



# Higher-order and off-shell effects in top-quark processes at high-energy colliders

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# Introduction

Improving the **perturbative description** of full off-shell top-quark processes at colliders is a mandatory step for realistic predictions, though not the only one (parton-shower matching, hadronisation, ...).

Computing **NLO QCD** and **EW** corrections is **not straightforward**:

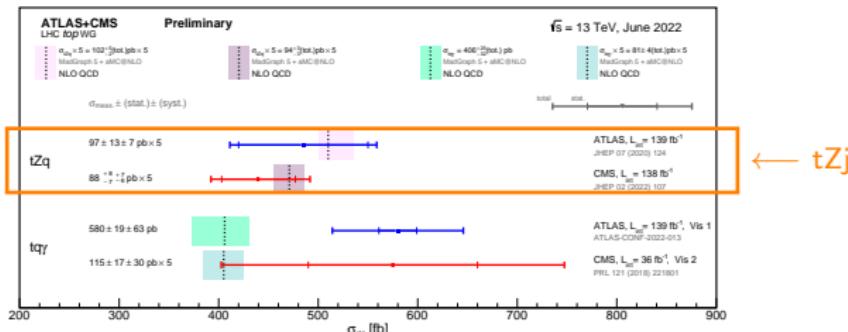
1. **high-multiplicity** final states,
2. **complicated resonant** structures,
3. **non-resonant effects** and **spin-correlations** must be included,
4. **mixing** of **EW** and **QCD** corrections at a given order.

In this talk I introduce such complications using as illustrative processes:

- **tZj at the LHC**
- **tt** at lepton colliders

# Off-shell effects at the LHC: the tZj process

A rare process at the LHC: weak boson Z in association with a single (anti)top quark  
→ electroweak induced



Run-2: observed [CMS 1812.05900, ATLAS 2002.07546], differential meas. [CMS 2111.02860].

Gives access to top-quark-to-Z-boson (more directly than  $t\bar{t}Z$ ), triple-gauge (WWZ) and Wtb couplings to constrain new physics [Li et al. 1103.5122, Kidonakis 1712.01144, Degrande et al. 1804.07773, Liu Moretti 2010.05148].

EW-induced process: top quark is polarised [Mahlon Parke 9912458].

## tZj: SM predictions

NLO QCD: narrow-width approximation (NWA) [Campbell Ellis Röntsch 1302.3856].

NLO QCD+EW: on-shell top , off-shell Z [Pagani Tsinikos Vryonidou 2006.10086].

PS matching: NLO QCD + QCD shower, LO decays [Pagani Tsinikos Vryonidou 2006.10086]

NLO, full off-shell: NLO EW + QCD [Denner GP Schwan 2207.11264] in the  $3\ell$  channel.

Soft-gluon resummation: exact NLO + soft-gluon corr. [Kidonakis Yamanaka 2210.09542].

Broad SMEFT interpretation also available [Degrande et al. 1804.07773]

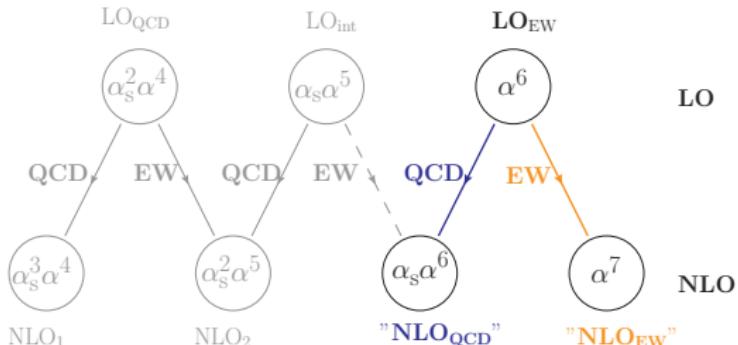
# tZ: LO contributions

$p p \rightarrow e^+ e^- \mu^+ \nu_\mu j_b J + X$

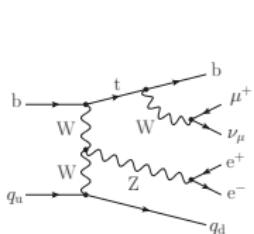
$j_b = b\text{-tagged jet}$

$J = \text{any jet}$

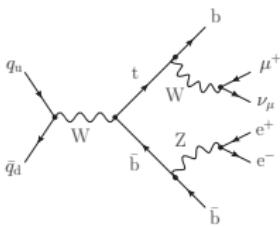
in the 5-flavour scheme



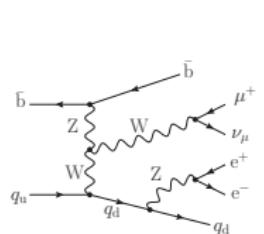
**LO:**  $\text{LO}_{\text{QCD}}$  non-resonant,  $\text{LO}_{\text{int}}$  vanishes (CKM unit matrix), single-top in  $\text{LO}_{\text{EW}}$ .  
Channels with initial states  $q\bar{q}$ ,  $qb$



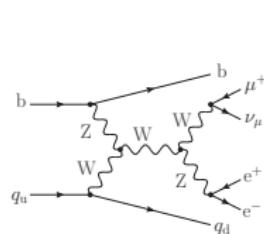
**t-channel resonant**



**s-channel resonant**



**non-resonant**

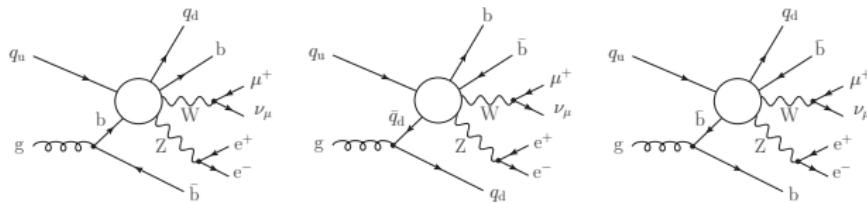


**VBS-like**

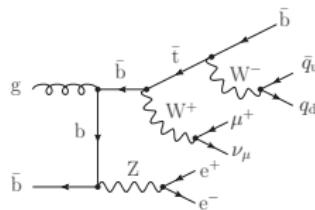
# tZj: NLO contributions

**NLO QCD and EW:** genuine corrections to LO EW (no interference).  
Real channels with initial states  $q\bar{q}$ ,  $qb$ ,  $gq$ ,  $\gamma q$ ,  $gb$ ,  $\gamma b$ .

Not possible to distinguish between ***t*-channel** and ***s*-channel** contributions at NLO:



Fiducial-volume for **top quark** contaminated by **hadronically decaying antitop** ( $\gamma \bar{b}$ ,  $gb$ ):



The same holds for the charged-conjugated process: **very large** correction ( $\approx +10\%$ ).  
**Irreducible bkg** that can only be treated with jet vetoes/ special cuts.

# tZj: integrated cross-sections and off-shell effects

Fiducial cross-sections [Denner GP Schwan 2207.11264] in the setup of [ATLAS 2002.07546].

- ▶ Sizeable QCD and EW corrections.
- ▶ QCD-scale (downward) uncertainty diminished from LO to NLO QCD.

order	$\sigma$ [fb]	ratio [/LO]
LO [ $\mathcal{O}(\alpha^6)$ ]	0.6416(0) $^{+8.9\%}_{-13.5\%}$	100.0%
$\delta_{\text{QCD}}$ [ $\mathcal{O}(\alpha_s \alpha^6)$ ]	0.1987(5)	31.0%
$\delta_{\text{EW}}$ [ $\mathcal{O}(\alpha^7)$ ]	-0.0416(6)	-6.5%
NLO QCD	0.8402(5) $^{+8.6\%}_{-3.9\%}$	131.0%
NLO EW	0.5999(6) $^{+9.4\%}_{-13.9\%}$	93.5%
NLO QCD+EW	0.7986(8) $^{+9.4\%}_{-4.2\%}$	124.5%

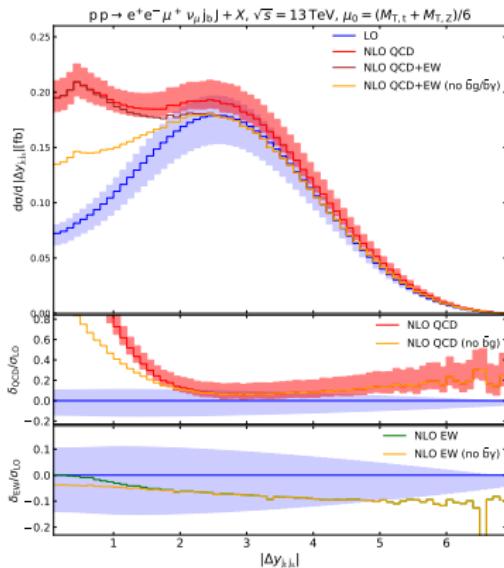
Off-shell [Denner GP Schwan 2207.11264] vs on-shell [Pagani et al. 2006.10086] in Z-peak setup: same EW correction (relative to NLO QCD), differences at NLO QCD.

