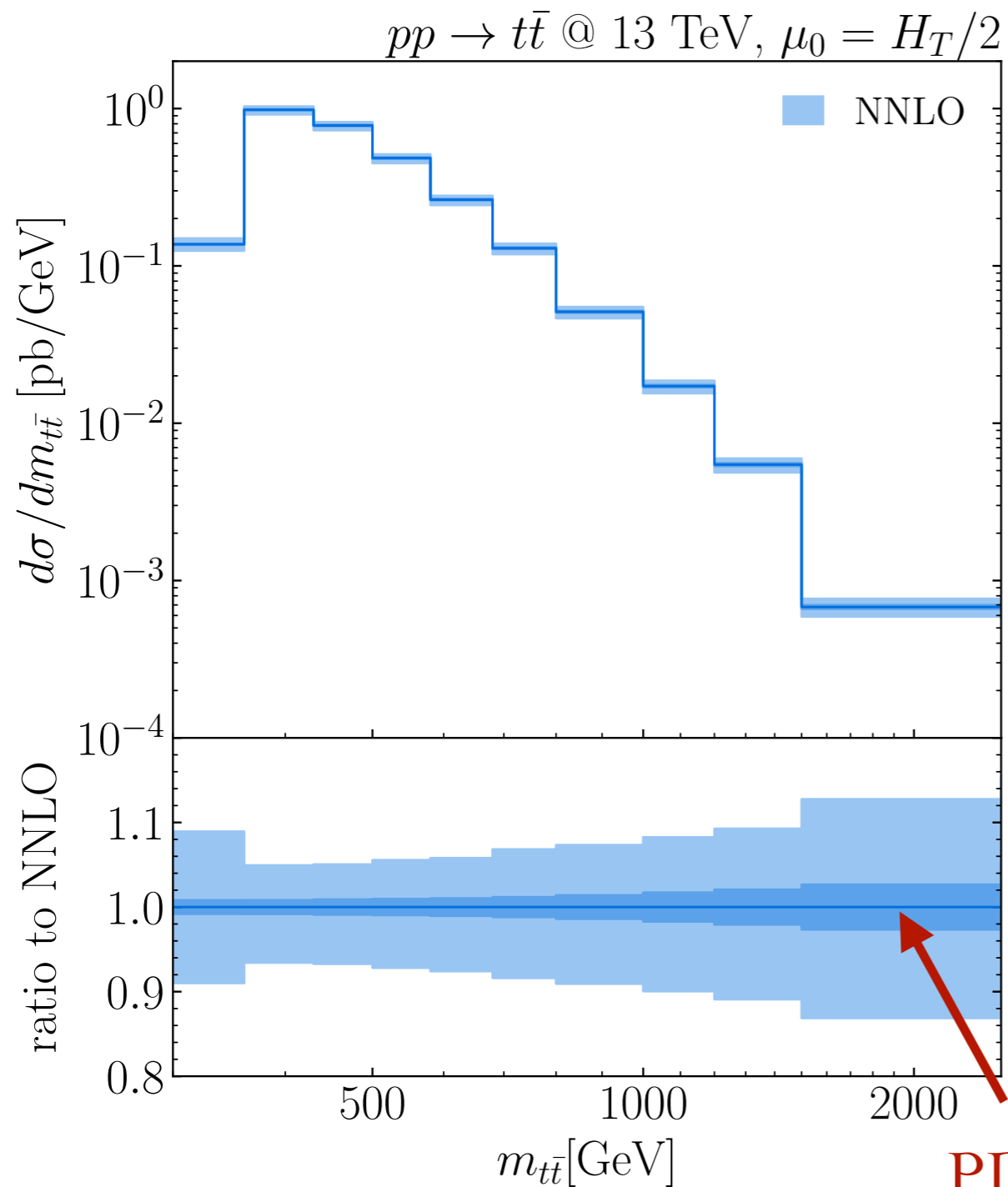
## Multidifferential distributions



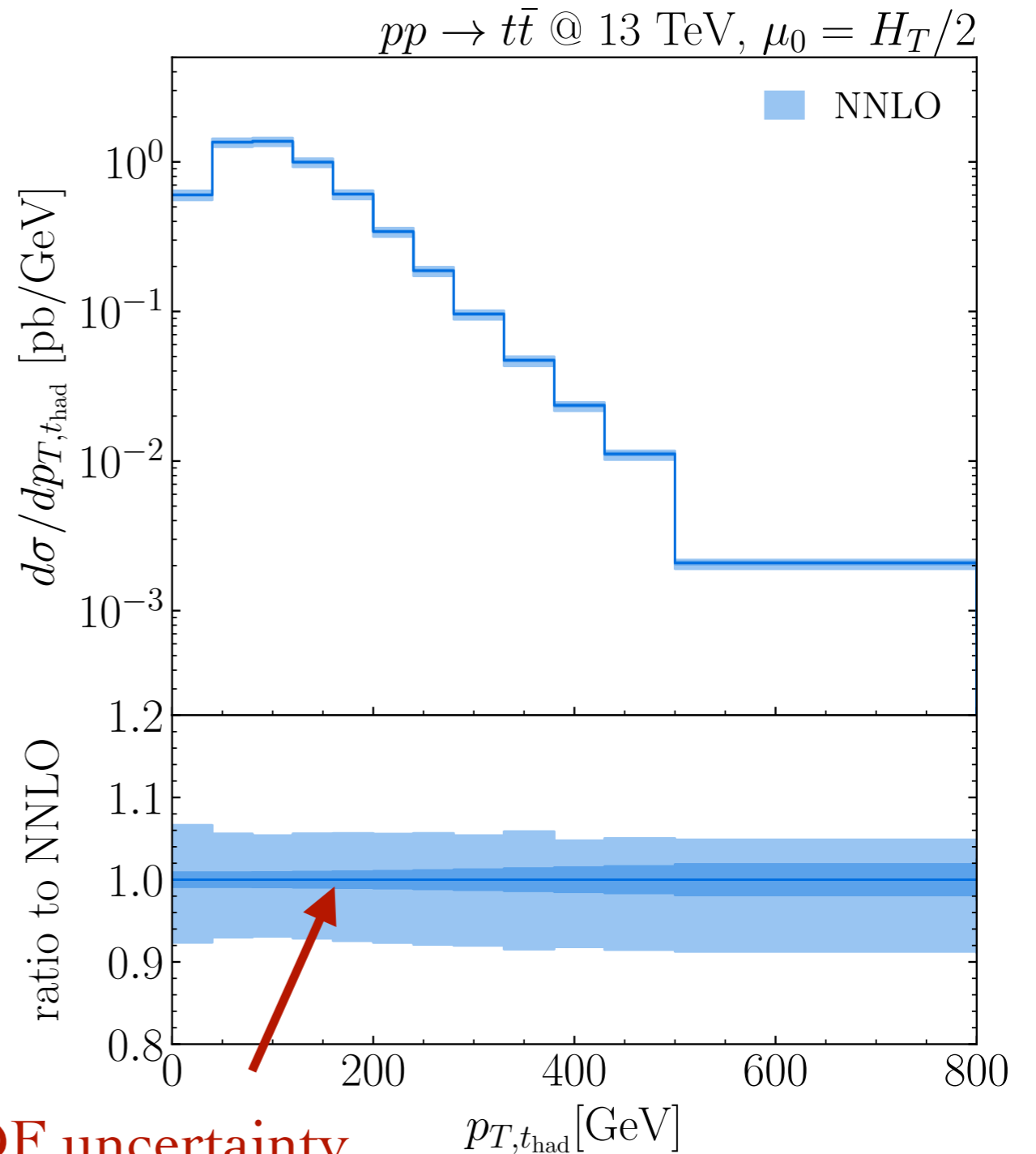
NNLO corrections significantly improve the agreement with the data

**NEW:** PDF uncertainties: **MATRIX+PineAPPL** interface

Devoto, Jezo, Kallweit,  
Schwan (in preparation)