	on-shell	off-shell* (w/o decay corr.)	off-shell*
NLO QCD/LO	1.24	1.289	1.195
(NLO QCD+EW)/NLO QCD	0.93	0.919	0.924

\* excluded  $\bar{b}\gamma$ ,  $\bar{b}g$  channels

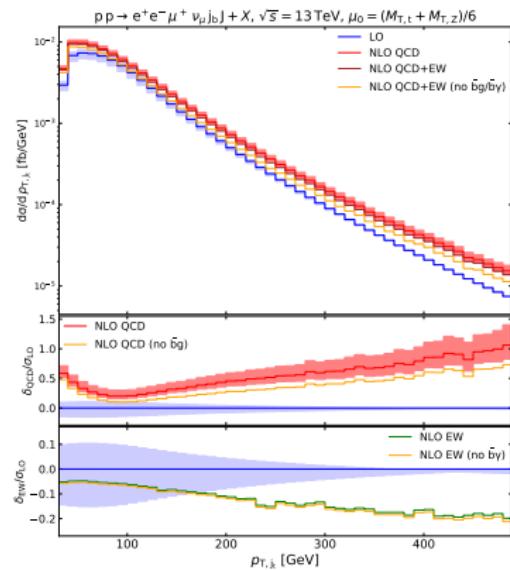
# tZ: differential results

Rapidity separation between top-decay jet and spectator jet,  $|\Delta y_{j_{\text{t}} j_{\text{s}}}|$ .



- ▶ Dominant tZ topology gives peak at  $|\Delta y_{j_{\text{t}} j_{\text{s}}}| \approx 2.5$ .
- ▶ Large hadronic-antitop contribution at small values ( $\approx 100\%$  of LO for  $|\Delta y_{j_{\text{t}} j_{\text{s}}}| < 1$ )

Transverse momentum of the top-decay jet,  $p_{T,j_{\text{t}}}$ .

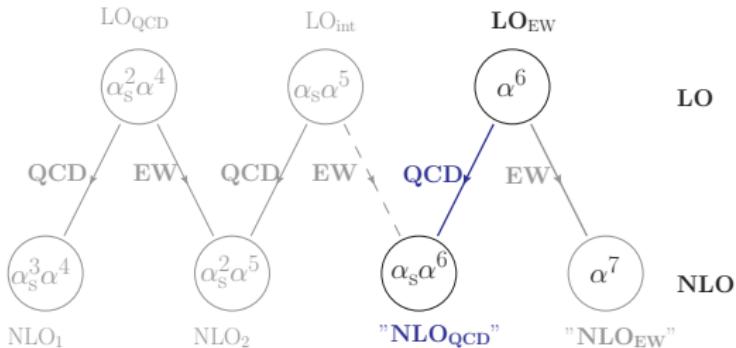


- ▶ Increasing positive QCD corrections (up to 100%), at variance with spectator jet ( $\rightarrow 0$ , at large  $p_T$ ).
- ▶ EW-Sudakov enhancements in the tails (negative EW corr., up to -20%)

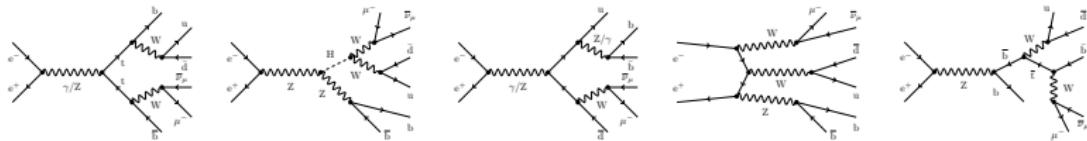
# Off-shell effects at lepton colliders: $t\bar{t}$

$t\bar{t}$  production at **lepton colliders** is **EW induced**: cleaner environment (than LHC), similar issues arise with off-shell effects, especially in **semi-leptonic decay channel**.

$e^+e^- \rightarrow j_b j_b jj \mu^+\nu_\mu$   
at **NLO** accuracy:  
(mostly) annihilation process



Full off-shell description: resonant ( $t\bar{t}$ ) and non-resonant (single-top, triboson ...)



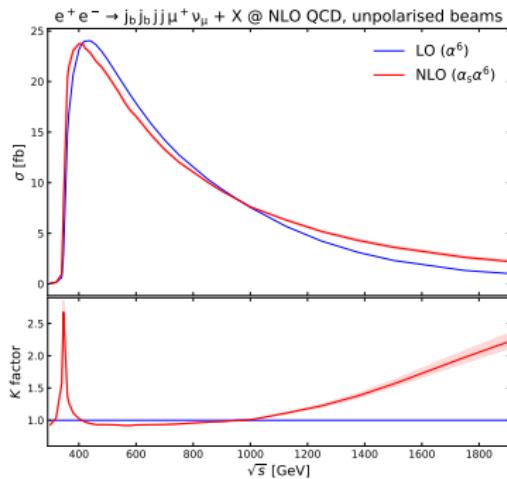
# $t\bar{t}$ at lepton colliders: cross-section scan

Higher-order and non-resonant effects strongly depend on the decay channel, e.g

$e^+e^- \rightarrow j_b j_b jj e^+ \nu_e$ : t-channel contributions (not only annihilation),

$e^+e^- \rightarrow j_b j_b e^+ \nu_e \mu^- \bar{\nu}_\mu$ : different QCD corrections (two jets only),

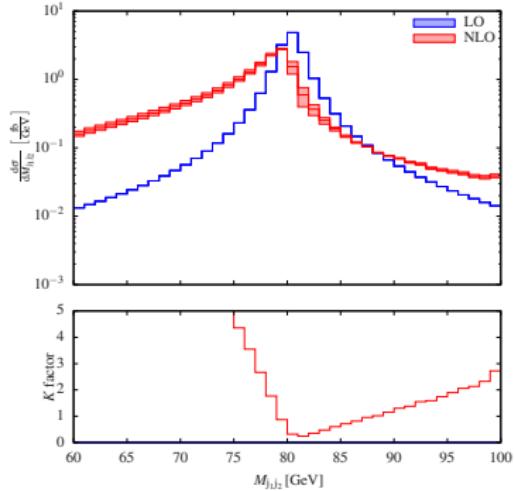
and on the collider energy,



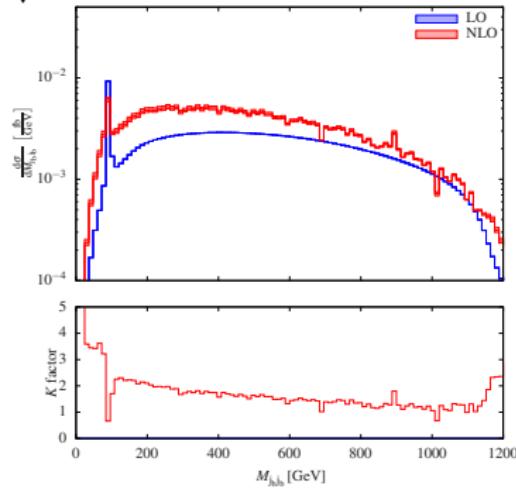
- below and about threshold ( $2 m_{top}$ ) similar QCD corrections as in fully leptonic channel
- positive and increasing QCD effects for  $\sqrt{s} \gtrsim 1$  TeV
- irreducible-bkg larger with increasing  $\sqrt{s}$
- huge QCD corrections at high energy due to event selection (2 light jets with  $R = 0.4$ ) cutting boosted-W topologies at LO

# $t\bar{t}$ at lepton colliders: differential results

Invariant mass of the two-light-jet system,  
 $\sqrt{s} = 365\text{GeV}$



Invariant mass of the two-b-jet system,  
 $\sqrt{s} = 1.5\text{TeV}$



- ▶ strong distortion of  $M_{jj}$  spectrum with huge radiative tail
- ▶ hard-gluon radiation modify also the high-energy tail (larger effects at  $1.5\text{TeV}$ )

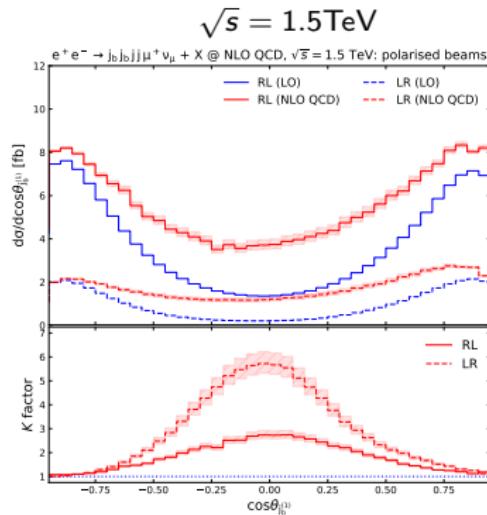
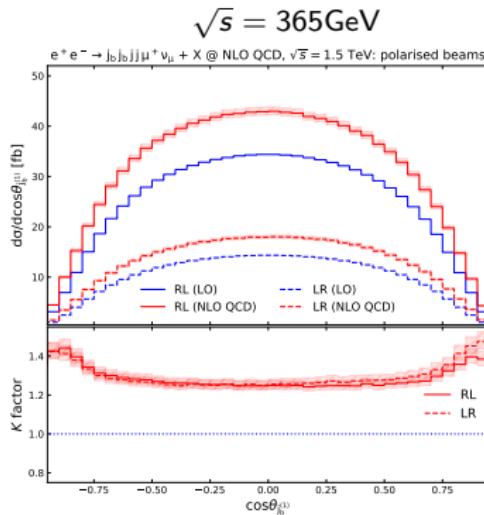
- ▶ peak at the Z mass:  $Z \rightarrow jbjb$  sitting on top of  $t\bar{t}$  and single-top
- ▶ small QCD corr. approaching maximum allowed (on-shell top), larger towards end-point.

# $t\bar{t}$ at lepton colliders: polarised-beam effects

Polarisation of  $e^\pm$  along beam axis: only **LR** and **RL** states allowed (annihilation).

Around threshold QCD effects are independent of polarised-beam effects.

At **high energy** very different  $K$ -factors for LR and RL: real radiation opens up helicity configurations that are suppressed at LO, and to increased irreducible bgks (with different helicity structure).



Cosine of the polar angle of the leading b jet.

# Conclusions

Essential to model full off-shell top-quark processes at least at NLO QCD and EW accuracy, both at LHC and at lepton colliders.

Typically dominated by top-resonant contributions, but non-resonant ones may be sizeable, depending on:

- type of process (QCD or EW induced),
- decay channel (leptonic or hadronic),
- energy regime (at threshold, boosted topologies, . . . ),

and NLO corrections may open up kinematic configurations that are suppressed at LO.

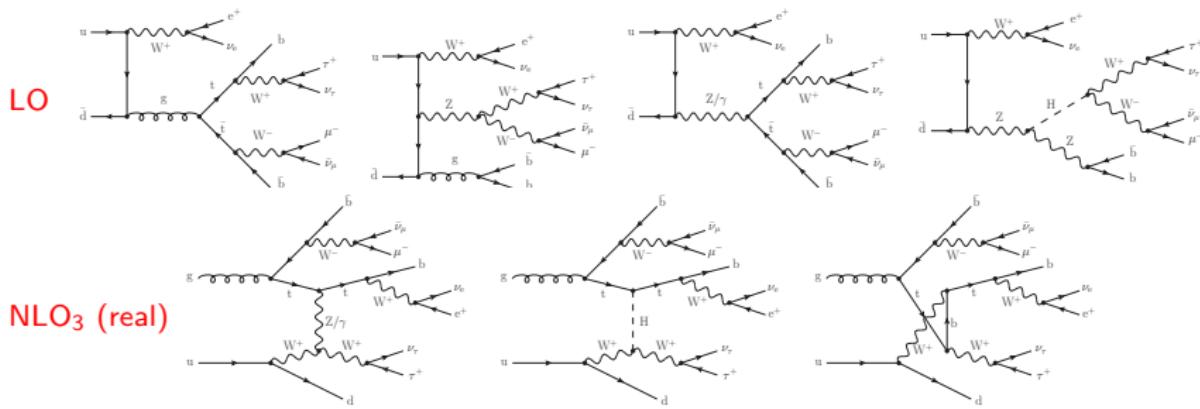
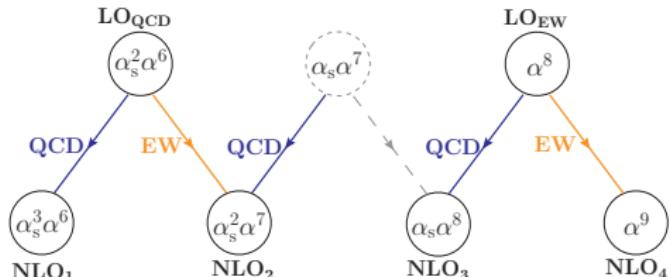
A good practice: compare full off-shell calculations with production  $\times$  decay approximations (narrow width, pole) for a quantitative estimate of off-shell effects.

# Backup ( $t\bar{t}W$ )

# A quick glance at $t\bar{t}W$

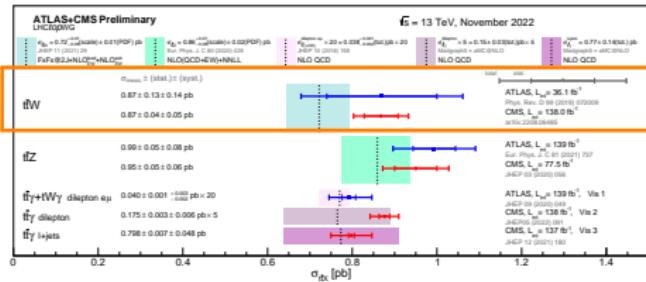
The situation here is even more involved → QCD induced but large EW contributions.

$p p \rightarrow b \bar{b} e^+ \nu_e \mu^- \bar{\nu}_\mu \tau^+ \nu_\tau + X$   
at NLO accuracy  
Several “signal” contributions.



Rare processes at the LHC: weak boson(s)  $V$  in association with

- ★ a top-antitop pair:  $t\bar{t}V \rightarrow$  QCD induced (but large EW contribution)



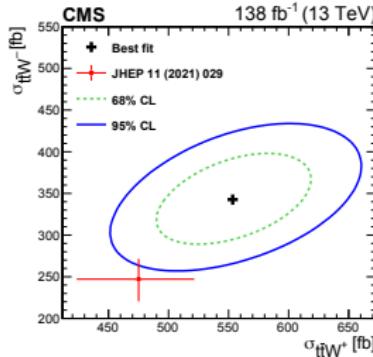
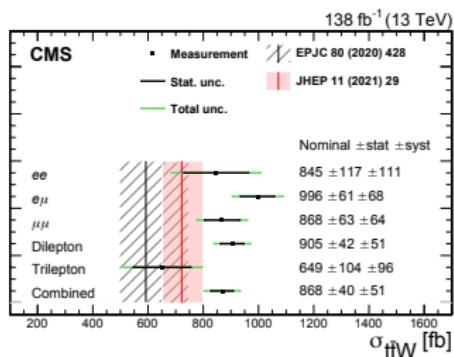
# A tension to be addressed

Hadro-production of  $t\bar{t}W^\pm$  at the LHC gives access to  $t\bar{t}V$  couplings in the SM, new-physics effects [Dror et al. 1511.03674, Bylund et al. 1601.08193] and charge asymmetries [Maltoni et al. 1406.3262]. Important background to  $t\bar{t}h$  [Maltoni et al. 1507.05640].

Measured with Run-2 dataset [ATLAS 1609.01599, 1901.03584, CMS 1711.02547, 2208.06485].

Tension between data and SM for both  $t\bar{t}W$  analyses [CMS 1711.02547, ATLAS 1901.03584] and as background to  $t\bar{t}h$  [CMS 1804.02610, ATLAS 1806.00425].

Latest results [CMS 2208.06485], full Run-2 dataset: improved theory,  $2\sigma$  tension remains.



## Theory status (SM)

**NLO, on-shell/NWA:** NLO QCD [Maltoni et al. 1406.3262], subleading NLO orders [Frixione et al. 1504.03446, Frederix et al. 1711.02116, 1804.10017]. NLO QCD in NWA [Campbell Ellis 1204.5678].

**Soft-gluon resummation:** NLO+NNLL (on-shell) [Broggio et al. 1907.04343, Kulesza et al. 2001.03031].

**NLOPS matching:** NLO QCD to LO QCD [Garzelli et al. 1208.2665] and NLO QCD to LO EW [Frederix Tsinikos 2004.09552, Cordero et al. 2101.11808] in NWA (LO decays).

**Multi-jet merging:** NLO on-shell [von Buddenbrock et al. 2009.00032], in NWA (LO decays) [Frederix Tsinikos 2108.07826].

**NLO, full off-shell:** NLO QCD [Bevilacqua et al. 2005.09427, 2012.01363, Denner GP 2007.12089], subleading NLO orders [Denner GP 2102.03246] in the  $3\ell$  channel.

**Broad comparison** between full off-shell, NWA and PS-matched predictions [Bevilacqua et al. 2109.15181] in the  $3\ell$  channel.