PDF uncertainty



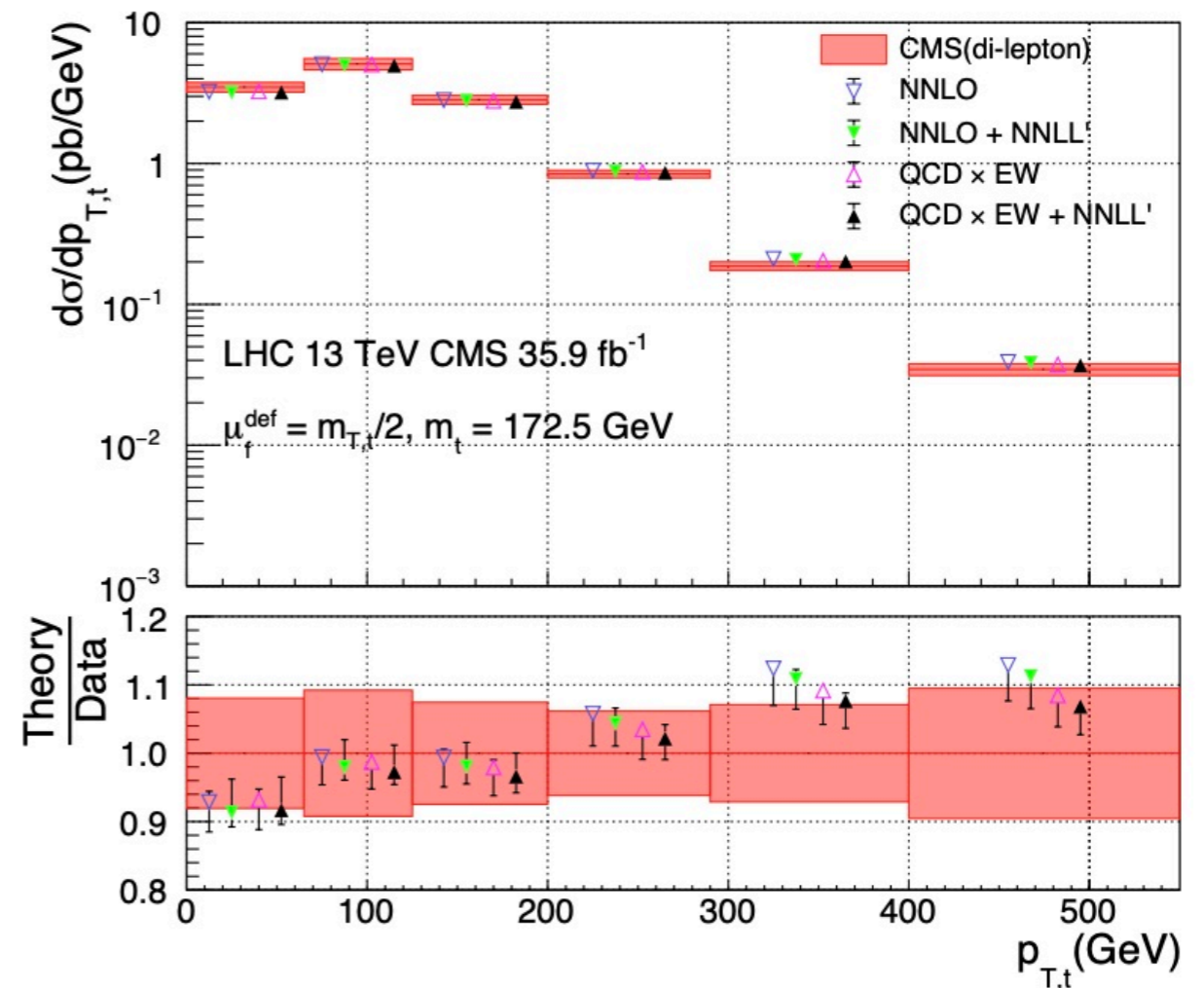
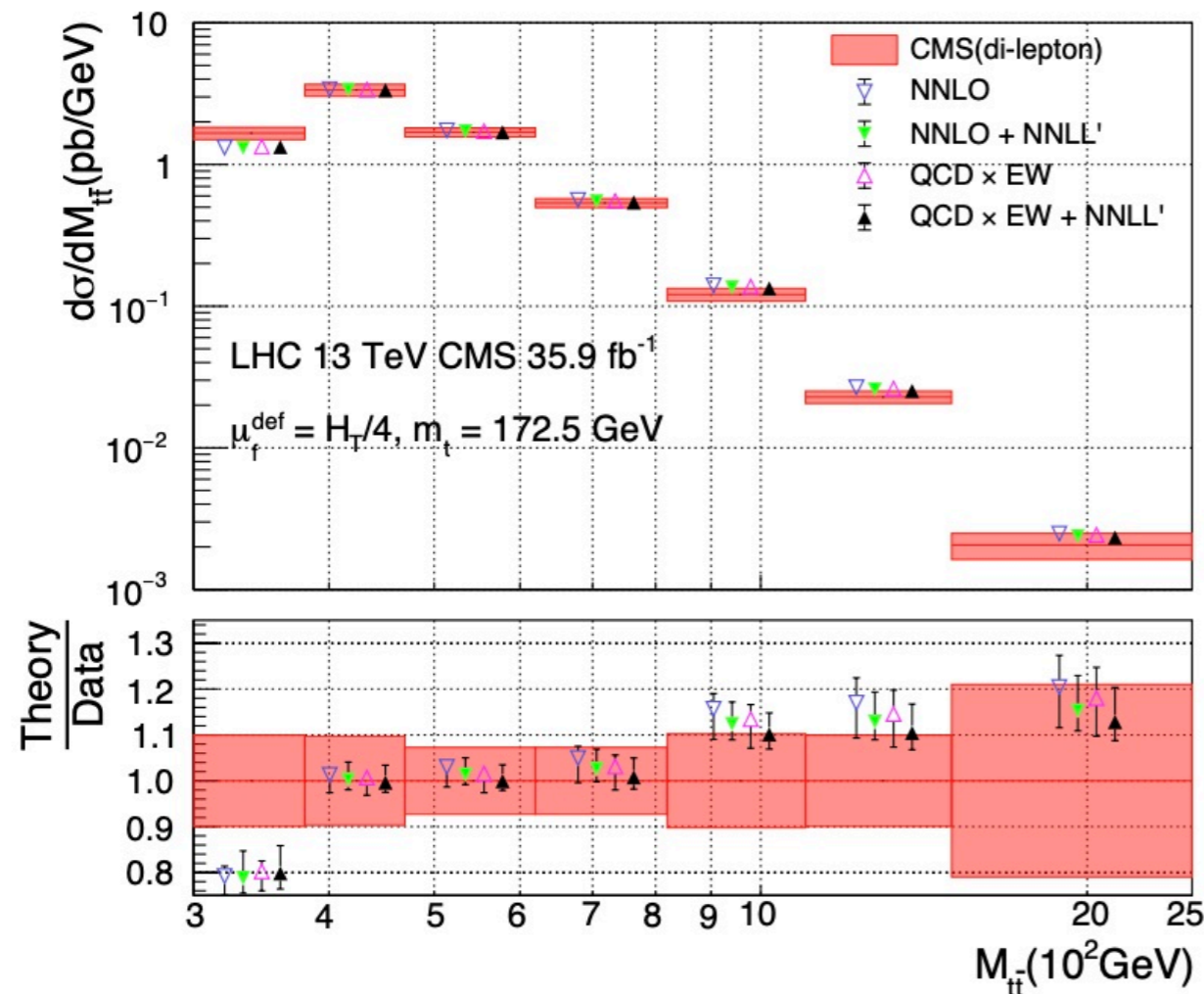
Plots: courtesy S. Devoto

# Beyond NNLO effects

Further effects that can/should be included are EW corrections and soft-gluon resummations at small and large invariant masses

Zaro et al (2019)

Relatively small impact but slightly improves the agreement with the data



Still threshold region not properly described

Resummation of Coulomb effects partially improves the situation

L. L. Yang et al (2019)

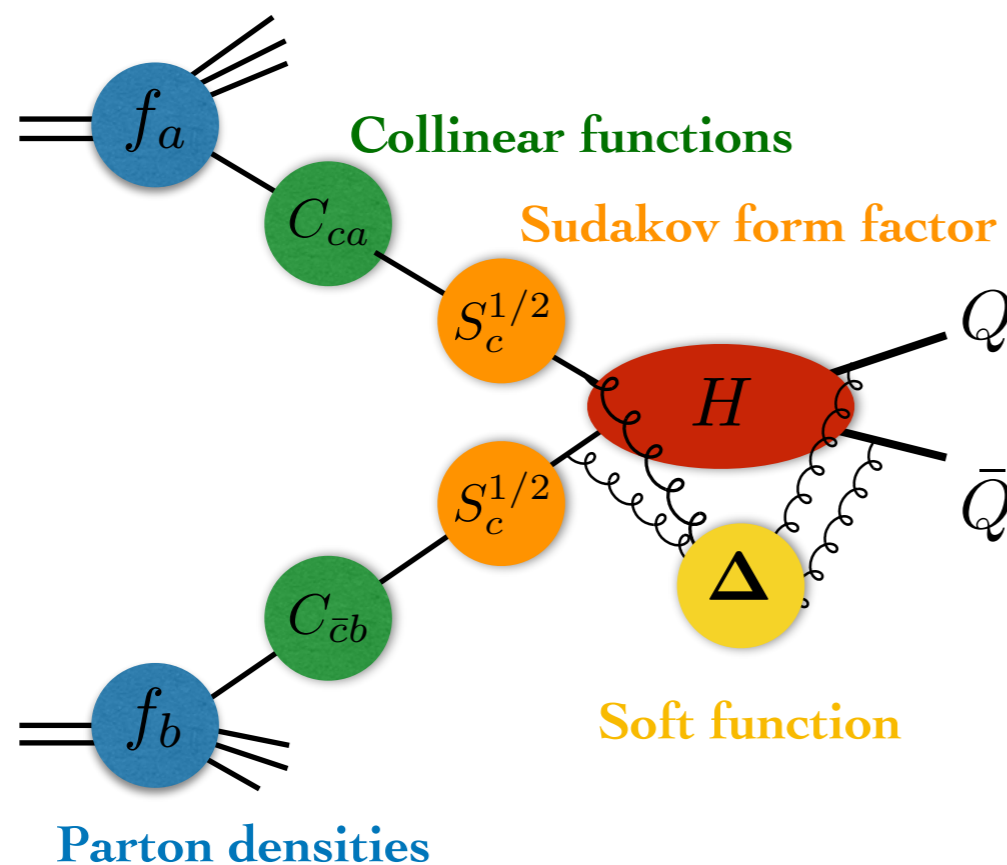
# NNLOPS

Event generators keeping formal NNLO accuracy for inclusive observables

Recently achieved for  $t\bar{t}$  with the MiNNLOPS method

Mazzitelli et al (2020,2021)

Exploit available knowledge of transverse-momentum resummation



Catani, Torre, MG (2014)

Catani, Devoto, Mazzitelli, MG (2023)

NNLO matching for colourless production well established

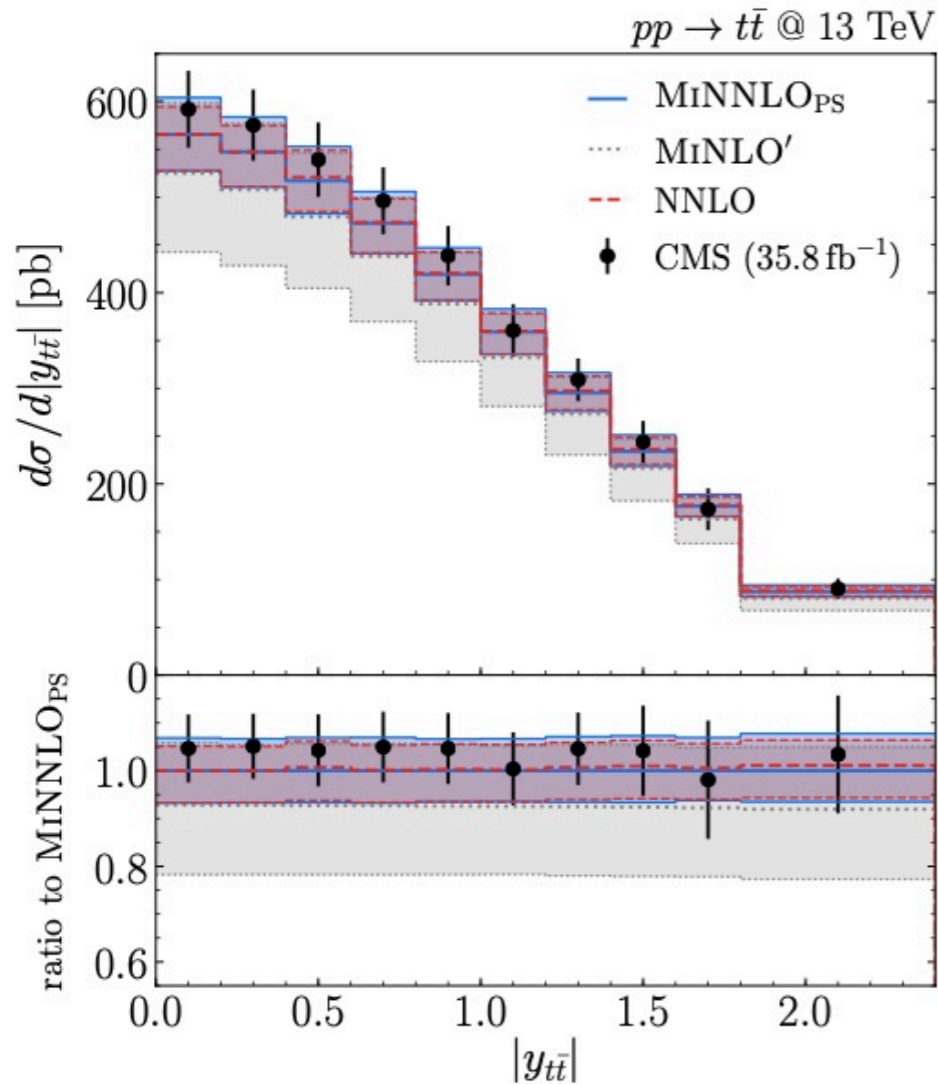
See talk by Silvia Zanolini

$t\bar{t}$  production first example of coloured final state with non trivial soft-radiation pattern

Allows to directly deploy NNLO precision into  $t\bar{t}$  experimental analyses

# NNLOPS

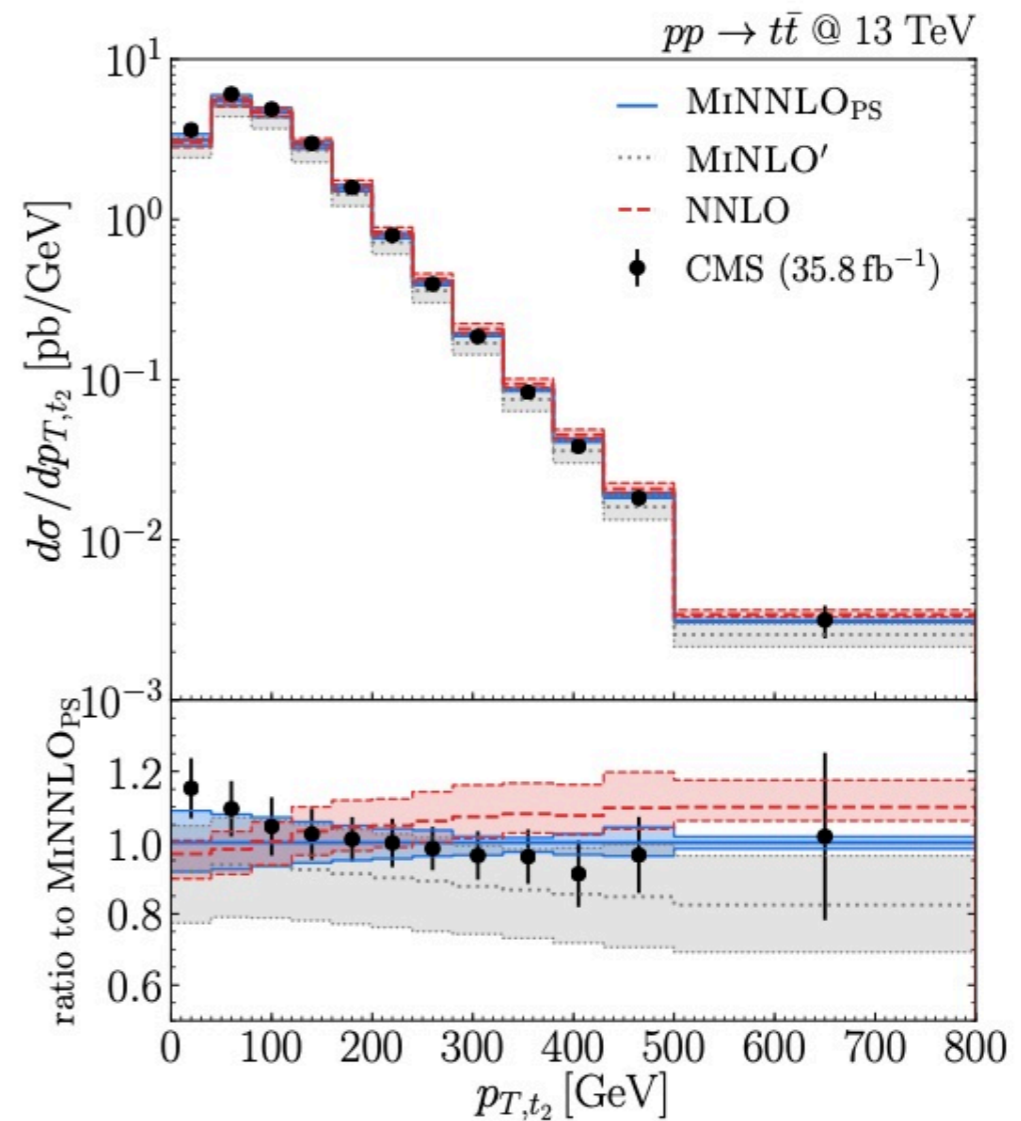
Mazzitelli et al (2020,2021)



Improves where fixed order NNLO has problems (like  $p_T$  of softer top quark)

Excellent agreement with NNLO prediction, with differences only at the permille level

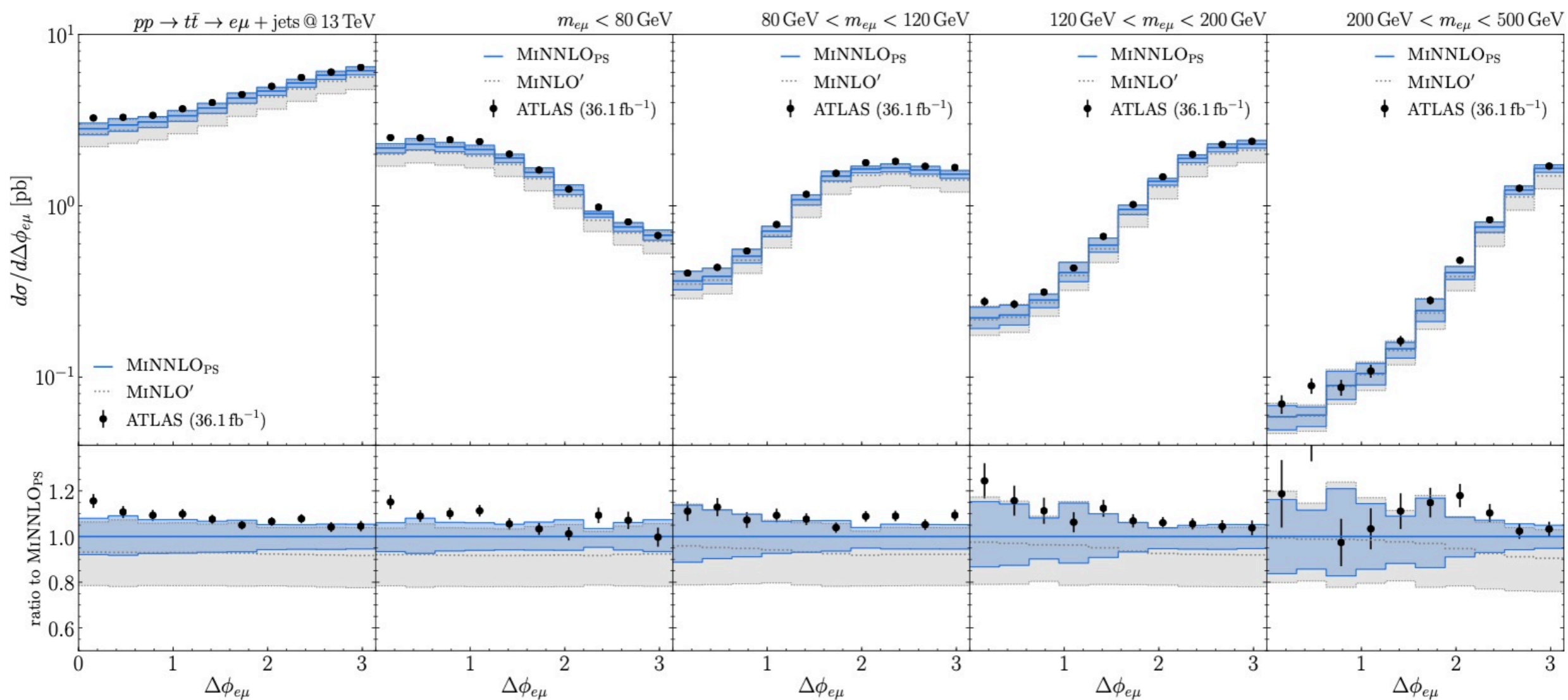
Excellent description of the data



# NNLOPS

Mazzitelli et al (2020,2021)

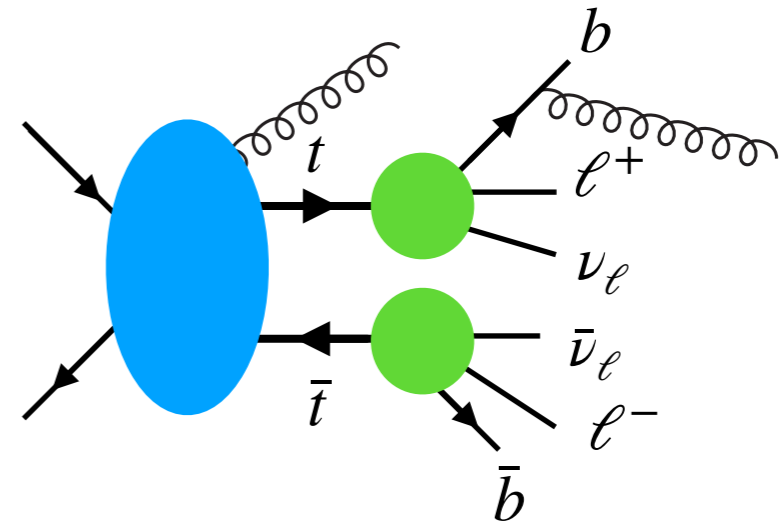
Top decay and spin correlations included at LO only



Still good description of the data

# Top decay

- Narrow width approximation (NWA)
  - based on the limit  $\Gamma_t/m_t \rightarrow 0$
  - considerable simplifications from the factorisation of production and decay
  - treatment of spin-correlations possible



Melnikov, Schulze (2009)

- Off-shell calculations
  - consider the complete process, say  $pp \rightarrow b\bar{b}l\nu l\nu + X$
  - challenges come from high-multiplicity phase space and interferences between production and decay