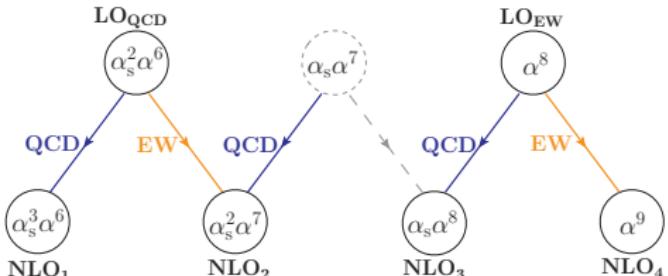
# LO and NLO<sub>1</sub> contributions

LHC process:

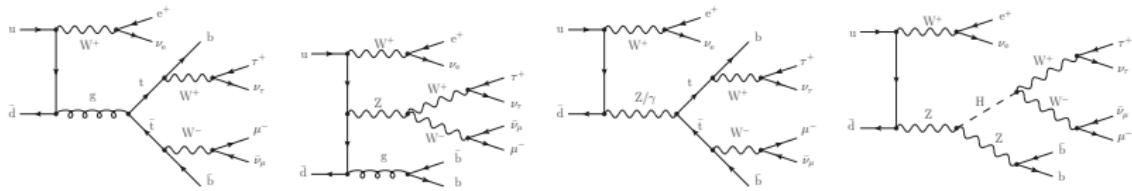
$$pp \rightarrow b\bar{b} e^+ \nu_e \mu^- \bar{\nu}_\mu \tau^+ \nu_\tau + X$$

at NLO accuracy

→ several contributions.



**LO**: double-resonant ( $t\bar{t}$ ), single-resonant ( $t$  or  $\bar{t}$ ), non-resonant diagrams. Interference of order  $\mathcal{O}(\alpha_s \alpha_e^7)$  vanishes (if CKM is unit matrix).

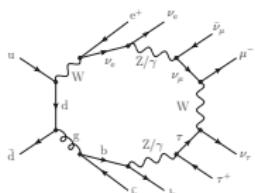


**NLO<sub>1</sub>**: genuine NLO QCD to LO QCD (expected to be dominant NLO), up to 7-point functions in virtual corr., challenging real corr. (high-multiplicity). Real channels with initial states  $q\bar{q}$ ,  $gq$ . First computed [Bevilacqua et al. 2005.09427, Denner GP 2007.12089].

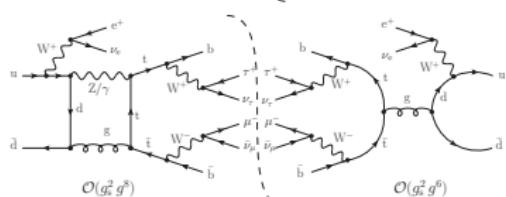
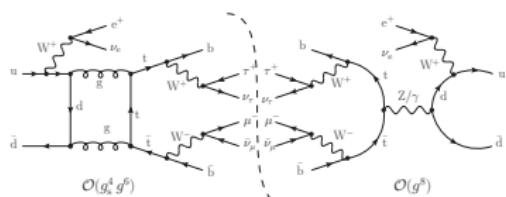
# NLO<sub>2</sub> contribution

**NLO<sub>2</sub>:** EW corrections to LO QCD plus QCD corrections to LO interference.

Up to 10-point functions in virtuals.



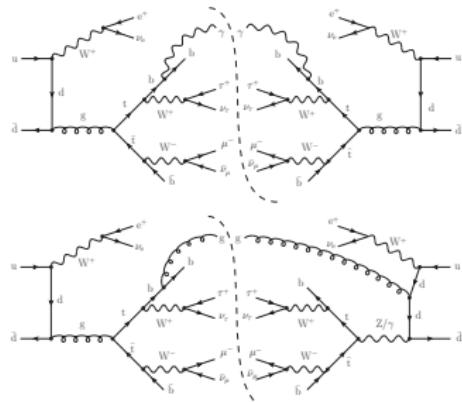
Two contributions:



High-multiplicity reals ( $2 \rightarrow 9$ ) and large number of IR-singular configurations.

Channels:  $q\bar{q}, \gamma q, gq$  ( $\gamma q$  suppressed by PDFs).

QCD real corr. to LO interf. is non-zero if gluon is emitted by the initial state and absorbed by final state.



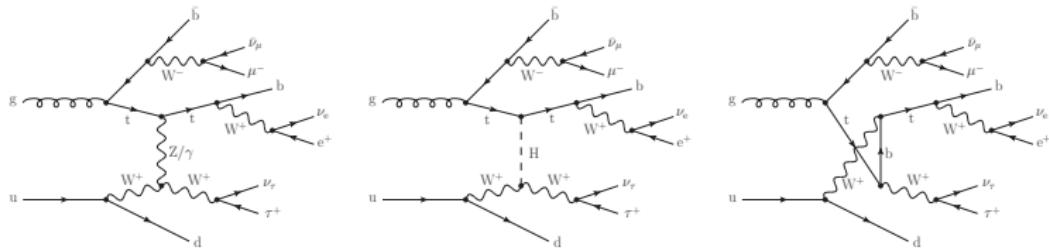
Virtual IR poles for  $\mathcal{O}(g_s^2 g^8) \times \mathcal{O}(g_s^2 g^6)$  are cancelled by both classes of reals:  
only the sum of all contributions is IR safe!

# NLO<sub>3</sub> and NLO<sub>4</sub> contributions

**NLO<sub>3</sub>:** pure QCD corrections to LO EW (EW corrections do not change color structure of LO interference) → enable simple matching to QCD PS (as NLO<sub>1</sub>).

Expected to be subleading but larger than NLO<sub>2</sub> (already for on-shell production [Frederix et al. 1711.02116, 1804.10017]).

Dominated by **gq-channel** contribution, that embeds  $tW^+ \rightarrow tW^+$  scattering:



**NLO<sub>4</sub>:** EW corrections to LO<sub>EW</sub>, amount at 0.04% of LO<sub>QCD</sub> at inclusive level [Frederix et al. 1711.02116]. Out of reach (fiducial phase-space) even at HL-LHC → negligible.

# Combining NLO EW and QCD: setup

$p p \rightarrow b \bar{b} e^+ \nu_e \mu^- \bar{\nu}_\mu \tau^+ \nu_\tau + X$  at  $\mathcal{O}(\alpha_s^3 \alpha^6)$ ,  $\mathcal{O}(\alpha_s^2 \alpha^7)$ ,  $\mathcal{O}(\alpha_s \alpha^8)$  [Denner GP 2102.03246]

- full tree-level and one-loop amplitudes: RECOLA1 [Actis et al. 1605.01090]
- 1-loop tensor-integral reduction and evaluation: COLLIER [Denner et al. 1604.06792]
- multi-channel integration with MoCANLO in-house Monte Carlo
- dipole subtraction of IR singularities [Catani Seymour 9605323, Dittmaier 9904440]
- complex-mass scheme [Denner et al. 9904472] for W, Z, top
- NNPDF3.1 NLO LUXQED PDFs (photon included, [Bertone et al. 1712.07053]) for both LO and NLO;  $N_F = 5$
- $\Gamma_t$  computed including NLO QCD+EW corrections [Basso et al. 1507.04676] (for both LO and NLO).

**Selections**, mimic those of Ref. [ATLAS 1901.03584]:

2 b-jets (anti- $k_t$ ,  $R = 0.4(0.1)$  for jet (photon) clustering,  $p_{T,b} > 25$  GeV,  $|\eta_b| < 2.5$ ),  
3 ch. leptons ( $p_{T,\ell} > 27$  GeV,  $|\eta_\ell| < 2.5$ ,  $\Delta R_{\ell b} > 0.4$ ).

**Three central-scale choices:**  $\mu_0^{(c)} = H_T/3$ ,  $\mu_0^{(d)} = \sqrt{M_{T,t} M_{T,\bar{t}}}$ ,  $\mu_0^{(e)} = \sqrt{M_{T,t} M_{T,\bar{t}}}/2$ .

# Combining NLO EW and QCD: integrated cross-sections

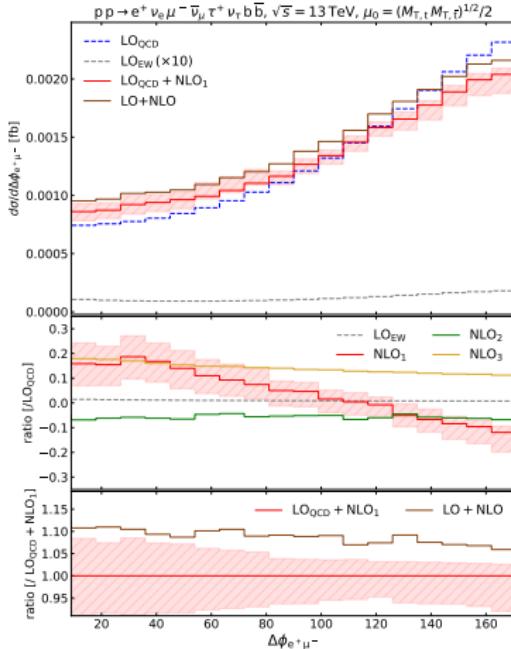
Fiducial cross-sections [Denner GP 2102.03246]:

order	$\mu_0^{(c)}$		$\mu_0^{(d)}$		$\mu_0^{(e)}$	
	$\sigma$ (fb)	ratio	$\sigma$ (fb)	ratio	$\sigma$ (fb)	ratio
LO <sub>QCD</sub> ( $\alpha_s^2 \alpha^6$ )	0.2218(1) <sup>+25.3%</sup> <sub>-18.8%</sub>	1	0.1948(1) <sup>+23.9%</sup> <sub>-18.1%</sub>	1	0.2414(1) <sup>+26.2%</sup> <sub>-19.3%</sub>	1
LO <sub>EW</sub> ( $\alpha^8$ )	0.002164(1) <sup>+3.7%</sup> <sub>-3.6%</sub>	0.010	0.002122(1) <sup>+3.7%</sup> <sub>-3.6%</sub>	0.011	0.002201(1) <sup>+3.7%</sup> <sub>-3.6%</sub>	0.009
NLO <sub>1</sub> ( $\alpha_s^3 \alpha^6$ )	0.0147(6)	0.066	0.0349(6)	0.179	0.0009(7)	0.004
NLO <sub>2</sub> ( $\alpha_s^5 \alpha^7$ )	-0.0122(3)	-0.055	-0.0106(3)	-0.054	-0.0134(4)	-0.056
NLO <sub>3</sub> ( $\alpha_s \alpha^8$ )	0.0293(1)	0.131	0.0263(1)	0.135	0.0320(1)	0.133
LO <sub>QCD</sub> +NLO <sub>1</sub>	0.2365(6) <sup>+2.9%</sup> <sub>-6.0%</sub>	1.066	0.2297(6) <sup>+5.5%</sup> <sub>-7.3%</sub>	1.179	0.2423(7) <sup>+3.5%</sup> <sub>-5.2%</sub>	1.004
LO <sub>QCD</sub> +NLO <sub>2</sub>	0.2094(3) <sup>+25.0%</sup> <sub>-18.7%</sub>	0.945	0.1840(3) <sup>+23.8%</sup> <sub>-17.9%</sub>	0.946	0.2277(4) <sup>+25.9%</sup> <sub>-19.2%</sub>	0.944
LO <sub>EW</sub> +NLO <sub>3</sub>	0.03142(4) <sup>+22.2%</sup> <sub>-16.8%</sub>	0.141	0.02843(6) <sup>+20.5%</sup> <sub>-15.6%</sub>	0.146	0.03425(7) <sup>+22.8%</sup> <sub>-17.0%</sub>	0.142
LO+NLO	0.2554(7) <sup>+4.0%</sup> <sub>-6.5%</sub>	1.151	0.2473(7) <sup>+6.3%</sup> <sub>-7.6%</sub>	1.270	0.2628(9) <sup>+4.3%</sup> <sub>-5.9%</sub>	1.089

- NLO<sub>1</sub>-corr. impact depends a lot on scale choice (from +0.5% to +18%)
- NLO<sub>2</sub> and NLO<sub>3</sub> relative corr. are scale-independent: -5% and +13% resp.
- LO<sub>EW</sub> is 1% of LO<sub>QCD</sub>, NLO<sub>3</sub> corr. 10 times larger than its LO (tW scattering)
- scale-uncertainties dominated by NLO<sub>1</sub>:  $\approx \pm 5\%$  for combined NLO result

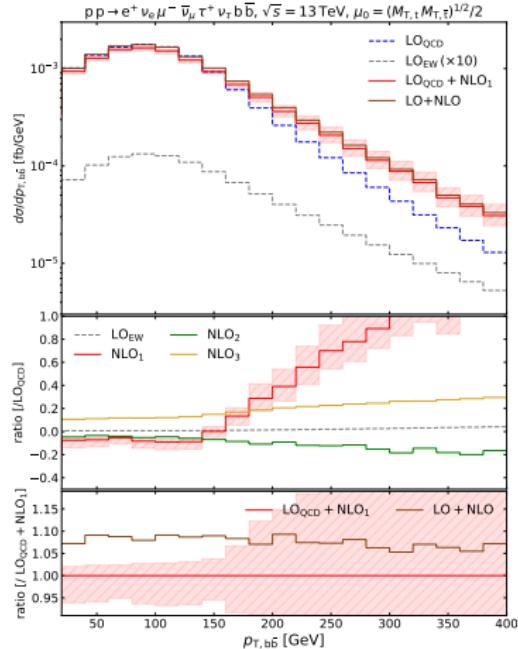
# Combining NLO EW and QCD: differential results

## Azimuthal separation between $e^+$ and $\mu^-$



- NLO<sub>1</sub> diminish with constant slope, NLO<sub>2</sub>+NLO<sub>3</sub> give a rather flat correction to LO+NLO<sub>1</sub>.

## Transverse momentum of $b\bar{b}$ system



- Very large NLO<sub>1</sub> correction for  $p_{T,bb} > 150$  GeV. Small NLO corrections in the soft region.

# NLO<sub>1</sub>: numerical setups

“Aachen group” [Bevilacqua et al. 2005.09427]

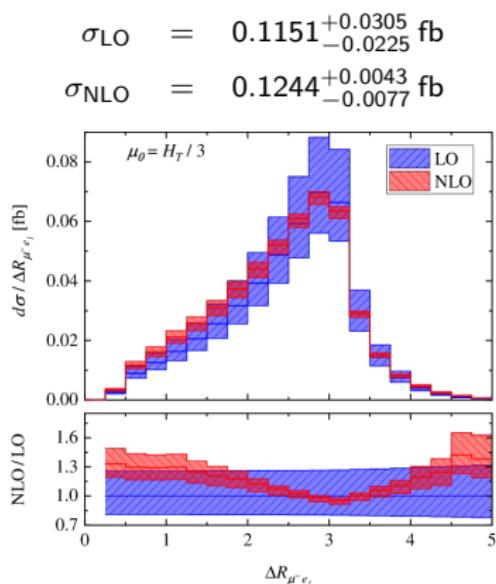
- ★  $p p \rightarrow b \bar{b} e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e + X$  (+ cc)
- Full tree/one-loop amplitudes and MC integration with HELAC-NLO framework [G. Bevilacqua et al. 1110.1499]
- Dipole [Catani, Seymour 9605323] and Nagy-Soper [Bevilacqua et al. 1308.5605] subtractions
- Complex-mass [Denner et al. 9904472] for top, fixed width for W, Z.
- CT14, MMHT14 and NNPDF3.0 (N)LO PDFs,  $N_F = 5$
- ★ **Selections:** 2 b-jets (anti- $k_t$ ,  $R = 0.4$ ,  $p_{T,b} > 25$  GeV,  $|\eta_b| < 2.5$ ), 3 ch. leptons ( $p_{T,\ell} > 25$  GeV,  $|\eta_\ell| < 2.5$ ,  $\Delta R_{\ell b} > 0.4$ ,  $\Delta R_{\ell\ell} > 0.4$ ).

“Würzburg group” [Denner, GP 2007.12089]

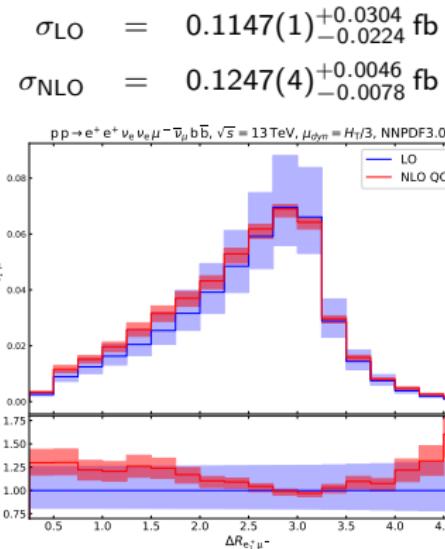
- ★  $p p \rightarrow b \bar{b} e^+ \nu_e \mu^- \bar{\nu}_\mu \tau^+ \nu_\tau + X$
- Full tree/one-loop amplitudes with RECOLA [Actis et al. 1605.01090] + COLLIER [Denner et al. 1604.06792], MC integration with MoCANLO
- Dipole subtraction [Catani, Seymour 9605323]
- Complex-mass scheme [Denner et al. 9904472] for W, Z, top
- NNPDF3.1 (N)LO PDFs,  $N_F = 5$
- ★ **Selections:** 2 b-jets (anti- $k_t$ ,  $R = 0.4$ ,  $p_{T,b} > 25$  GeV,  $|\eta_b| < 2.5$ ), 3 ch. leptons ( $p_{T,\ell} > 27$  GeV,  $|\eta_\ell| < 2.5$ ,  $\Delta R_{\ell b} > 0.4$ ).