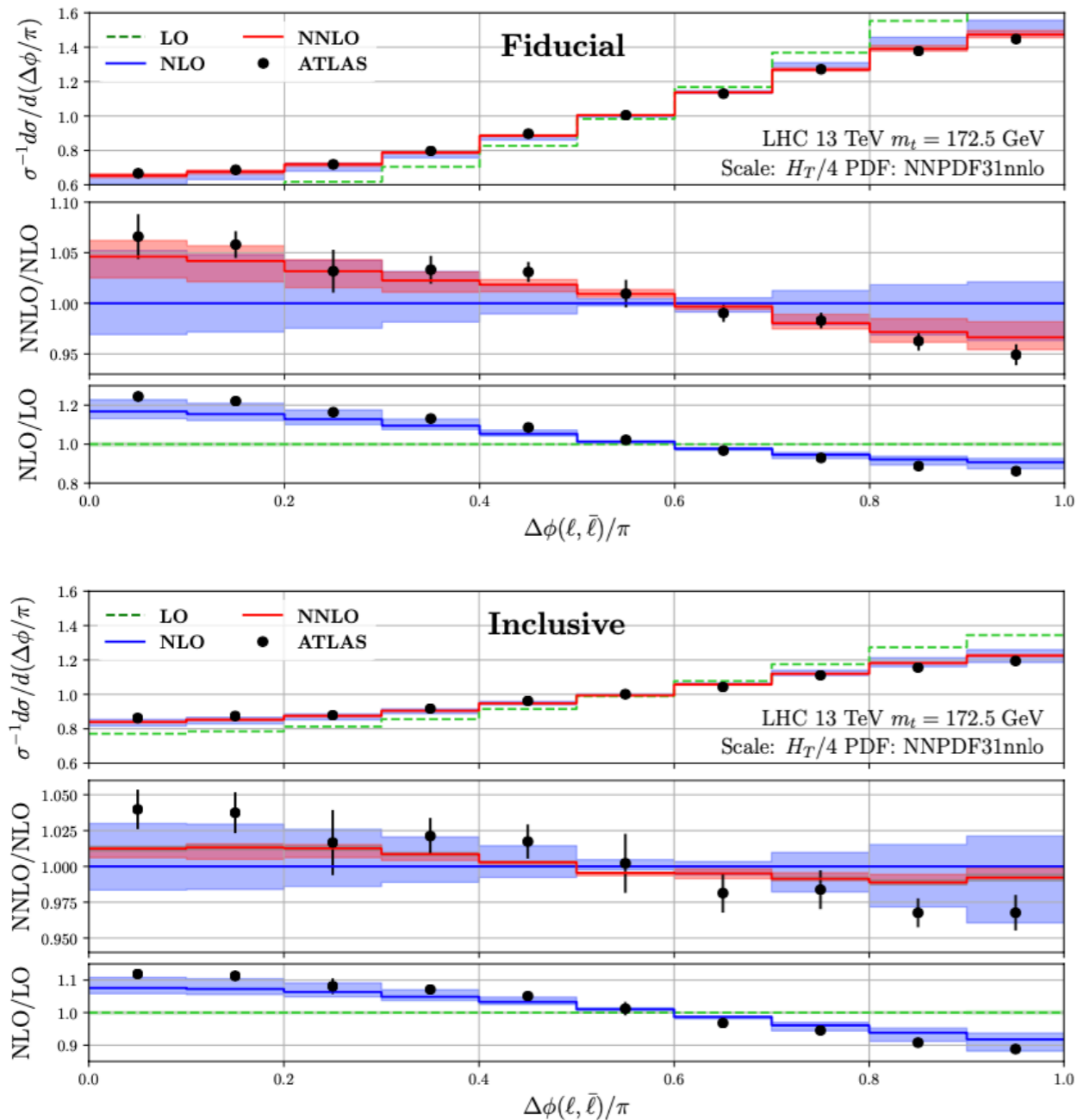
More on on-shell effects in the talk  
by Giovanni Pelliccioli



# Full NNLO in NWA

NNLO production and NNLO decay combined in NWA

Czakon et al (2019,2020)

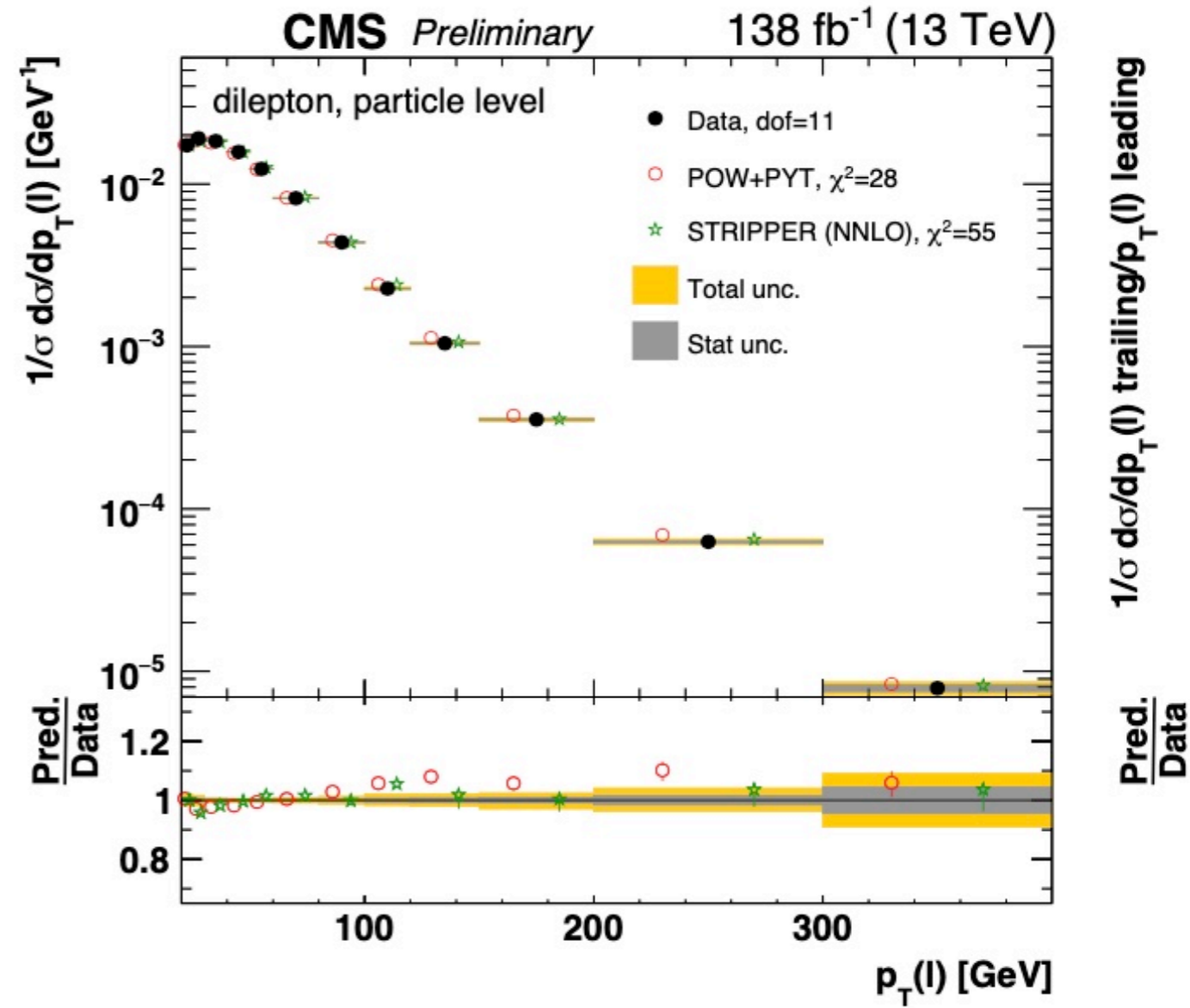
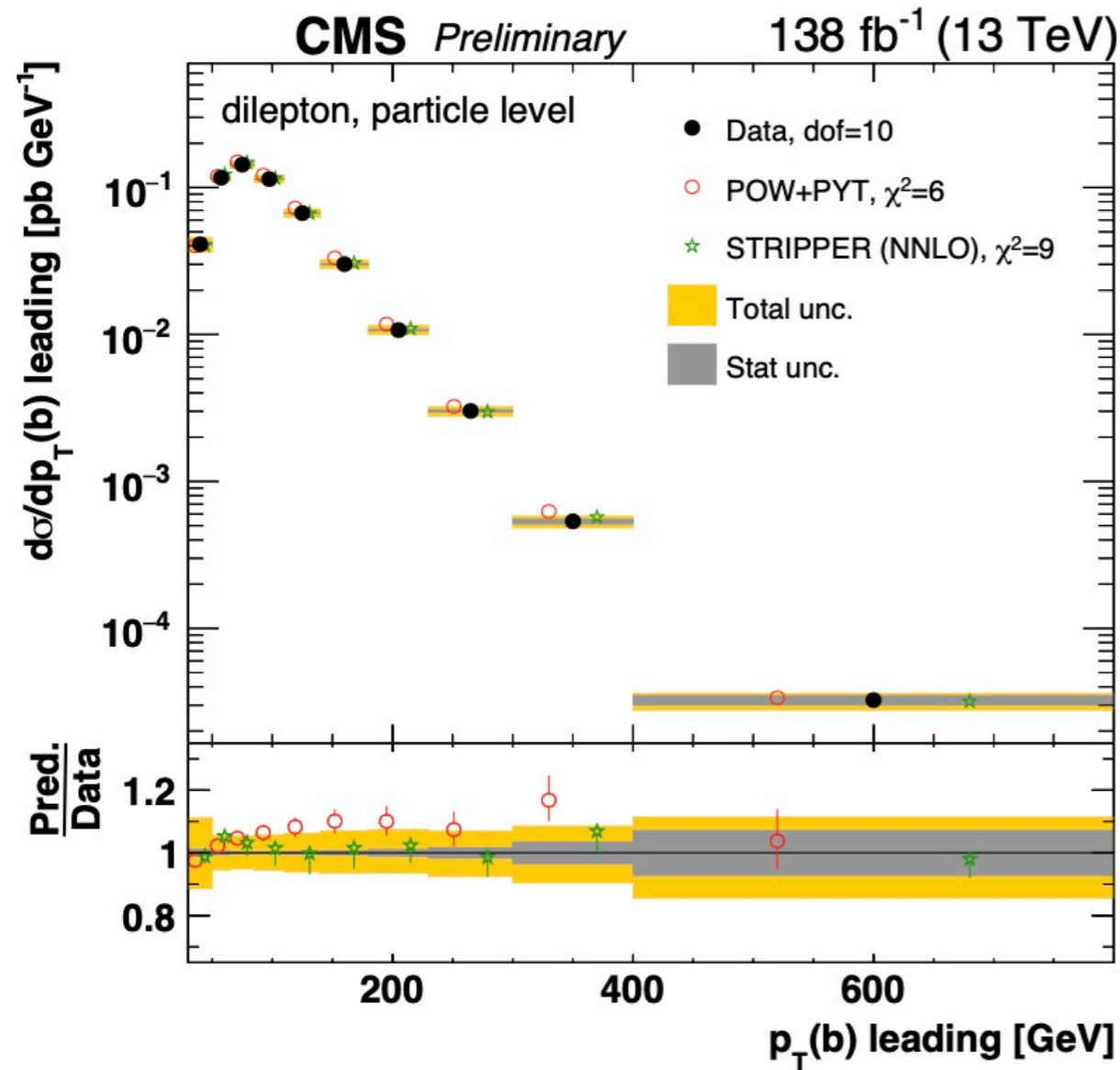


NNLO predictions describe the  $\Delta\phi(\ell\bar{\ell})$  well in the fiducial region while some tension exists when the comparison is done in the inclusive phase space