# NLO<sub>1</sub>: comparison of the two calculations

Good agreement using the setup of Ref. [Bevilacqua et al. 2005.09427], both at integrated and differential level (also for scale unc. and  $K$ -factors).



[Bevilacqua et al. 2005.09427]



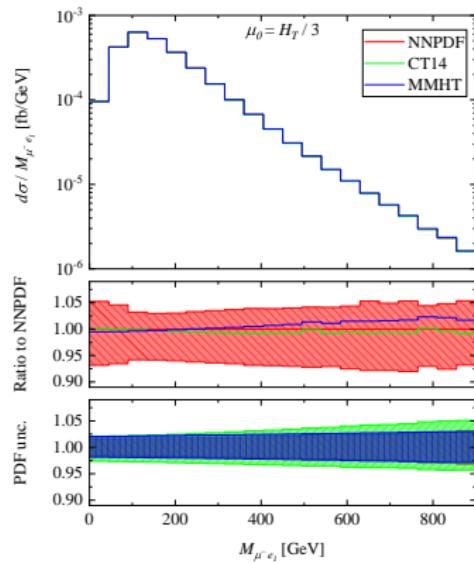
[Denner, GP 2007.12089]

# NLO<sub>1</sub>: theory uncertainties and scale dependence

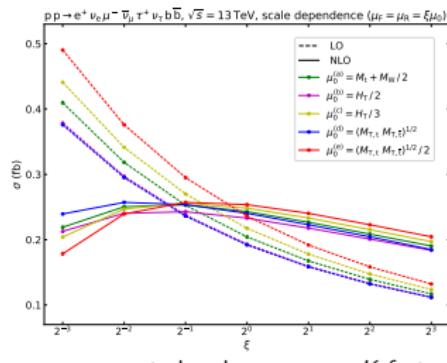
NLO QCD corrections substantially reduce scale-uncertainties (from 25% to 5%)

[Bevilacqua et al. 2005.09427, Denner GP 2007.12089].

QCD-scale variations give the dominant source of theory unc., PDF unc. are of order 2-3% [Bevilacqua et al. 2005.09427]



QCD K-factors range between 1.07 and 1.25 depending on the central-scale choice  
[Denner GP 2007.12089]:

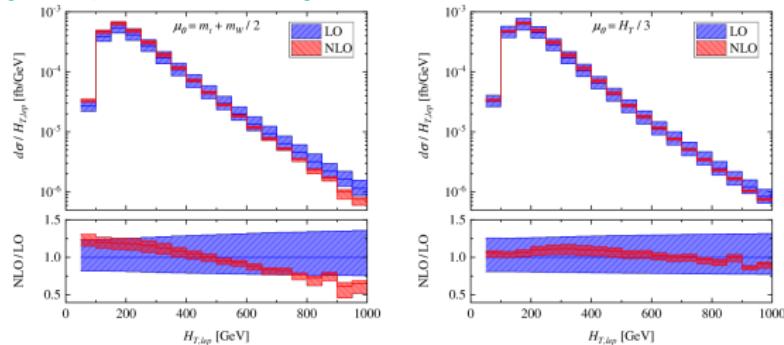


central scale	K-fact.
$\mu_0^{(a)} = M_t + M_{W^{\pm}}/2$	1.20
$\mu_0^{(b)} = H_T/2$	1.21
$\mu_0^{(c)} = H_T/3$	1.13
$\mu_0^{(d)} = (M_{T,\ell}, M_{\bar{T}}, \ell)^{1/2}$	1.25
$\mu_0^{(e)} = (M_{T,\ell}, M_{\bar{T}}, \ell)^{1/2}/2$	1.07

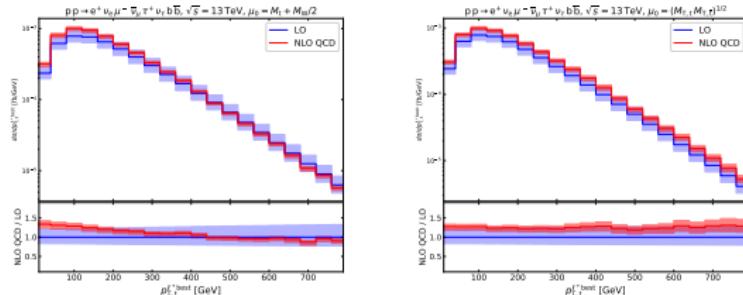
# NLO<sub>1</sub>: fixed vs dynamical scale

Dynamical-scale choices give flatter  $K$ -factors than fixed ones.

The  $H_T/3$  choice sizeably improves perturbative convergence. Fig: scalar sum of lepton  $p_T$ 's [Bevilacqua et al. 2005.09427].



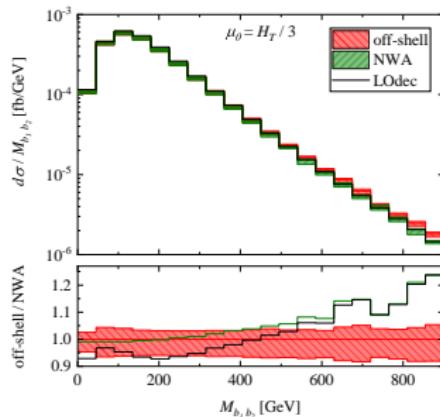
The resonance-aware choice ( $\sqrt{M_{T,t} M_{T,\bar{t}}}$ ) also performs well, similar results as  $H_T/3$  (larger scale unc.). Fig: best-reco. top  $p_T$  [Denner, GP 2007.12089].



# Full off-shell vs narrow-width

Comparison at NLO QCD between full off-shell calculation and two narrow-width approximations (NWA, with/without NLO corr. in  $t/\bar{t}$  decays) [Bevilacqua et al. 2005.09427].

$\mu_0 = H_T / 3$	LO	NLO QCD
full off-shell	115.1 $+30.5\ (26\%)$ $-22.5\ (20\%)$	124.4 $+4.3\ (3\%)$ $-7.7\ (6\%)$
NWA	115.1 $+30.4\ (26\%)$ $-22.4\ (19\%)$	124.2 $+4.1\ (3\%)$ $-7.7\ (6\%)$
NWA <sub>LO decay</sub>	"	130.7 $+13.6\ (10\%)$ $-13.2\ (10\%)$



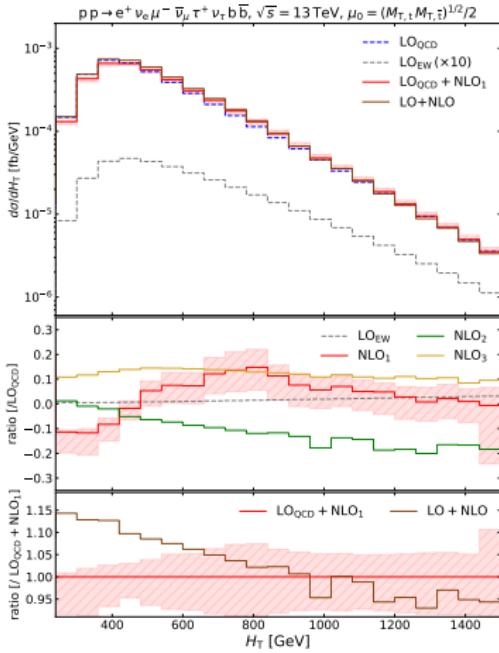
More recent detailed comparison → [Bevilacqua et al. 2109.15181].

# NLO EW and QCD: integrated cross-sections

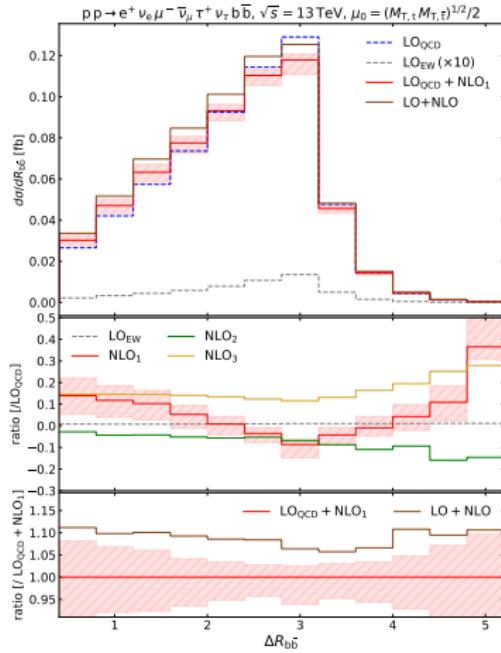
central scale	LO	NLO QCD	K-fact.
$\mu_0^{(a)} = M_t + M_W/2$	$0.2042(1)^{+23.8\%}_{-18.0\%}$	$0.2452(7)^{+4.5\%}_{-6.8\%}$	1.20
$\mu_0^{(b)} = H_T/2$	$0.1931(1)^{+23.0\%}_{-17.5\%}$	$0.2330(9)^{+4.2\%}_{-6.5\%}$	1.21
$\mu_0^{(c)} = H_T/3$	$0.2175(1)^{+24.2\%}_{-18.2\%}$	$0.2462(8)^{+2.8\%}_{-5.8\%}$	1.13
$\mu_0^{(d)} = (M_{T,t} M_{T,\bar{t}})^{1/2}$	$0.1920(1)^{+23.0\%}_{-17.5\%}$	$0.2394(6)^{+5.4\%}_{-7.2\%}$	1.25
$\mu_0^{(e)} = (M_{T,t} M_{T,\bar{t}})^{1/2}/2$	$0.2360(1)^{+24.9\%}_{-18.7\%}$	$0.2535(8)^{+3.4\%}_{-5.2\%}$	1.07

# NLO EW and QCD: more distributions (1)

$H_T$  variable

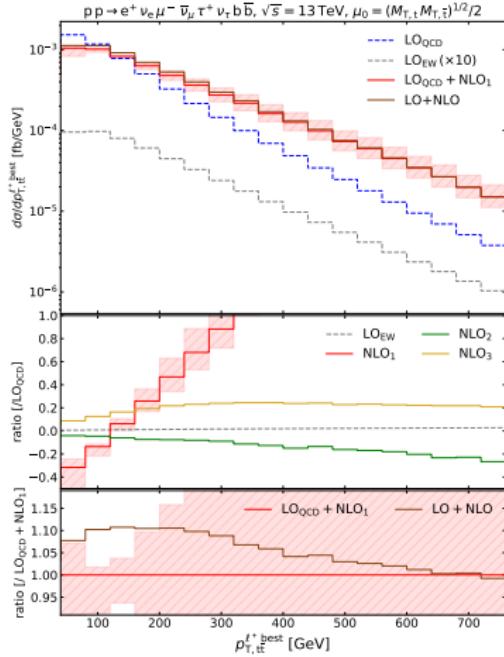


$R$ -distance between the two b-jets

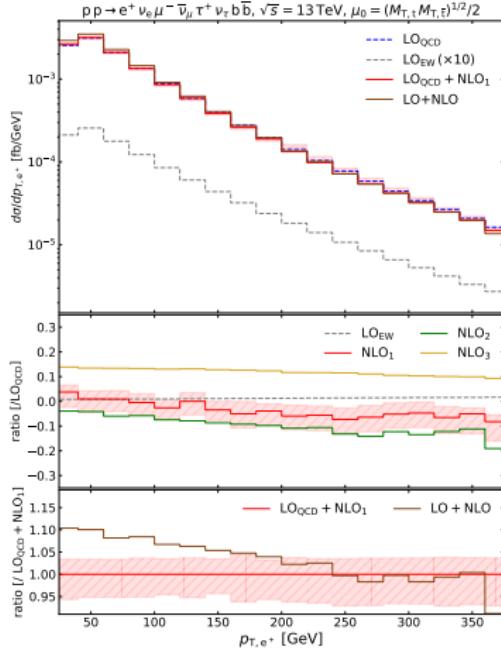


## NLO EW and QCD: more distributions (2)

Transverse momentum of the  $t\bar{t}$  system

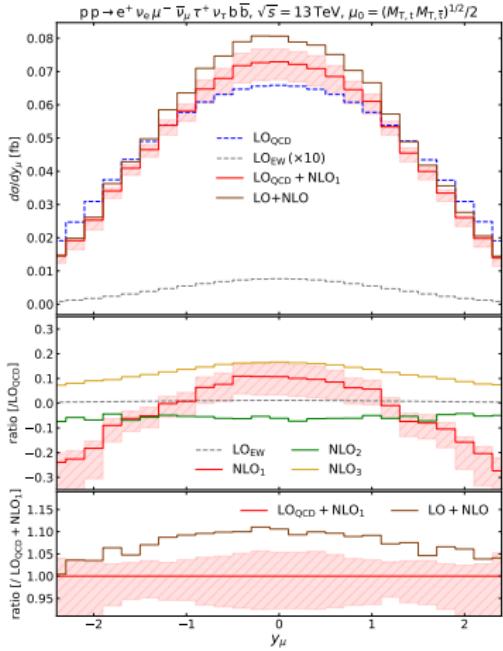


Transverse momentum of the positron

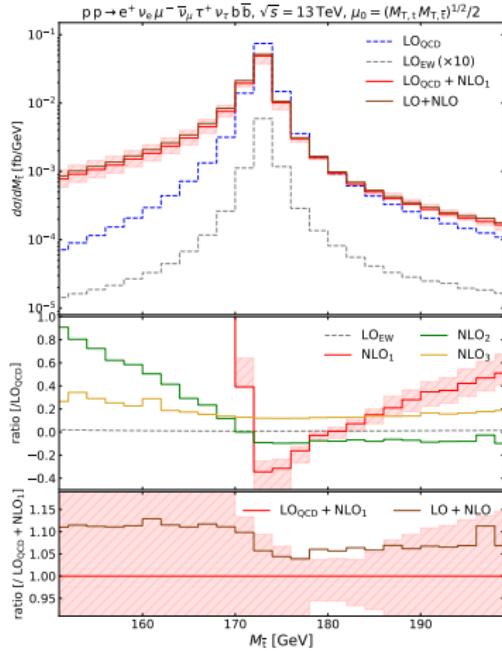


# NLO EW and QCD: more distributions (3)

Rapidity of the muon



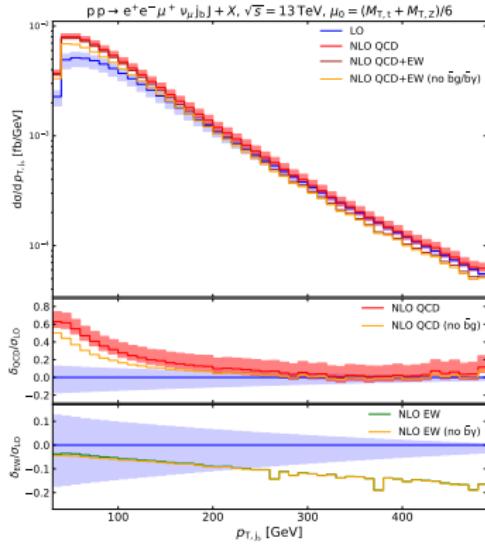
Invariant mass of the antitop quark



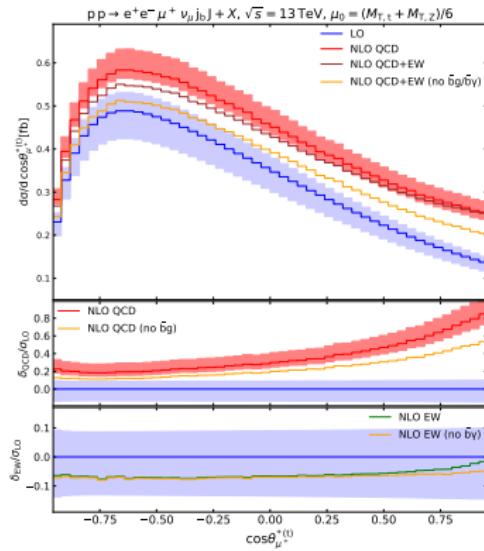
# Backup (tZj)