Effect of extrapolation relevant at this level of precision

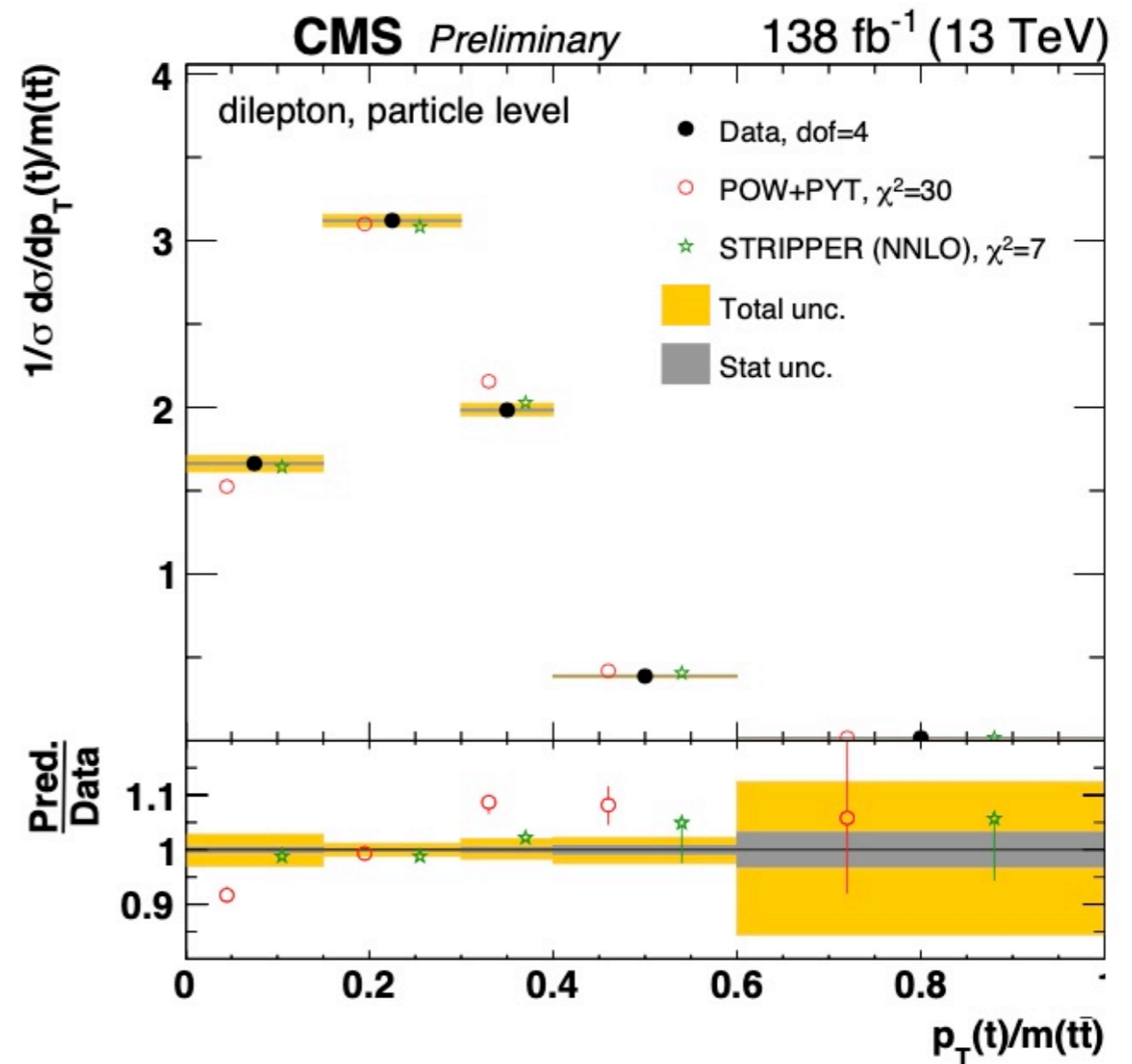
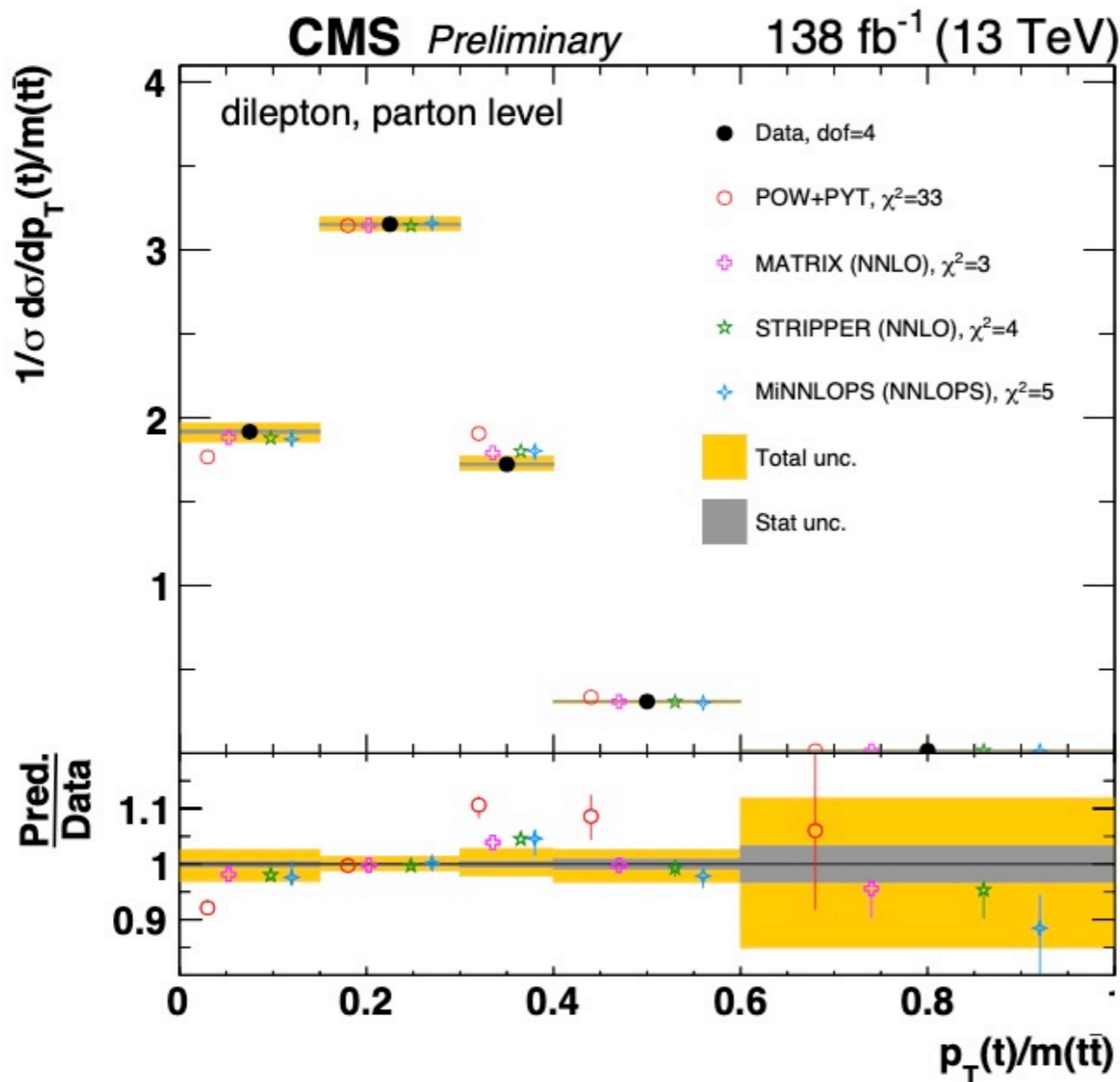
# Full NNLO in NWA



Excellent description of the data both in shape and normalisation

# Full NNLO in NWA

Reconstructed top  $p_T$  normalised to  $m_{t\bar{t}}$ : extrapolated vs fiducial



# Full NLO QCD and EW calculations

- Off-shell effects through complete process  $pp \rightarrow b\bar{b}l\nu l\nu + X$  in NLO QCD

Bevilacqua, Czakon, van Hameren,  
Papadopoulos, Worek (2010)

Denner, Dittmaier, Kallweit, Pozzorini (2012)

Heinrich et al (2013)

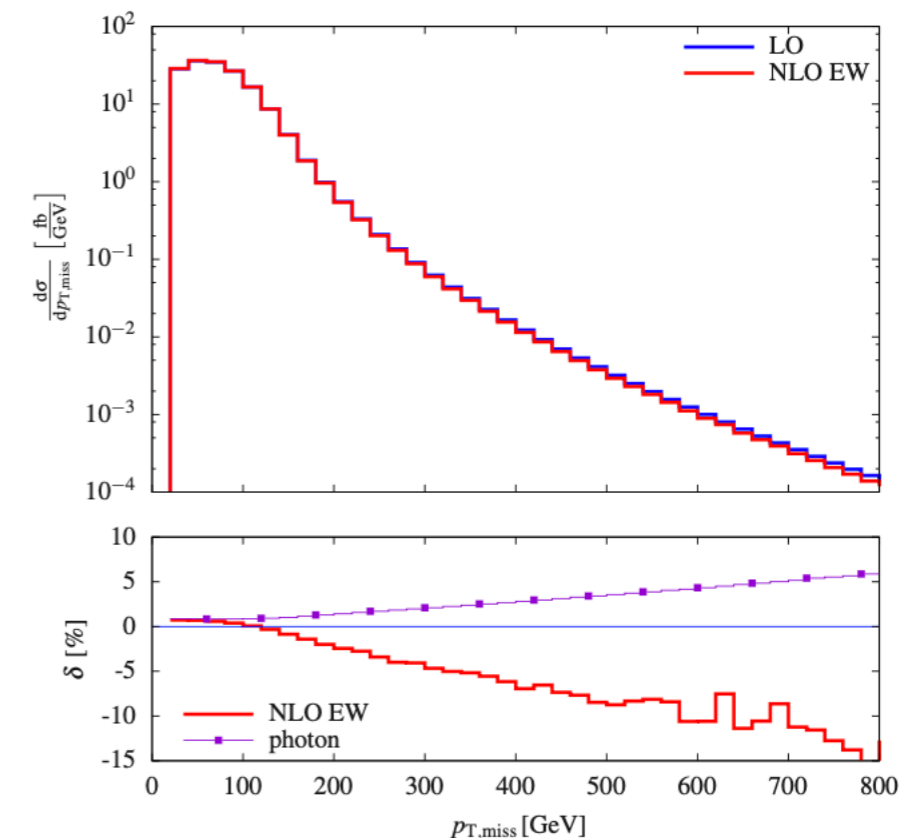
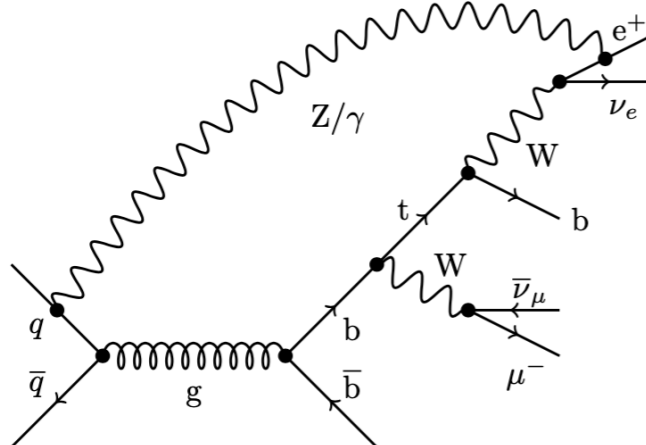
- Unified  $t\bar{t}$  and  $Wt$  with massive b-quarks

Cascioli, Kallweit, Maierhöfer, Pozzorini (2013)

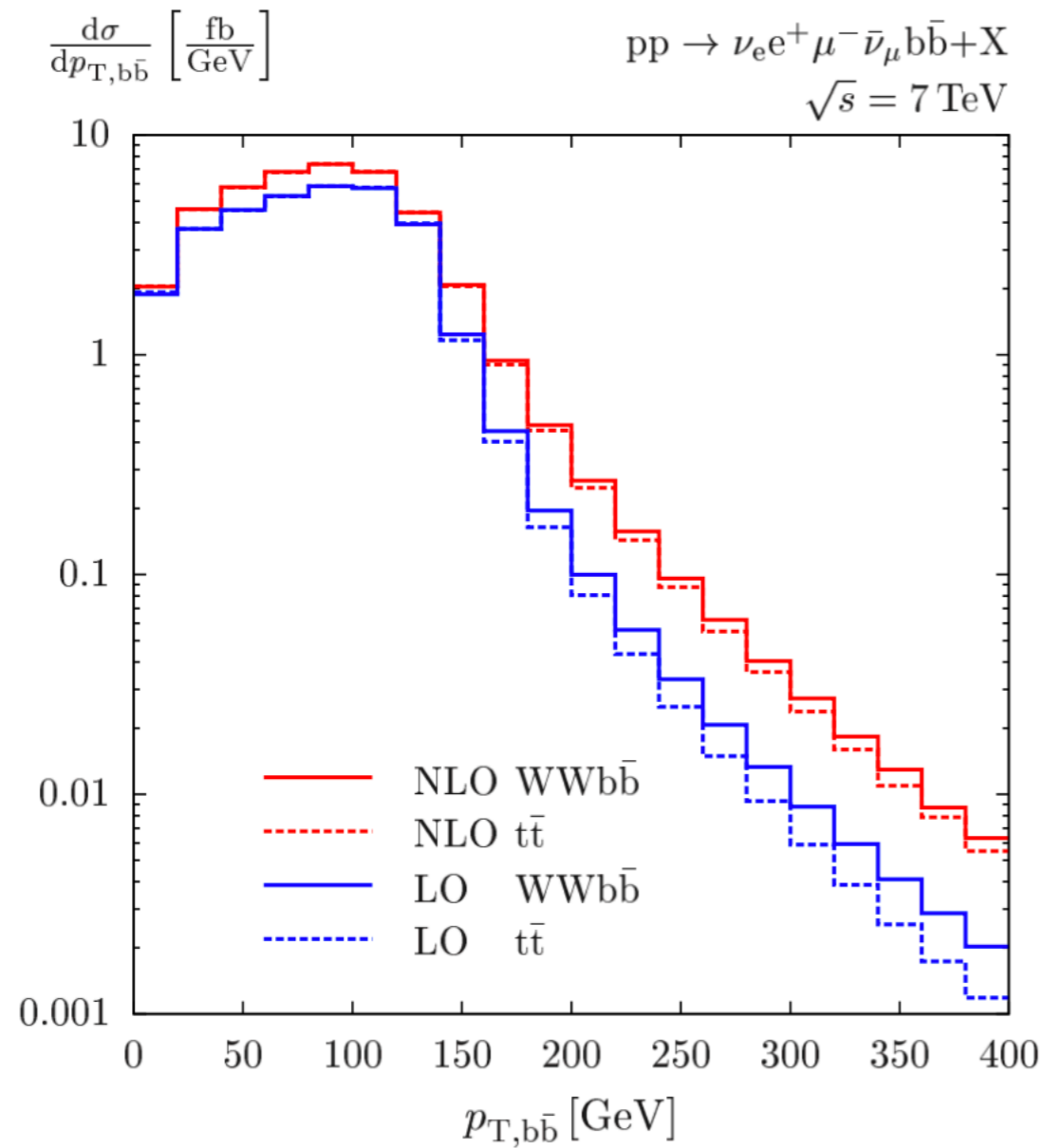
Frederix (2013)

- NLO EW corrections to full  $b\bar{b}l\nu l\nu$

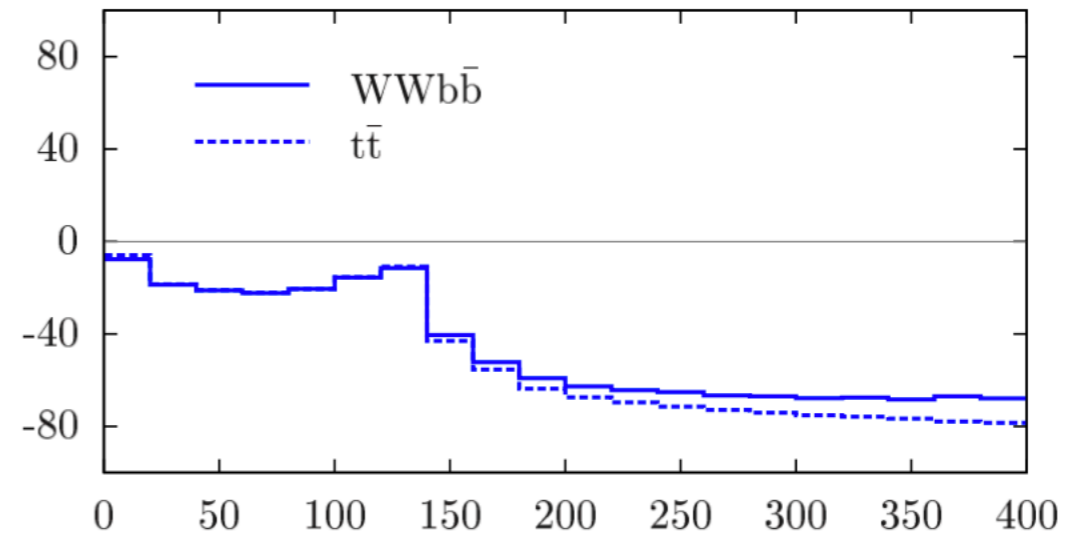
Denner and Pellen (2016)



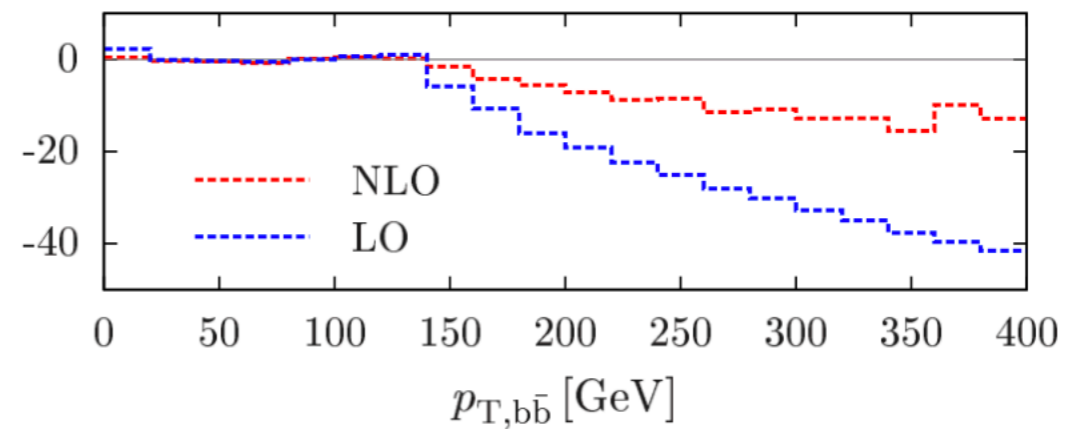
# Finite-width effects



LO/NLO - 1 [%]



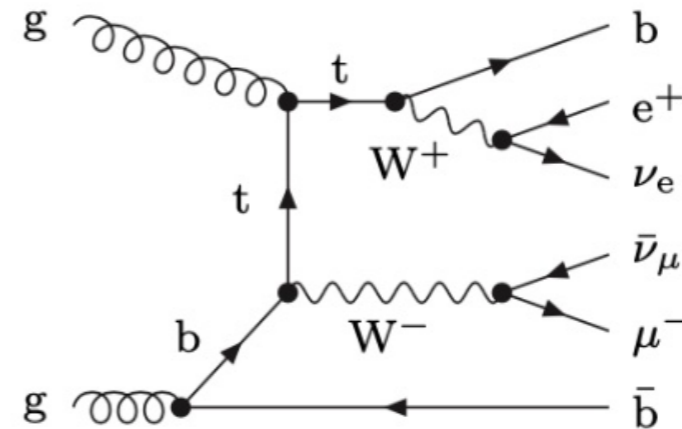
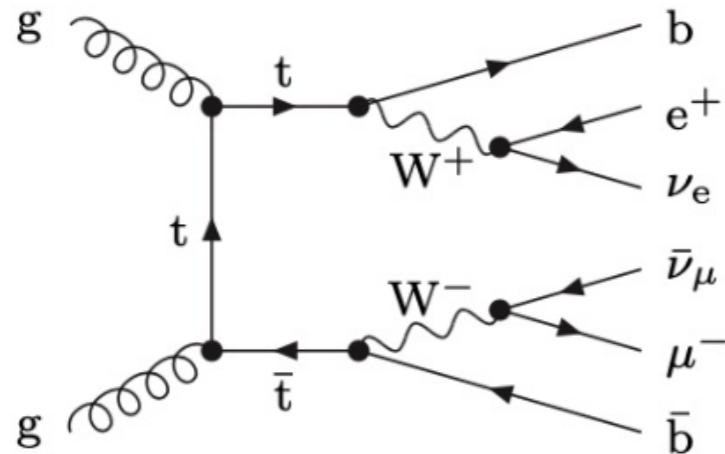
$t\bar{t}/WWb\bar{b} - 1$  [%]



Pozzorini et al. (2012)

Finite-width effects of the top quark are typically small but more important than those of the  $W$

# Isolating $Wt$



NLO  $Wt$  simulations typically based on either

Frixione et al (2008)

- Diagram Removal (DR): removing doubly resonant diagrams
- Diagram Subtraction (DS): cancelling doubly resonant contributions in a gauge invariant way