# Transverse-momentum and angular distributions

## Transverse momentum of the spectator jet

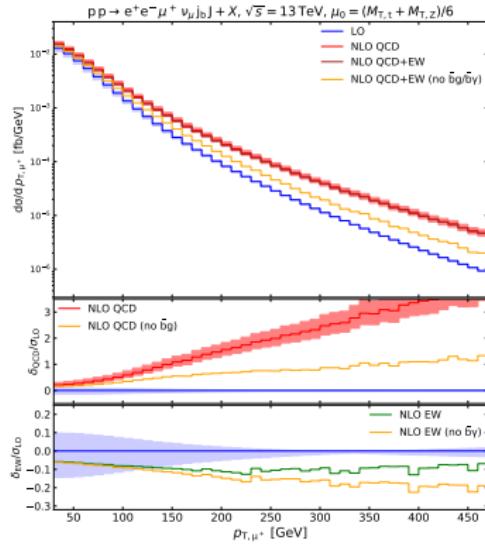


## Polarisation-sensitive polar angle of the antimuon in the top-quark rest frame

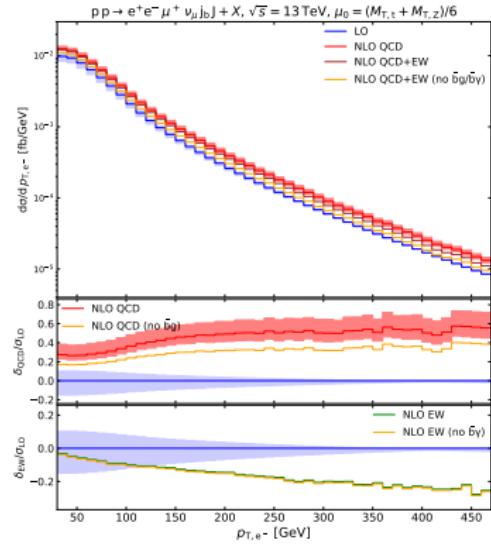


# Transverse-momentum distributions for leptons

Antimuon (top-quark decay)

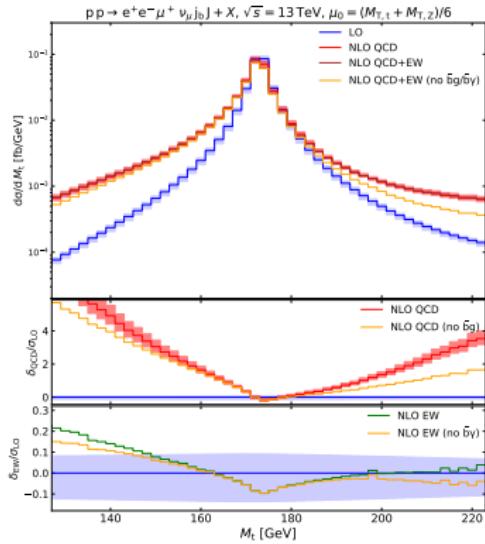


Electron (Z-boson decay)

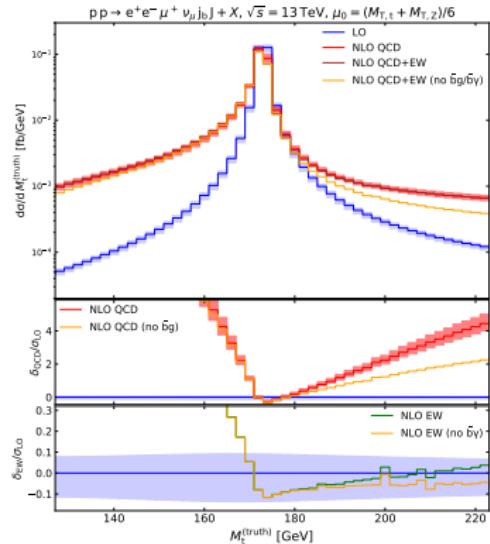


# Invariant-mass distributions (1)

Reconstructed top quark

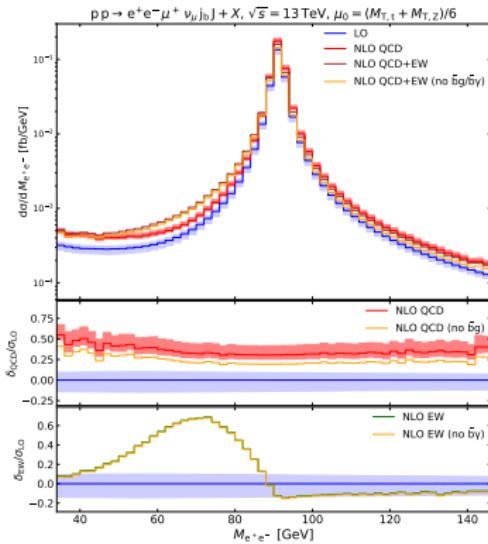


MC-truth top quark

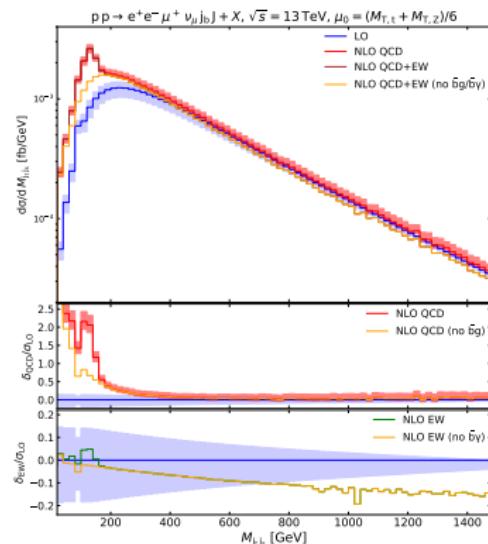


## Invariant-mass distributions (2)

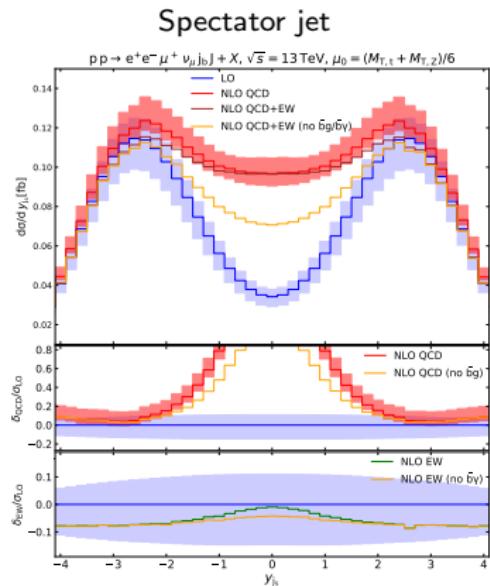
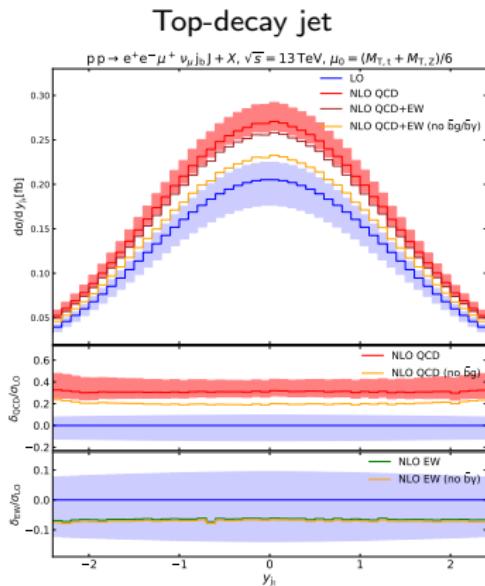
Z-boson



Di-jet



# Rapidity distributions



# Combining NLO EW and QCD: setup

$p p \rightarrow e^+ e^- \mu^+ \nu_\mu j_b J + X$  at  $\mathcal{O}(\alpha_s \alpha^6)$  and  $\mathcal{O}(\alpha^7)$  [Denner GP Schwan 2207.11264]

- full tree-level and one-loop amplitudes: RECOLA1 [Actis et al. 1605.01090]
- 1-loop tensor-integral reduction and evaluation: COLLIER [Denner et al. 1604.06792]
- multi-channel integration with MoCANLO in-house Monte Carlo
- dipole subtraction of IR singularities [Catani Seymour 9605323, Dittmaier 9904440]
- complex-mass scheme [Denner et al. 9904472] for W, Z, top
- NNPDF3.1 NNLO LUXQED PDFs (photon included, [Bertone et al. 1712.07053]);
- $\Gamma_t$  computed including NLO QCD+EW corrections [Basso et al. 1507.04676].

Selections mimic those of [ATLAS 2002.07546].

**Jets:** b-jets ( $j_b$ ) and light jets ( $j$ ) clustered with  $k_t$  algorithm [Catani et al. Nucl.Phys.B406(1993)] and  $R = 0.4$ ,  $N_b \geq 1$ ,  $N_{j_b} + N_j \geq 2$ ,  $p_{T,j_b}, p_{T,j} > 35\text{GeV}$ ,  $|y_{j_b}| < 2.5$ ,  $|y_j| < 4.5$

**Leptons** 3 dressed leptons clustered with  $k_t$  algorithm and  $R = 0.1$ ,  $p_{T,\ell_1} > 28\text{GeV}$ ,  $p_{T,\ell} > 20\text{GeV}$ ,  $|y_\ell| < 2.5$ ,  $M_{e^+e^-} > 30\text{GeV}$ ,  $\Delta R_{\ell J} > 0.4$

**Central-scale choice:**  $\mu_0 = (M_{T,t} + M_{T,z})/6$  (inspired by [Pagani et al. 2006.10086]).