These methods are a significant source of uncertainty for many BSM searches

# Unified tt and Wt description

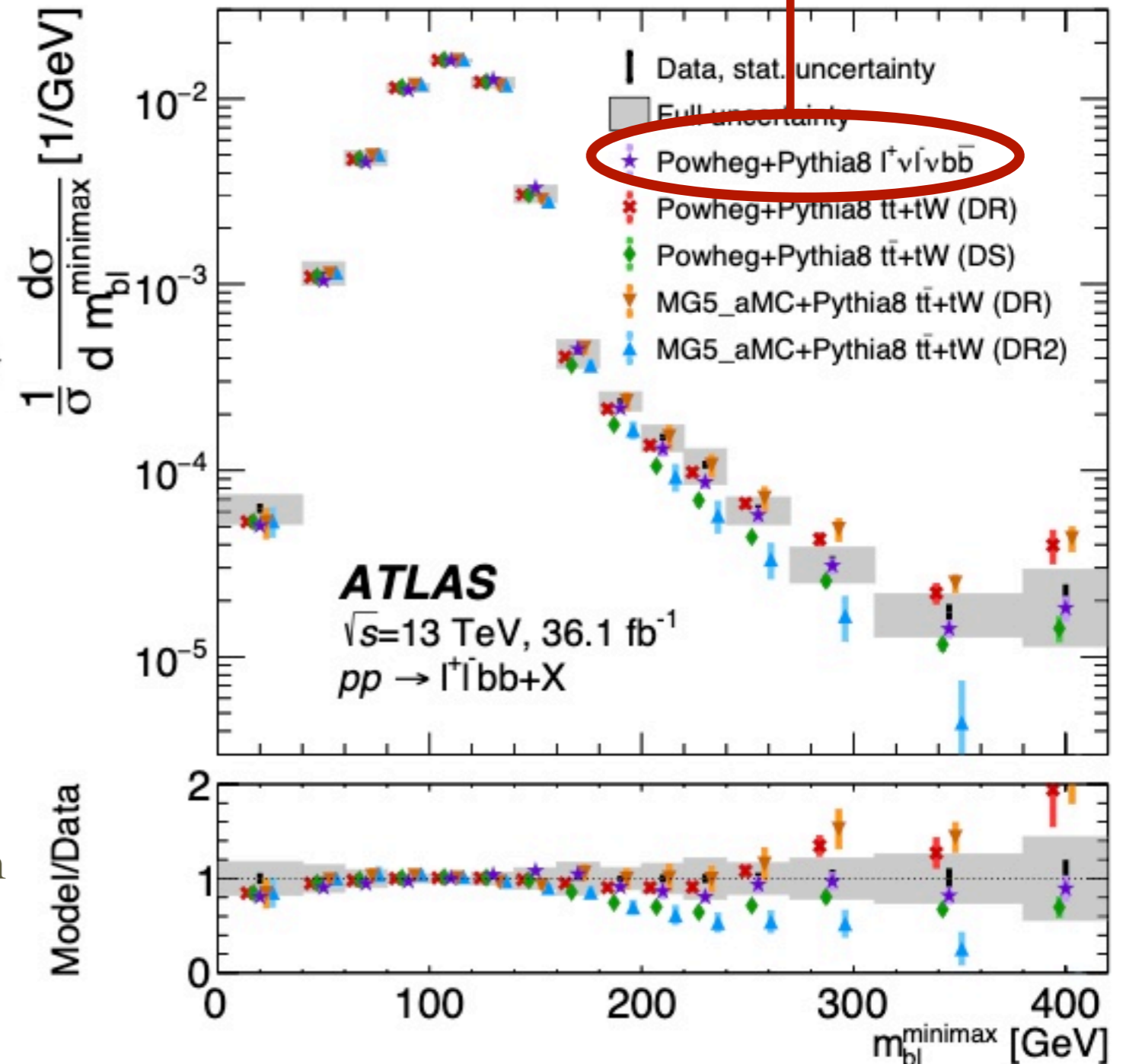
Full tt+Wt prediction Jezo, Lindert, Nason, Oleari, Pozzorini (2016)

Experimental studies have shown the limitations of simulations based on subtraction of Wt contribution

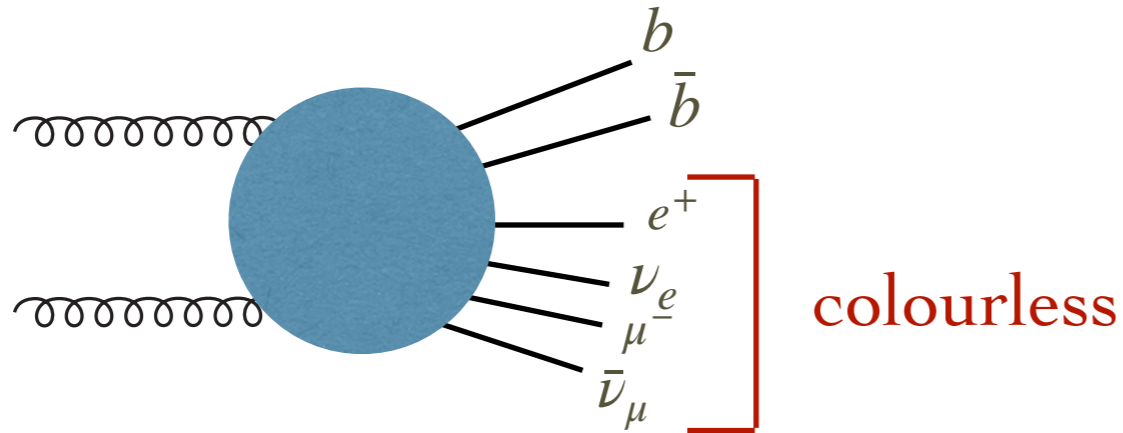
$$m_{bl}^{\text{minimax}} \equiv \min\{\max(m_{b_1\ell_1}, m_{b_2\ell_2}), \max(m_{b_1\ell_2}, m_{b_2\ell_1})\}$$

Low  $m_{bl}^{\text{minimax}}$  region dominated by doubly resonant topologies

High  $m_{bl}^{\text{minimax}}$  region properly modelled by full tt+Wt simulation

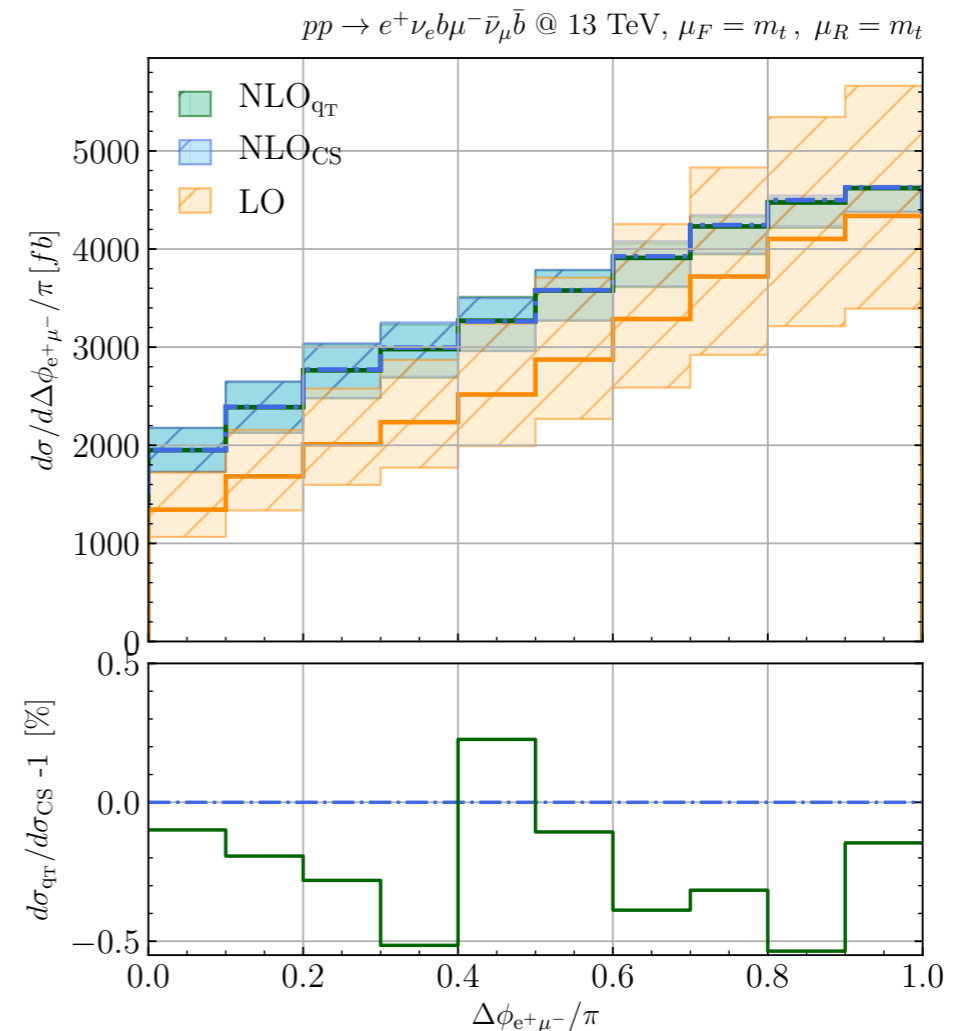
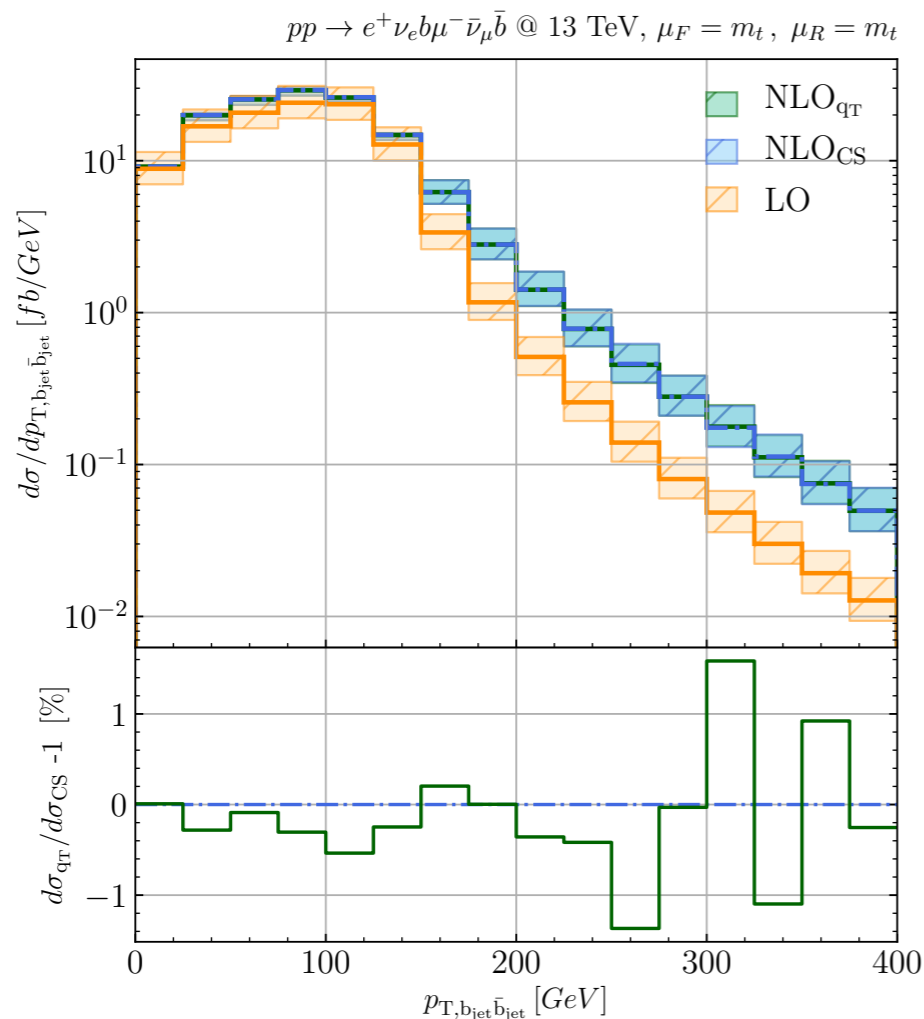


# NNLO ?



Required two-loop amplitudes are beyond current possibilities

→ Appropriate approximations needed



Fully validated at NLO

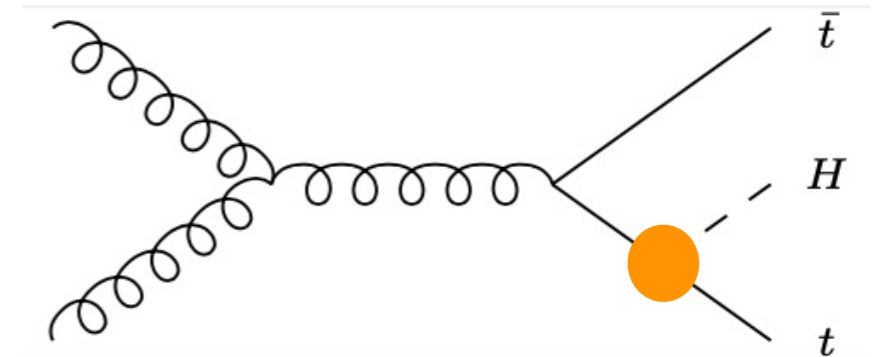
work in progress with Buonocore, Lindert, Devoto, Mazzitelli, Kallweit, Savoini



# $t\bar{t}H$

The associated production of the Higgs boson with a top-quark pair is a crucial process at the LHC

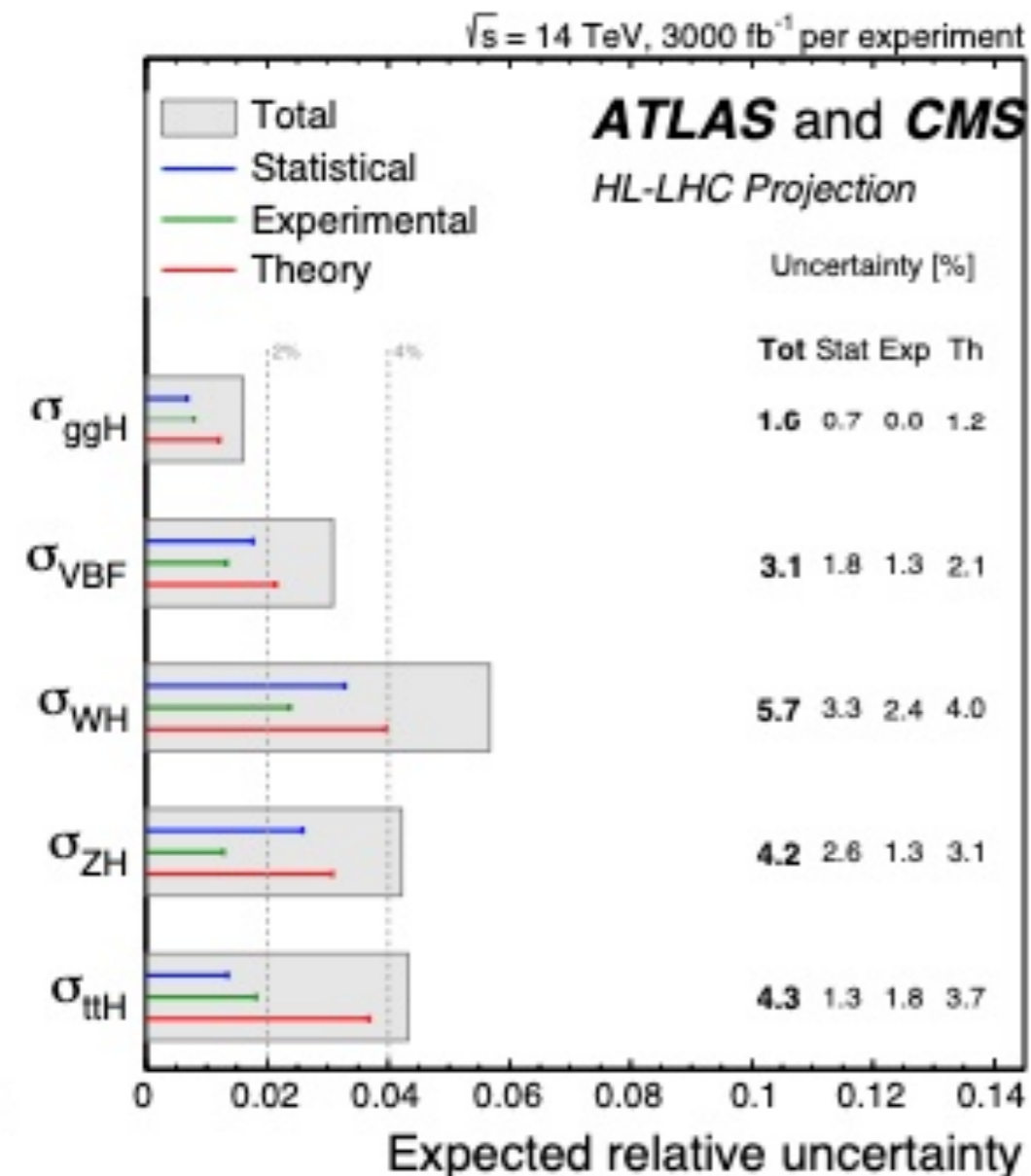
It allows a direct extraction of the top Yukawa



Experimental uncertainties are now at the  $\mathcal{O}(20\%)$  level but expected to go down to the 2% level at the end of the HL-LHC

Current predictions based on NLO QCD+EW (+ resummations) affected by  $\mathcal{O}(10\%)$  uncertainty

Missing ingredients for NNLO are the **two-loop**  $gg \rightarrow t\bar{t}H$  and  $q\bar{q} \rightarrow t\bar{t}H$  amplitudes



# ttH

**The idea:** use an approximation for the missing two-loop amplitude (similar in spirit to recent  $2 \rightarrow 3$  NNLO calculations where leading colour approximation for the 2-loop is used)

See talk by Javier Mazzitelli

$$\mathcal{M}(\{p_i\}, k) \simeq F(\alpha_S(\mu_R); m/\mu_R) J(k) \mathcal{M}(\{p_i\})$$

Soft limit of the scalar heavy-quark form factor

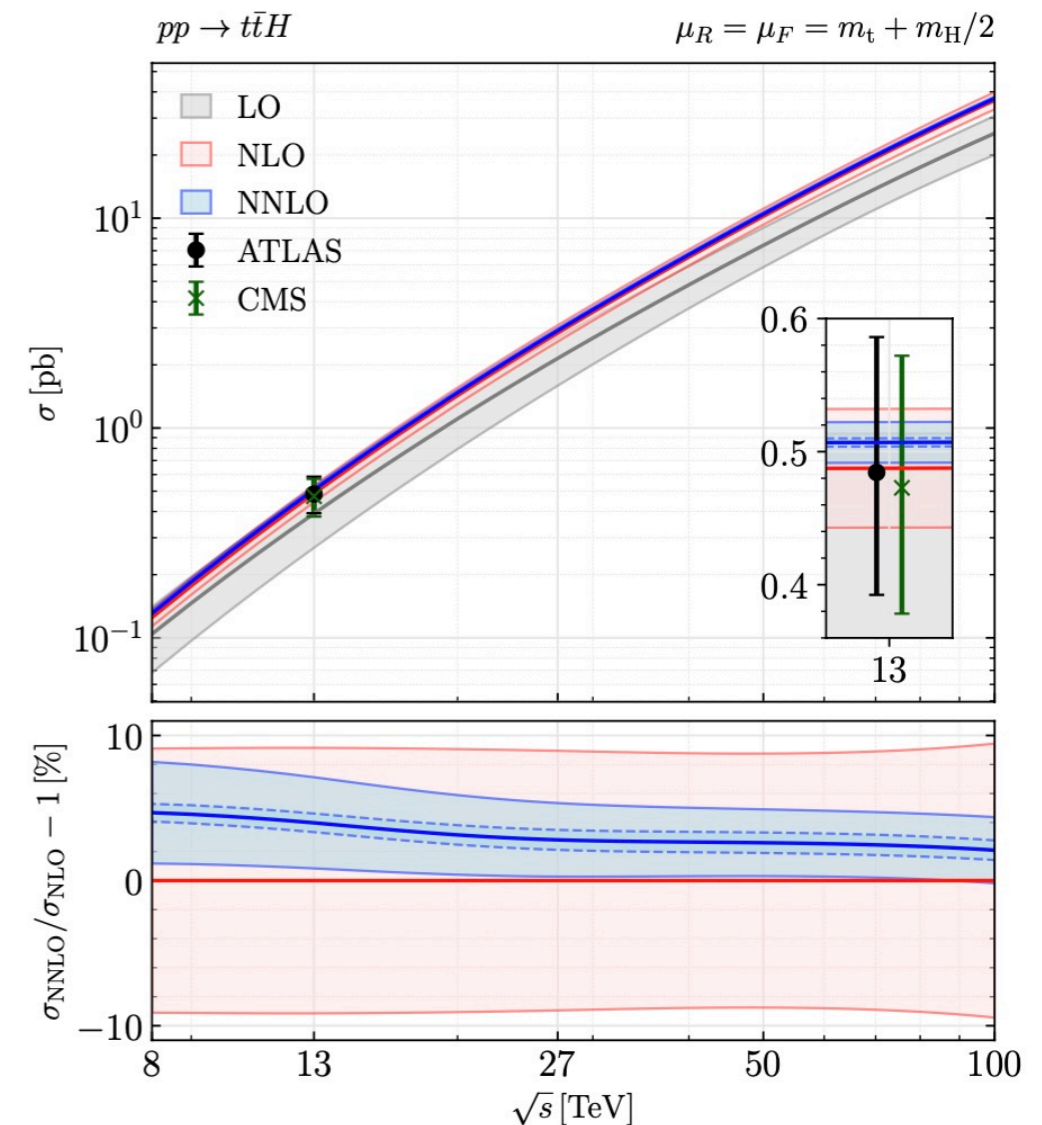
Approximated term has very small impact

$\sigma$ [pb]	$\sqrt{s} = 13$ TeV	$\sqrt{s} = 100$ TeV
$\sigma_{\text{LO}}$	$0.3910^{+31.3\%}_{-22.2\%}$	$25.38^{+21.1\%}_{-16.0\%}$
$\sigma_{\text{NLO}}$	$0.4875^{+5.6\%}_{-9.1\%}$	$36.43^{+9.4\%}_{-8.7\%}$
$\sigma_{\text{NNLO}}$	$0.5070(31)^{+0.9\%}_{-3.0\%}$	$37.20(25)^{+0.1\%}_{-2.2\%}$

NNLO effect is about **+4%** at 13 TeV and **+2%** at 100 TeV

Catani, Devoto, Mazzitelli, Kallweit, Savoini, MG (2022)

Bernreuther et al (2005); Blümlein et al (2017)  
Fael, Lange, Schönwald, Steinhauser (2022)



# Summary

- Top quarks are ubiquitous at the LHC
- Precise control of top production is fundamental to tame backgrounds in most of BSM searches and to fully exploit the LHC potential
- Theoretical predictions in good shape with NNLO+NLO EW becoming the standard
- NNLO precision starts to be deployed in MC generators
- Further progress is expected/needed to include off-shell effects beyond NLO
- First NNLO results for  $t\bar{t}H$